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Pricing and warranty decisions in a two-period closed-loop supply chain

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For a two-period closed-loop supply chain (CLSC) consisting of a manufacturer and a retailer, Stackelberg game analyses are conducted to examine pricing and warranty decisions under two warranty models depending on who offers warranty for new and remanufactured products and the corresponding benchmark models with a warranty for new products only. Next, we identify the conditions under which warranty for remanufactured products is offered and investigate how this warranty affects the CLSC operations. Subsequently, comparative studies are carried out to examine equilibrium decisions, profitability and consumer surplus of the CLSC between the two warranty models. Analytical results show that offering warranty for remanufactured products does not affect new product pricing in period 2, but influences the pricing of new products in period 1 and remanufactured products in period 2, thereby enhancing remanufacturing, individual and channel profitability, and consumer surplus. Compared to the retailer warranty for remanufactured products, the manufacturer warranty can attain a more equitable profit distribution. If the warranty cost advantage of the manufacturer (retailer) is significant relative to that of the retailer (the manufacturer), the manufacturer (retailer) arises as a natural choice to offer warranty for remanufactured products as this decision enhances both profitability and consumer surplus.

Keywords: Closed-loop supply chain (CLSC); remanufacturing; warranty; pricing decision; Stackelberg game

1. Introduction

Remanufacturing is often considered as an ideal choice for recycling and reuse of used products (Esenduran, Kemahlioğlu-Ziya, and Swaminathan 2016). As a sustainable and green development mode, remanufacturing fosters the formation of a recycling industrial chain and lays the foundation for green and circular development of the economy. Governments at different levels have issued diverse regulatory policies to encourage remanufacturing. For instance, in July 2013, led by the National Development and Reform Commission, China's five ministries jointly issued *the Pilot Program on 'Bartering Used for Remanufactured Products'* to promote remanufacturing. In 2015, the United States House of Representatives passed the *Federal Vehicle Repair Cost Savings Act* to require federal agencies to consider using remanufactured parts for vehicle fleet repairs. Since more and more countries recognise the importance of and commit support to remanufacture, an increasing number of enterprises are entering the remanufacturing arena (such as Kodak, Xerox, Siemens, Lenovo and Caterpillar), resulting in rapid growth in the remanufacturing industry. In 2013, the annual sales of the global remanufacturing industry were more than 150 billion U.S. dollars and the United States alone reached more than 100 billion U.S. dollars (Liu, Wu, et al. 2017). Meanwhile, remanufacturing has also drawn significant attention from academia and has been extensively studied in recent years (Savaskan, Bhattacharya, and Van Wassenhove 2004; Atasu, Van Wassenhove, and Sarvary 2009; Ferrer and Swaminathan 2010; Özdemir and Denizel 2012; Ma et al. 2016; Wang et al. 2017; Liu et al. 2019).

Although remanufacturing has made significant progress in theory and practice, it still faces many challenges such as consumers' low perceived quality and willingness-to-pay for remanufactured products (Abbey et al. 2015). Among all factors influencing consumers' willingness-to-pay for remanufactured products, the retail price and consumers' perceived quality are the two most important considerations. Understandably, the lower the retail price and the higher the perceived quality, the greater the demand for remanufactured products (Abbey et al. 2015). However, if the remanufactured product is priced too low, consumers may lose confidence in its quality. Therefore, it is not viable to purely rely on aggressive pricing to stimulate demand for remanufactured products (Esenduran, Kemahltoğlu-Ziya, and Swaminathan 2016). In many cases, remanufactured and new products have comparable levels of quality, but consumers tend to discount the quality of remanufactured products. If effective methods can be developed to improve consumers' perception on the quality of

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remanufactured products or appropriate mechanisms that can be devised to convey to consumers the right quality signal of remanufactured products, their market demand will be properly stimulated (Abbey et al. 2015). Generally speaking, the product warranty is a proven mechanism to signal product quality to consumers. A longer warranty period tends to enhance consumers' confidence in and perception of product quality (Dai, Zhou, and Xu 2012). Therefore, offering a warranty for remanufactured products is presumably able to strengthen consumers' willingness-to-pay.

Researchers have conducted some studies on warranty policies for remanufactured products (Zhu et al. 2016; Alqahtani and Gupta 2017; Liao 2018), and their results indicate that a warranty policy for remanufactured products, such as a refund warranty, can enhance the remanufacturer's profit. In a CLSC where the manufacturer is responsible for remanufacturing, operational decisions are often made in two or multiple periods. For instance, for a two-period CLSC with remanufacturing, the manufacturer prices and provides warranty for new products in the first period and, then, collects used products to produce remanufactured products, prices and provides warranty for both products in the second period. In this context, it would be interesting to know if the results obtained from a single-period model are still applicable to the two-period model. Furthermore, a warranty for products can be provided by either the manufacturer or the retailer (Dai, Zhou, and Xu 2012; Bian et al. 2019). So, it is a worthy topic to investigate who is a better choice to offer a warranty for new and remanufactured products in terms of profitability and consumer surplus in a two-period setting. We attempt to deal with this significant problem by resorting to Stackelberg game analyses. In reality, a warranty policy for new and remanufactured products such as scope, free replacement, and refund (Alqahtani and Gupta 2017; Liao 2018). In this research, we focus on the warranty period of free replacement to investigate the provider's warranty decision and its efficiency.

More specifically, this study first examines the pricing and warranty period decisions under two warranty models where either the manufacturer or the retailer offers warranty for new and remanufactured products and the corresponding benchmark models with a warranty for new products only in a two-period CLSC. We then investigate the impact of warranty on the operational decisions and efficiency of the CLSC from the perspectives of individual and channel profitability as well as consumer surplus. Subsequently, we explore who arises as a better warranty provider from the manufacturer's, retailer's, CLSC's and consumer's angle. This study attempts to address the following three questions.

- How does the warranty affect the pricing decisions of new products in both periods and of remanufactured products in the second period?
- Does warranty enhance market demand for remanufactured products and the profit of the warranty provider and the other CLSC member?
- Is the manufacturer or the retailer a better warranty provider in terms of individual and channel profitability as well as consumer surplus?

The remainder of this paper is organised as follows. Section 2 conducts a brief literature review. Section 3 presents the problem description and assumptions. Section 4 establishes two-period CLSC Stackelberg game models with the manufacturer or the retailer being the warranty provider for new and remanufactured products as well as the corresponding benchmark models with a warranty for new products only, and derives their equilibrium solutions. In Section 5, we discuss the effect of offering warranty for remanufactured products on the operations of the CLSC, and analyse the warranty efficiency in the two warranty models. Section 6 presents a numerical experiment to illustrate the propositions and reports further results for more general cases. Conclusions are drawn in Section 7.

2. Literature review

This paper draws on and contributes to two streams of literature: pricing decisions of CLSCs and warranty policies for new and second-hand (remanufactured) products.

2.1. Pricing decisions of CLSCs

Extensive research has been conducted on pricing decisions of new, used and remanufactured products in CSLCs under different contexts. For example, some researchers focus on the optimal pricing under certain government regulations (Atasu, Van Wassenhove, and Sarvary 2009; Özdemir and Denizel 2012; Esenduran, Kemahlıoğlu-Ziya, and Swaminathan 2016; Liu, Tang, et al. 2017; Zhou, Zheng, and Huang 2017; Wang, Ding, and Sun 2018), some literature investigates these pricing decisions under different collection patterns (Savaskan, Bhattacharya, and Van Wassenhove 2004; Atasu, Toktay, and Van Wassenhove 2013; Govindan, Feng, and Li 2017; He et al. 2019) and various decision structures (Ferrer and Swaminathan 2006, 2010; Xiong et al. 2013; Wang et al. 2017). In addition, many articles jointly optimise pricing and

other decisions such as product design (Örsdemir, Kemahlıoğlu-Ziya, and Parlaktürk 2014; Wu 2013), remanufacturing authorisation (Oraiopoulos, Ferguson, and Toktay 2012; Hong et al. 2017) and warranty policy decisions.

It is a relatively new research topic to consider the pricing decision under warranty for new or remanufactured products. By assuming both linear and nonlinear demand functions for remanufactured products in a single period setting, Yazdian, Shahanaghi, and Makui (2014) investigate the remanufacturer's optimal collection price of used products, sale price and warranty period of remanufactured products. Zhu et al. (2016) optimise the warranty length and selling price for remanufactured products under free-replacement and extended warranty services from the remanufacturer's perspective and their empirical analysis indicates that the remanufacturer profits more from the free-replacement warranty than the extended warranty service. Liao (2018) focuses on a partial-refund warranty policy for remanufactured products and develops a newsvendor model to explore the impact of this warranty policy on product pricing decisions, members' profits and consumer surplus. Giri, Mondal, and Maiti (2018) assume that the warranty period for new products affects the collection quantity of used products and investigate the optimal price of new and remanufactured products and warranty period of new products when the manufacturer refurbishes and remanufactures defective products.

This brief literature review reveals that extant research tends to focus on warranty for either new or remanufactured products in a single period and does not consider pricing decisions with warranty offerings to both products by the same warranty provider. In contrast, this paper incorporates warranty for both new and remanufactured products in a two-period CLSC setting and examines the impact of offering a warranty on the pricing decisions of both products in different periods.

2.2. Warranty for new and second-hand (remanufactured) products

Researchers have conducted extensive studies on product warranty from different angles. Warranty studies in operational management can be grouped into three streams: Estimation of warranty cost, optimisation of the warranty service level and efficiency analysis of warranty policies.

Warranty cost depends on product reliability, rectification and warranty terms, so a bulk of literature considers it from the angles of the product failure rate and warranty policy at the component and product level (Murthy and Djamaludin 2002; Wang and Xie 2018). For new products, Polatoglu and Sahin (1998) derive a probability distribution of the warranty cost for pro-rata warranties; Liu, Wu, and Xie (2015) develop warranty cost models for series and parallel systems with failure interaction under renewing free-replacement warranty; Park, Jung, and Park (2016) develop a new warranty cost model for a renewable two-dimensional policy based on failure time and warranty servicing time; Zhang, Fouladirad, and Barros (2018) analyse the expected warranty cost for non-renewing and renewing free replacement policy in a two-series system with stochastically dependent components; Luo and Wu (2019) estimate the warranty cost originated from software, hardware failures or human errors as well as their interactions. As for second-hand products, Chattopadhyay and Murthy (2000) develop probabilistic models to estimate their expected warranty cost under free replacement or pro-rata warranty at the component and system level. Shafiee et al. (2011) estimate the warranty cost based on past age, usage, service strategy and reliability of second-hand products. Algahtani and Gupta (2017) examine the impact of warranty for remanufactured products from a remanufacturer's perspective and furnish an approach to minimise the warranty cost. The aforesaid literature provides theoretical bases for optimising warranty policies and many studies build upon these warranty cost models to examine their specific problems (Chen, Li, and Zhou 2012; Wei, Zhao, and Li 2015; Dan, Zhang, and Zhou 2017; Giri, Mondal, and Maiti 2018; Luo and Wu 2018). This paper differs from existing literature by combining the features of the cost structure in two papers (Chen, Li, and Zhou 2012; Wei, Zhao, and Li 2015) and takes a more generic form to model the warranty cost in our CLSC.

The warranty service level can be reflected in different aspects, ranging from the length of the warranty period, the comprehensive service level consisting of warranty period and coverage, to refund due to product failure. For new products, Chen, Li, and Zhou (2012), Chen, Lo and Weng (2017), Chien (2005), Esmaeili, Shamsi, and Asgharizadeh (2014), Giri, Mondal, and Maiti (2018), Park, Jung, and Park (2016), Taleizadeh et al. (2017), Wei, Zhao, and Li (2015), Xie (2017) and Zhang et al. (2019) explore the optimal warranty period under different specific scenarios. Dan, Zhang, and Zhou (2017) investigate the optimal warranty service level, added-value service level and their interaction in a cooperative and competitive context. Li et al. (2018) formulate a two-period model to analyse the optimal warranty compensation strategy when the consumer's quality perception and valuation change. For second-hand and remanufactured products, Chattopadhyay and Murthy (2010), Lu and Shang (2019) study the optimal warranty for second-hand products; Yazdian, Shahanaghi, and Makui (2014) and Zhu et al. (2016) optimise the warranty period of remanufactured products. This literature review shows that it is a key concern to determine the warranty period and this has been extensively studied. However, existing research is typically confined to a single period setting and optimising the warranty period for a single product (either new, second-hand, or

remanufactured product). In contrast, this paper establishes a two-period CLSC where a warranty provider (either the manufacturer or the retailer) furnishes a warranty for new products in both periods and warranty for remanufactured products in the second period. This new model setup allows us to determine the optimal warranty period of remanufactured products and examine how the operations of the two-period CLSC is affected by offering warranty for both new and remanufactured products.

In the stream of warranty efficiency, Zhou, Li, and Tang (2009) compare a non-renewing with a renewing warranty policy for repairable products with known market entry and departure under consumer's risk aversion. Their research reveals that the renewing warranty policy is more conductive to the warranty provider. Dai, Zhou, and Xu (2012) focus on the impact of product quality and warranty period decisions on supply chain performance under two scenarios where the warranty period is determined by the manufacturer or the supplier. Chari et al. (2016) study the optimal warranty policy of a manufacturer who services products within the warranty period by replacing defective components with new or reconditioned ones. Mo, Zeng, and Xu (2017) provide a hybrid warranty policy combining free-replacement warranty with the buyer's investment in prevention management. Zhu, Jiao, and Yuan (2019) establish a model to determine the product reliability, warranty policy, pricing decisions in the period of regular and promotion sales, and compare four nonrenewable warranty policies to provide managerial insights on warranty policy selection. Existing literature pays more attention to the efficiency of different warranty policies, but this research assesses warranty efficiency from a service provider's perspective. More specifically, this paper examines warranty efficiency by allowing the manufacturer or the retailer to offer warranty for both new and remanufactured products in a two-period CLSC and this assessment is conducted under the criteria of profitability and consumer surplus.

Table 1 shows the difference between our paper with existing studies on pricing decisions in a CLSC and warranty decision in general supply chain management in a proper literature context. The literature review and Table 1 reveal that the majority of research is confined to either pricing or warranty decision for a single product (new, remanufactured, or second-hand product) and limited attention is dedicated to examining joint warranty and pricing decisions for remanufactured products in a single period (Yazdian, Shahanaghi, and Makui 2014; Zhu et al. 2016; Alqahtani and Gupta 2017; Liao 2018). On the other hand, the focus of this paper differs from existing studies in that it jointly optimises pricing and warranty decisions where either the manufacturer or the retailer provides warranty service for both new and remanufactured products in a two-period CLSC setting. We then examine the interaction of warranty and pricing decisions and the implications on the CLSC performance from both profitability and consumer surplus angles, thereby assessing warranty efficiency offered by different parties.

| Reference | Multi-period CLSC? | Warranty for new products? | Warranty for remanufactured products? | Warranty period? | The optimal warranty provider? |
|--|-----------------------|----------------------------|---|------------------|--------------------------------|
| Alqahtani and Gupta (2017) | N | Ν | Y | Ν | Ν |
| Chen, Li, and Zhou (2012) | Ν | Y | Ν | Y | N |
| Dai, Zhou, and Xu (2012) | Ν | Y | Ν | Y | Y |
| Esmaeili, Shamsi, and Asgharizadeh (2014) | Ν | Y | Ν | Y | Ν |
| Ferrer and Swaminathan (2010) | Y | N | N | Ν | Ν |
| Giri, Mondal, and Maiti (2018) | Ν | Y | N | Y | Ν |
| He et al. (2019) | Ν | N | N | Ν | Ν |
| Liao (2018) | Ν | N | Y | Ν | Ν |
| Li et al. (2018) | Y | Y | N | Ν | Ν |
| Park et al.(2016) | Ν | Y | N | Y | Ν |
| Savaskan, Bhattacharya, and Van Wassenhove (2004) | Ν | Ν | Ν | Ν | Ν |
| Taleizadeh et al. (2017) | Ν | Y | N | Y | Ν |
| Wang, Ding, and Sun (2018) | Y | N | N | Ν | Ν |
| Wei, Zhao, and Li (2015) | Ν | Y | N | Y | Ν |
| Xie (2017) | N | Y | N | Y | N |
| Yazdian, Shahanaghi, and Makui (2014) | Ν | Ν | Y | Y | Ν |
| Zhu et al. (2016) | Ν | Ν | Y | Y | Ν |
| Zhu, Jiao, and Yuan (2019) | Ν | Y | Ν | Y | Ν |
| Our paper | Y | Y | Y | Y | Y |

Table 1. Literature positioning of this research and existing studies (Y = Yes; N = No).

3. Problem description and model assumptions

In a two-period CLSC consisting of a manufacturer and a retailer, the manufacturer is modelled as the leader and organises production in response to market demand for new products in period 1; in period 2, it continues to produce new products, collects and remanufactures used products as a result of new product sales in period 1. The retailer is modelled as the follower and sets the retail prices for new and remanufactured products to sell them to the end market. Generally, only a portion of used products can be collected and remanufactured, so $q_r \le \gamma q_1$, where $0 < \gamma \le 1$ is the collection yield and defined as the fraction of new products made in period 1 that is available for remanufacturing in period 2 (Ferrer and Swaminathan 2006, 2010; Atasu, Toktay, and Van Wassenhove 2013). Here, q_1 is the sale quantity of new products in period 1, q_r is the demand for remanufactured products in period 2. Conceptually, the profit obtained in period 2 should be discounted into the present value in period 1 (Ferrer and Swaminathan 2006, 2010). For simplicity and without loss of generality, we ignore this discount factor following extant literature (Ferguson and Toktay 2010; Wu 2013; Hong et al. 2017).

Remanufactured products are generally perceived to be of lower quality compared to new products, and consumers tend to demonstrate a loss-averse preference. Thus, to promote sales of remanufactured products, the manufacturer or retailer can resort to offering a warranty policy to boost consumers' confidence. Although a warranty policy for products typically contains different items (Alqahtani and Gupta 2017; Liao 2018), this research focuses on the warranty period of free replacement. Without loss of generality, the warranty period for new products is the same in the two periods and is denoted by *n* and that for remanufactured products is denoted by *t*. If t > 0, the manufacturer or retailer provides warranty for remanufactured products. If t = 0, the manufacturer or retailer does not provide warranty for remanufactured products. In general, *n* and *t* are different and $t \le n$ is commonly observed in practice. For instance, eBay provides a 5-year warranty period for a new Big Ball Canister vacuum cleaner but only a 2-year for a remanufactured one. Lenovo provides the same 1-year warranty period for new and refurbished laptops. For simplicity, we normalise *n* to 1 and assume that $t \le 1$. The results derived from this simplified case can be extended to the more general case when *n* is set at different values.

Consumers' willingness-to-pay for new products is set as v, which is assumed to be uniformly distributed in the whole market capacity Q in each period. Consumers' willingness-to-pay for remanufactured products in period 2 is set as δv , where $\delta \in [0, 1)$ denotes the consumer's value discount for remanufactured products. Given the warranty period n and t for new and remanufactured products, the utilities for consumers to purchase new products are $u_1 = v - p_1 + \varepsilon_n n$ and $u_n = v - p_n + \varepsilon_n n$ in the two periods, respectively; the utility to purchase remanufactured products is $u_r = \delta v - p_r + \varepsilon_r t$ in period 2. Here, $\varepsilon_n > 0(\varepsilon_r > 0)$ measures the impact of the warranty period n (t) on the consumers' willingness-to-pay for new (remanufactured) products. Following Liu, Tang, et al. (2017) and Li and Chen (2018), consumers make a purchasing decision in the principle of utility maximisation. Assume that Θ_1 and Θ_n denote the set of consumers purchasing new products in period 1 and 2, respectively, and Θ_r represents the set of consumers purchasing remanufactured products in period 2, that is $\Theta_1 = \{v : u_1 \ge 0\}, \Theta_n = \{v : u_n \ge \max\{u_r, 0\}\}$ and $\Theta_r = \{v : u_r \ge \max\{u_n, 0\}\}$. Hence, by setting n = 1, demand for new and remanufactured products is derived as $q_1 = Q - p_1 + \varepsilon_n , q_n = Q - \frac{p_n - p_r + \varepsilon_r t - \varepsilon_n}{1 - \delta}$ and $q_r = \frac{\delta p_n - p_r + \varepsilon_r t - \delta \varepsilon_n}{\delta(1 - \delta)}$, respectively. The manufacturer produces as per market demand q_1 , q_n and q_r .

We assume that the warranty for new and remanufactured products is provided for consumers by either the manufacturer or the retailer and the warranty provider incurs the warranty cost over both periods. In each period, the warranty cost consists of a linear component $c_{nw}^{i}k(c_{nw}^{i}k)$ and a quadratic portion $(1/2)\beta_{nw}^{j}k^{2}((1/2)\beta_{nw}^{j}k^{2})$, k = n, t. Parameter $c_{nw}^{i}(c_{nw}^{i})$ is a linear maintenance cost for malfunctions of a new (remanufactured) product in each unit time. Parameter $\beta_{nw}^{i}(\beta_{nw}^{i})$ is the quadratic cost coefficient for offering a new (remanufactured) product warranty. This warranty cost structure combines the features in two existing articles (Chen, Li, and Zhou 2012; Wei, Zhao, and Li 2015) and takes a more general form. If $c_{nw}^i = 0$, $(c_{nw}^i = 0)$, the cost structure is consistent with that in (Wei, Zhao, and Li 2015); if $\beta_{nw}^{j} = 0(\beta_{nw}^{j} = 0)$, it is the same as that in (Chen, Li, and Zhou 2012). Here, $j \in \{M, R\}$ represents the manufacturer and retailer, respectively. The remanufactured product is assumed to be as good as the new product, and warranty for new and remanufactured products is provided by the same member. As such, we assume that the linear and quadratic warranty cost parameters for a new product are the same as those for a remanufactured product, i.e. $c'_{nw} = c'_{rw} = c'_w$ and $\beta'_{nw} = \beta'_{rw} = \beta'_w$. The unit production costs of new and remanufactured products are c_n and c_r , and $c_r < c_n$. It is noted that a unit collection cost is often assumed in a typical CLSC setting when a used product is recycled for remanufacturing period 2 (Atasu, Toktay, and Van Wassenhove 2013; Ma et al. 2016). Without loss of generality, we assume that c_r here incorporates the collection cost into the unit remanufacturing cost and this assumption does not materially change the main results derived in this paper. To make remanufacturing economically sensible, given consumers' value discount δ , it is assumed that $c_r < \delta(c_n + c_w^J - \varepsilon_n)$. This assumption is similar as that in existing literature (Esenduran, Kemahlıoğlu-Ziya, and Swaminathan 2016).

In this research, we analyse the impact of the warranty policy on pricing decisions and operational efficiency of the CLSC under two warranty models, where either the manufacturer or the retailer offers warranty for new and remanufactured

| Symbol | Definition | | |
|----------------------|--|--|--|
| $\overline{c_n/c_r}$ | The unit production cost of a new/remanufactured product | | |
| $w_1/p_1/q_1$ | The unit wholesale price/retail price/sale quantity of new products in period 1 | | |
| w_n/w_r | The unit wholesale price of a new/remanufactured product in period 2 | | |
| p_n/p_r | The unit retail price of a new/remanufactured product in period 2 | | |
| q_n/q_r | Sales quantity of new/remanufactured products in period 2 | | |
| Q | The whole market capacity in each period | | |
| v v | Consumer's willingness-to-pay for the new product in each period | | |
| δ | Consumer's value discount for the remanufactured product | | |
| t | Warranty period for the remanufactured product | | |
| γ | The collection yield of used products for remanufacturing | | |
| c_w^j/β_w^j | The linear/quadratic warranty cost parameter for remanufactured and new products incurred by the warranty provider $j, j \in \{M, R\}$ | | |
| ε _r | The impact of warranty period t on the consumer's willingness-to-pay for the remanufactured product | | |
| ε_{n_i} | The impact of warranty period n on the consumer's willingness-to-pay for the new product | | |
| π_j^i | Profit function of member j in model $i, i \in \{MM, RR, MN, RN\}$ | | |
| CS^{i} | Consumer surplus in model <i>i</i> | | |

Table 2. Parameters and decision variables.

products (denoted by *MM* or *RR* accordingly) over two periods. In addition, to facilitate comparative analyses, we consider two benchmark models where the manufacturer or the retailer offers warranty for new products only (denoted by *MN* or *RN* accordingly). The manufacturer and retailer are rational and profit maximisers. Hereafter, π_j^i denotes the profit of member *j* under model *i*, and π_T^i denotes the channel profit of the CLSC; $i \in \{MM, RR, MN, RN\}, j \in \{M, R\}$.

In addition, let *CS* denote consumer surplus obtained from purchasing new and remanufactured products over the two periods, which is calculated as $CS = \frac{1}{2}(q_1^2 + q_n^2 + 2\delta q_n q_r + \delta q_r^2)$ (Yenipazarli 2016).

Table 2 summarises the symbols and notation used in this paper. For a more concise presentation of equilibrium solutions, we further introduce $\phi_{j0} = Q - (c_n + c_w^j - \varepsilon_n)$, $\phi_{j1} = \delta(c_n + c_w^j - \varepsilon_n) - c_r$, $\phi_{j2} = \beta_w^j \delta(1 - \delta)$, $\phi_{j3} = \varepsilon_r - c_w^j$, $\phi_{j4} = \phi_{j0} + \gamma \phi_{j1}$, $\varphi_0 = 1 + \gamma^2 \delta(1 - \delta)$, $\phi_{MM} = 4\phi_{M2} - \phi_{M3}^2$, $\phi_{RR} = 4\phi_{R2} - \phi_{R3}^2$, $\varphi_{MM} = 4\beta_w^M + \gamma^2 \phi_{MM}$, and $\varphi_{RR} = 2\beta_w^R + \gamma^2 \phi_{RR}$.

4. Model formulation and equilibrium solution

Since we normalise the warranty period for new products to be n = 1 and assume the warranty period for remanufactured products $t \le n = 1$, the warranty provider's decision on the warranty period is confined to remanufactured products for the remainder of this research. On the other hand, the linear and quadratic warranty costs for new products in both periods are incorporated into the warranty provider's profit function by using n = 1.

4.1. Model MM- the manufacturer offers a warranty for new and remanufactured products

In model *MM*, the manufacturer provides a warranty for new and remanufactured products. The profit functions of the manufacturer and retailer can be formulated as:

$$\pi_M^{MM}(w_1, w_n, w_r, t) = (w_1 - c_n - c_w^M)q_1 + (w_n - c_n - c_w^M)q_n + (w_r - c_r - c_w^M t)q_r - \beta_w^M - \frac{1}{2}\beta_w^M t^2$$
(1)

$$\pi_R^{MM}(p_1, p_n, p_r) = (p_1 - w_1)q_1 + (p_n - w_n)q_n + (p_r - w_r)q_r$$
⁽²⁾

s.t. $0 < q_r \leq \gamma q_1$

The constraint means that the quantity of remanufactured products is constrained by a proportion of new products that are collected and remanufactured after one period of use. Since the manufacturer is the leader and the retailer is the follower, the decision sequence is as follows. Stage 1: the manufacturer decides the wholesale price of new products and, then, the retailer decides its retail price in period 1. Stage 2: the manufacturer decides the wholesale price of new and remanufactured products, as well as the warranty period for remanufactured products and, then, the retailer, decides the retail price of both products in period 2. According to backward induction, model *MM* has a unique optimal solution if $\phi_{MM} = 4\phi_{M2} - \phi_{M3}^2 > 0$. Given the unit remanufacturing cost c_r , we derive the equilibrium decisions as follows.

If $\delta(Q - \phi_{M0}) - \frac{\gamma \phi_{M0} \phi_{MM}}{4\beta_w^M} \le c_r < \delta(Q - \phi_{M0})$, the manufacturer remanufactures part of available used products (referred to as partial remanufacturing). In this case, the optimal wholesale price and warranty period decisions are $w_1^{MM-P*} = c_n + c_w^M + \frac{\phi_{M0}}{2}$, $w_n^{MM-P*} = c_n + c_w^M + \frac{\phi_{M0}}{2}$, $w_r^{MM-P*} = \frac{\delta Q + c_r}{2} + \frac{\phi_{M1}\phi_{M3}(\varepsilon_r + c_w^M)}{2\phi_{MM}}$, and $t^{MM-P*} = \frac{\phi_{M1}\phi_{M3}}{\phi_{MM}}$; the corresponding optimal retail prices are $p_1^{MM-P*} = Q + \varepsilon_n - \frac{\phi_{M0}}{4}$, $p_n^{MM-P*} = Q + \varepsilon_n - \frac{\phi_{M0}}{4}$, and $p_r^{MM-P*} = \frac{\delta(4Q - \phi_{M0})}{4} - \frac{\phi_{M0}}{4}$. $\phi_{M1}(\phi_{M2}-\varepsilon_r\phi_{M3})$. ϕ_{MM}

If $0 < c_r < \delta(Q - \phi_{M0}) - \frac{\gamma \phi_{M0} \phi_{MM}}{4\beta^M}$, the manufacturer remanufactures all available used products (referred to as complete remanufacturing). In this case, the optimal wholesale price and warranty period decisions are $w_1^{MM-C*} = c_n + c_w^M + \frac{2\beta_w^M \phi_{M4}}{\varphi_{MM}}$, $w_n^{MM-C*} = c_n + c_w^M + \frac{\phi_{M0}}{2}$, $w_r^{MM-C*} = c_r + \frac{2\gamma^2(\delta Q - c_r)(2\phi_{M2} + c_w^M \phi_{M3}) + \phi_{M0}(4\beta_w^M \delta(1+\gamma(1-\delta)) - \phi_{M3}(\gamma^2\delta(c_w^M + \varepsilon_r) - 2\gamma c_w^M))}{2\varphi_{MM}}$, and $t^{MM-C*} = \frac{\gamma\phi_{M3}\phi_{M4}}{\varphi_{MM}}$; the corresponding optimal retail prices are $p_1^{MM-C*} = Q + \varepsilon_n - \frac{\beta_w^M \phi_{M4}}{\varphi_{MM}}$, $p_n^{MM-C*} = Q + \varepsilon_n - \frac{\phi_{M0}}{4}$, and $p_r^{MM-C*} = \delta(Q - \frac{\phi_{M0}}{4}) - \frac{\gamma\phi_{M4}(\phi_{M2} - \varepsilon_r \phi_{M3})}{\varphi_{MM}}$. The derivation process of the equilibrium solution is furnished in Appendix A-1.

4.2. Model RR- the retailer offers warranty for new and remanufactured products

In model RR, the retailer offers a warranty for new and remanufactured products, and the profit functions of the manufacturer and retailer can be formulated as:

$$\pi_M^{RR}(w_1, w_n, w_r) = (w_1 - c_n)q_1 + (w_n - c_n)q_n + (w_r - c_r)q_r$$
(3)

$$\pi_R^{RR}(p_1, p_n, p_r, t) = (p_1 - w_1 - c_w^R)q_1 + (p_n - w_n - c_w^R)q_n + (p_r - w_r - c_w^R t)q_r - \beta_w^R - \frac{1}{2}\beta_w^R t^2$$
(4)

s.t.
$$0 < q_r \leq \gamma q_1$$

The constraint is the same as that in model MM. Since the manufacturer is the leader and the retailer is the follower, the decision sequence is as follows. Stage 1: the manufacturer decides the wholesale price of new products and, then, the retailer decides its retail price in period 1. Stage 2: the manufacturer decides the wholesale price of new and remanufactured products and, then, the retailer decides the retail price of both products and the warranty period for remanufactured products in period 2. According to backward induction, model RR has a unique optimal solution if $\phi_{RR} = 2\phi_{R2} - \phi_{R3}^2 > 0$. Given the unit remanufacturing cost c_r , one obtains the equilibrium decisions as follows. If $\delta(Q - \phi_{R0}) - \frac{\gamma \phi_{R0} \phi_{RR}}{2\beta_r^R} \le c_r < \delta(Q - \phi_{R0})$, the manufacturer commits to partial remanufacturing. In this case, the

optimal pricing and warranty period decisions are $w_1^{RR-P*} = c_n + \frac{\phi_{R0}}{2}$, $w_n^{RR-P*} = c_n + \frac{\phi_{R0}}{2}$, $w_r^{RR-P*} = \frac{\delta Q + c_r}{2}$, $p_1^{RR-P*} = Q + \varepsilon_n - \frac{\phi_{R0}}{4}$, $p_r^{RR-P*} = \frac{\delta(4Q - \phi_{R0})}{4} - \frac{\phi_{R1}(\phi_{R2} - \varepsilon_r \phi_{R3})}{2\phi_{RR}}$, and $t^{RR-P*} = \frac{\phi_{R1}\phi_{R3}}{2\phi_{RR}}$. If $0 < c_r < \delta(Q - \phi_{R0}) - \frac{\gamma\phi_{R0}\phi_{RR}}{2\beta_w^R}$, the manufacturer is engaged in complete remanufacturing, and the equilibrium deci-

sions are obtained as $w_1^{RR-C*} = c_n + \frac{\beta_w^R \phi_{R4}}{\varphi_{RR}}$, $w_n^{RR-C*} = c_n + \frac{\phi_{R0}}{2}$, $w_r^{RR-C*} = \frac{\delta Q + c_r}{2} + \frac{\phi_{R0}}{2\gamma} - \frac{\beta_w^R \phi_{R4}}{\gamma \varphi_{RR}}$, $p_1^{RR-C*} = Q + \varepsilon_n - \frac{\beta_w^R \phi_{R4}}{2\varphi_{RR}}$, and $t^{RR-C*} = \frac{\gamma \phi_{R3} \phi_{R4}}{2\varphi_{RR}}$. The derivation process of the equilibrium solution is provided in Appendix A-2.

4.3. Benchmark models

To facilitate the impact analysis of warranty on supply chain operations, two benchmark models are formulated as follows, where the manufacturer and the retailer, respectively, offer warranty for new products only, denoted as MN and RN accordingly.

(1) Model MN – the manufacturer offers a warranty for new products only

Model MN is the simplified case of model MM where t = 0, meaning that the manufacturer provides warranty for new products only. In this model, when $\delta(Q - \phi_{M0}) - \gamma \delta(1 - \delta)\phi_{M0} \le c_r < \delta(Q - \phi_{M0})$, the manufacturer commits to partial remanufacturing and the equilibrium decisions are $w_1^{MN-P*} = c_n + c_w^M + \frac{\phi_{M0}}{2}$, $w_n^{MN-P*} = c_n + c_w^M + \frac{\phi_{M0}}{2}$, $w_r^{MN-P*} = Q + \varepsilon_n - \frac{\phi_{M0}}{4}$, $p_n^{MN-P*} = Q + \varepsilon_n - \frac{\phi_{M0}}{4}$, and $p_r^{MN-P*} = \delta Q - \frac{\delta Q - c_r}{4}$. When $0 < c_r < \delta(Q - \phi_{M0}) - \gamma \delta(1 - \delta)\phi_{M0}$, the manufacturer commits to complete remanufacturing and the equilibrium decisions are $w_1^{MN-P*} = \delta Q - \frac{\delta Q - c_r}{4}$. When $0 < c_r < \delta(Q - \phi_{M0}) - \gamma \delta(1 - \delta)\phi_{M0}$, the manufacturer commits to complete remanufacturing and the equilibrium decisions are $w_1^{MN-C*} = c_n + c_w^M + \frac{\phi_{M0}}{2\phi_0}$, $w_n^{MN-C*} = c_r + \frac{\delta(\varphi_0\phi_{M0} + \gamma(1 - \delta)\phi_{M0})}{2\phi_0}$, $p_1^{MN-C*} = Q + \varepsilon_n - \frac{\phi_{M4}}{4\phi_0}$, $p_n^{MN-C*} = Q + \varepsilon_n - \frac{\phi_{M4}}{4\phi_0}$.

The derivation process of the equilibrium solution is given in Appendix A-3.

(2) Model RN- the retailer offers warranty for new products only

Model RN is the simplified case of model RR where t = 0, meaning that the retailer offers warranty for new products Model *RN* is the simplified case of model *RR* where t = 0, meaning that the relation of the products only, but no warranty for remanufactured products. In this model, when $\delta(Q - \phi_{R0}) - \gamma \delta(1 - \delta)\phi_{R0} \le c_r < \delta(Q - \phi_{R0})$, the manufacturer commits to partial remanufacturing; the equilibrium decisions are $w_1^{RN-P*} = c_n + \frac{\phi_{R0}}{2}$, $w_n^{RN-P*} = Q + \varepsilon_n - \frac{\phi_{R0}}{4}$, $p_n^{RN-P*} = Q + \varepsilon_n - \frac{\phi_{R0}}{4}$, and $p_r^{RN-P*} = \delta Q - \frac{\delta Q - c_r}{4}$. When $0 \le c_r < \delta(Q - \phi_{R0}) - \gamma \delta(1 - \delta)\phi_{R0}$, the manufacturer commits to complete remanufacturing; the equilibrium decisions are obtained as $w_1^{RN-C*} = c_n + \frac{\phi_{R0}}{2}$, $w_n^{RN-C*} = c_n + \frac{\phi_{R0}}{2}$, $w_r^{RN-C*} = c_n + \frac{\phi_{R0}}{2}$, $w_r^{RN-C*} = \frac{\delta Q + c_r}{2} + \frac{\gamma \delta(1 - \delta)\phi_{R0} - \phi_{R1}}{2\phi_0}$, $p_1^{RN-C*} = Q + \varepsilon_n - \frac{\phi_{R0}}{4\phi_0}$, $p_n^{RN-C*} = Q + \varepsilon_n - \frac{\phi_{R0}}{2\phi_0}$. The derivation process of the equilibrium solution is detailed in Appendix A-4.

5. Main results and comparative analyses

5.1. An impact analysis of warranty on remanufacturing and supply chain operations

LEMMA 5.1.1 The manufacturer in model MM (the retailer in model RR) offers warranty for remanufactured products if and only if $\phi_{i3} = \varepsilon_r - c_w^j > 0, j \in \{M, R\}.$

The proof of Lemma 5.1.1 is obvious by examining the equilibrium warranty period decisions in Section 4.1 and 4.2. Loosely speaking, ϕ_{i3} gauges the net benefit of offering warranty for remanufactured products. The manufacturer in model MM and the retailer in model RR are willing to offer a warranty $(t^{i^*} > 0, i \in \{MM, RR\})$ if and only if they can benefit from it $(\phi_{i3} > 0)$. Otherwise, they will not offer a warranty for remanufactured products $(t^{i^*} = 0, i \in \{MM, RR\})$. If $\phi_{i3} > 0$, keeping other things equal, the larger the ϕ_{i3} , the longer the warranty period. However, there exists an upper limit for the increased warranty period: the existence of a unique optimal solution for model MM (RR) and the constraint $t^{i^*} \le n = 1$

imply that $\phi_{M3} < \frac{1}{2} \left(\sqrt{\phi_{M1}^2 + 16\phi_{M2}} - \phi_{M1} \right) \left(\phi_{R3} < \frac{1}{4} \left(\sqrt{\phi_{R1}^2 + 32\phi_{R2}} - \phi_{R1} \right) \right)$ when the manufacturer commits to partial remanufacturing; and $\phi_{M3} < \frac{1}{2\gamma^2} \left(\sqrt{\phi_{M4}^2 + 16\gamma^2 \beta_w^M \varphi_0} - \phi_{M4} \right) \left(\phi_{R3} < \frac{1}{4\gamma^2} \left(\sqrt{\phi_{R4}^2 + 32\gamma^2 \beta_w^R \varphi_0} - \phi_{R4} \right) \right)$ when the manufacturer commits to complete remanufacturing.

PROPOSITION 5.1.1 Compared to models MN and RN, the following results hold:

- (i) When the manufacturer commits to partial remanufacturing, the wholesale price of remanufactured products is higher in model MM than that in model MN, but it is the same in models RR and RN; offering warranty for remanufactured products leads to a higher retail price of remanufactured products, but does not affect the wholesale or retail price of new products in both periods.
- (ii) When the manufacturer commits to complete remanufacturing, the wholesale price of remanufactured products is higher in model MM than that in model MN, and it is lower in model RR than that in model RN; offering warranty for remanufactured products leads to a higher retailer price of remanufactured products, a higher wholesale price and a lower retail price of new products in period 1, but it has no effect on pricing decisions of new products in period 2.

The proof of Proposition 5.1.1 is given in Appendix B.

It is understandable that offering warranty for remanufactured products conveys the right quality signal to customers and increases consumers' utility of purchasing remanufactured products, thereby enhancing the sales of remanufactured products $(q_r^{MM-h*} > q_r^{MN-h*} \text{ and } q_r^{RR-h*} > q_r^{RN-h*}, h \in \{P, C\})$, exacerbating demand cannibalisation for new products in period 2 $(q_n^{MM-h*} < q_n^{MN-h*} \text{ and } q_n^{RR-h*} < q_n^{RN-h*})$. To curb profit loss in the new product market and maintain differentiated competition between new and remanufactured products in period 2, the manufacturer (retailer) does not adjust its wholesale price (retail price) of new products, thereby stabilising the profit margin of new products $(w_n^{MM-h*} = w_n^{MN-h*}, w_n^{RR-h*} = w_n^{RN-h*}, p_n^{MM-h*} = p_n^{MN-h*}, \text{ and } p_n^{RR-h*} = p_n^{RN-h*}).$

The impact of warranty for remanufactured products on pricing decisions of new products in period 1 and remanufactured products is closely related to the manufacturer's remanufacturing strategy. When the manufacturer commits to partial remanufacturing, offering warranty for remanufactured products has no effect on the pricing decisions of new products in period 1. In terms of wholesale pricing of remanufactured products, in model MM where the manufacturer offers warranty and incurs warranty cost, it can pass the increased warranty cost onto the retailer by bumping up the wholesale price $(w_r^{MM-P*} > w_r^{MN-P*})$. On the other hand, in model *RR* where the retailer provides warranty and bears warranty cost, as the follower in the CLSC, it has no mechanism to influence the manufacturer's wholesale price of remanufactured products $(w_r^{RR-P*} = w_r^{RN-P*})$. As for the retail price, offering warranty incurs additional cost to the manufacturer (retailer) in the *MM* (*RR*) model. In model *MM*, the manufacturer transfers part of this cost to the retailer by increasing the wholesale price, leading the retailer to raise its retail price $(p_r^{MM-P*} > p_r^{MN-P*})$. In model *RR*, the retailer has to pass this additional warranty cost onto the customers by increasing the retail price of remanufactured products $(p_r^{RR-P*} > p_r^{RN-P*})$.

When the manufacturer remanufactures all available used products, remanufactured products in period 2 and new products in period 1 are complements. In this case, compared to producing new products, remanufacturing has a significant cost advantage in the first place and offering warranty for remanufactured products will further enhance consumer's willingness-to-pay and demand for remanufactured products. For the wholesale price of remanufactured products, when the manufacturer offers warranty for remanufactured products in model MM, it can raise its wholesale price to share the benefit of enhanced demand for remanufactured products $(w_r^{MM-C*} > w_r^{MN-C*})$. When the retailer offers warranty for remanufactured products in model RR, the manufacturer lowers its wholesale price to compensate the retailer for its warranty cost $(w_r^{RR-C*} < w_r^{RN-C*})$. It is understandable that the retailer will charge a higher retail price for remanufactured products to absorb the additional cost when the warranty is extended to them by the manufacturer (retailer) in model MM (RR) $(p_r^{MM-C*} > p_r^{MN-C*} \text{ and } p_r^{RR-C*} > p_r^{RN-C*})$. Furthermore, the enhanced demand for remanufactured products requires more new products due to the complementary product relationship, allowing the retailer to lower the retail price of new products $(p_1^{MM-C*} < p_1^{MN-C*} \text{ and } p_1^{RR-C*} < p_1^{RN-C*})$ in period 1, thereby boosting the sale of new products and, eventually, resulting in more available used products for remanufacturing in period 2. As the retailer is closer to the end market and directly benefits from enhanced demand for remanufactured products when the warranty is extended to them, the profitability of the retailer increases much more than that of the manufacturer from the remanufactured product channel. To achieve an equitable allocation of the benefit, the manufacturer raises its wholesale price of new products to rake in more profit from this channel $(w_1^{MM-C*} > w_1^{MN-C*} \text{ and } w_1^{RR-C*} > w_1^{RN-C*})$ in models *MM* and *RR* in period 1. By collaborating with each other, both members achieve higher profitability by balancing their benefit from the new and remanufactured product channels.

PROPOSITION 5.1.2 Compared to benchmark models MN and RN, offering warranty for remanufactured products improves individual and channel profits, and consumer surplus.

The proof of Proposition 5.1.2 is given in Appendix C.

Proposition 5.1.2 indicates that the combined effect of pricing decisions and resulting quantities from offering warranty for remanufactured products leads to heightened individual and channel profitability as well as consumer surplus in the CLSC in *MM* and *RR* warranty models compared to the corresponding benchmark models *MN* and *RN* offering warranty for new products only $(\pi_j^{MM-h*} > \pi_j^{MN-h*}, \pi_j^{RR-h*} > \pi_j^{RN-h*}, j \in \{M, R\}; \pi_T^{MM-h*} > \pi_T^{MN-h*}, \pi_T^{RR-h*} > \pi_T^{RN-h*}, CS^{MM-h*} > CS^{MN-h*}, and CS^{RR-h*} > CS^{RN-h*}, h \in \{P, C\}$). This result remains true regardless of the manufacturer's remanufacturing strategy, indicating that offering warranty for remanufactured products is mutually beneficial for the manufacturer, retailer, and consumers. The implication is that a wise choice is for the manufacturer or the retailer to extend the warranty to remanufactured products. This is consistent with business practices in reality: Caterpillar and Lenovo, for example, provide warranty for remanufactured products comparable to that for their new products.

COROLLARY 5.1.1 The following results hold:

- (i) Compared to model MN, the increase in the manufacturer's profit is lower than the retailer's profit enhancement in model MM.
- (ii) Compared to model RN, the increase in the manufacturer's profit is higher than the retailer's profit enhancement in model RR.

The proof of Corollary 5.1.1 is given in Appendix D.

When the manufacturer offers warranty for remanufactured products in model *MM*, the manufacturer directly incurs the warranty cost, but its benefit from enhanced demand for remanufactured products is secondary. On the other hand, the retailer directly benefits from enhanced demand owing to offering warranty for remanufactured products, but its sharing of warranty cost is secondary. As such, it is reasonable that the retailer is better off in grabbing more shares in the enhanced profitability when the manufacturer offers warranty for remanufactured products in model *MM* compared to the benchmark model *MN*.

When the retailer offers warranty for remanufactured products in model *RR*, the retailer directly incurs the warranty cost and also directly enjoys the ensuing benefit of enhanced demand for remanufactured products. In this case, the manufacturer

reaps more secondary benefits from enhanced demand for remanufactured products than the secondary expense for offering a warranty, leading to a higher share of enhanced profitability for the manufacturer than the retailer.

Furthermore, a closer examination of the two members' profitability in different models reveals that the manufacturer as the leader in this CLSC takes a larger share of the channel profit than the retailer does if the manufacturer's quadratic warranty cost parameters for new and remanufactured products are not too high in models MN and MM. Corollary 5.1.1 implies that the profit inequity is always narrowed down if the manufacturer offers warranty for remanufactured products, but widened if the retailer does.

5.2. Equilibrium solution analysis

In this subsection, we compare equilibrium solutions between the two warranty models MM and RR. First, we identify the warranty cost parameter boundary conditions under which the manufacturer (retailer) offers a longer warranty period for remanufactured products. For apparent reasons, the manufacturer and retailer usually possess different levels of production technology and market knowledge. This difference tends to be reflected in different linear and quadratic warranty cost parameters $(c_w^M \neq c_w^R)$ and $\beta_w^M \neq \beta_w^R)$ when the manufacturer (retailer) offers warranty in model *MM* (*RR*). In general, three scenarios may arise Scenario I ($c_w^M = c_w^R = c$ and $\beta_w^M \neq \beta_w^R)$), Scenario II ($c_w^M \neq c_w^R$ and $\beta_w^M = \beta_w^R = \beta$), and Scenario III ($c_w^M \neq c_w^R$ and $\beta_w^M \neq \beta_w^R)$). Next, we restrict our discussion to Scenario I only and the analysis for Scenario II can be carried out in a similar fashion. For the more general scenario of $c_w^M \neq c_w^R$ and $\beta_w^M \neq \beta_w^R$, we cannot obtain closed-form solutions to compare warranty periods and warranty efficiency between models MM and RR and, hence, the relevant analysis is delegated to numerical experiments in Section 6.

PROPOSITION 5.2.3 Under scenario I when $c_w^M = c_w^R = c$, if $\bar{\beta}_{M1}^h \leq \beta_w^M \leq \bar{\beta}_{M2}^h$ $(h \in \{P, C\})$, a longer warranty period for remanufactured products is offered by the manufacturer in model MM; if $\beta_w^M = \bar{\beta}_{M2}^h$, models MM and RR offer the same warranty period; if $\beta_w^M > \bar{\beta}_{M2}^h$, a longer warranty period is offered by the retailer in model RR. Here $\beta_w^M \geq \bar{\beta}_{M1}^h$ is the lower bound of the quadratic cost parameter to guarantee that $t^{MM-h*} \leq n = 1$.

The proof of Proposition 5.2.3 is given in Appendix E.

As shown in Appendix E, when models MM and RR have the same linear cost parameter $c_w^M = c_w^R = c$ but different quadratic cost parameters in Scenario I, $\bar{\beta}_{M2}^h$ is a function of β_w^R . If $\bar{\beta}_{M1}^h \le \beta_w^M < \bar{\beta}_{M2}^h$, the quadratic cost parameter in the manufacturer warranty model MM is more efficient compared to that in the retailer warranty model RR. In this case, the manufacturer is willing to offer a longer warranty period for remanufactured products in model MM. On the other hand, if $\beta_w^M > \bar{\beta}_{M2}^h$, the retailer has a more efficient quadratic cost parameter in model *RR* than the manufacturer does in model *MM*, so the retailer in model *RR* is able to provide a longer warranty period. It is worth noting that this structural insight on the warranty period remains valid regardless of the manufacturer's remanufacturing strategy except for a shifted threshold value of $\bar{\beta}_{M2}^h$. It is also confirmed that $\bar{\beta}_{M2}^C$ decreases in collection rate γ , indicating that a higher collection rate makes it easier for the retailer in model RR to offer a longer warranty when the manufacturer remanufactures all available used products.

COROLLARY 5.2.2 Under scenario I when $c_w^M = c_w^R = c$, if $\bar{\beta}_{M1}^h \leq \beta_w^M < \bar{\beta}_{M3}^h$, a higher retail price is attained for remanufactured products in model MM than RR; if $\beta_w^M = \bar{\beta}_{M3}^h$, the retailer sets the same retail price in models MM and RR; if $\beta_w^M > \bar{\beta}_{M3}^h$, a higher retail price is achieved for remanufactured products in model RR than MM, where $\bar{\beta}_{M2}^h < \bar{\beta}_{M3}^h$ holds.

The proof of Corollary 5.2.2 is discussed in Appendix F. When $\bar{\beta}_{M1}^h \leq \beta_w^M < \bar{\beta}_{M2}^h$, the quadratic cost parameter of the manufacturer warranty model *MM* is more efficient than that in the retailer warranty model RR, the manufacturer is willing to provide a longer warranty period for remanufactured products and transfers part of the increased warranty cost to the retailer through the wholesale price, which is eventually passed onto consumers by the retailer at a higher retail price $(p_r^{MM-h*} > p_r^{RR-h*})$. At the other extreme end when $\beta_w^M > \bar{\beta}_{M3}^h > \bar{\beta}_{M2}^h$, the retailer in model *RR* has a significant relative quadratic cost parameter advantage over the manufacturer does in MM, it is natural from Proposition 5.2.3 that the retailer's cost advantage is translated into a longer warranty period in model RR. At the same time, the retailer can also raise its retail price of remanufactured products to maximise its economic benefit $(p_r^{MM-h*} < p_r^{RR-h*}).$

What is more complicated is in the middle range $\bar{\beta}_{M2}^h < \beta_w^M < \bar{\beta}_{M3}^h$, where the retailer in model *RR* has a more efficient quadratic cost parameter than the manufacturer does in model *MM*. This cost advantage allows the retailer to offer a longer warranty period for remanufactured products in model RR than the manufacturer does in model MM as shown in Proposition 5.2.3. When the manufacturer offers warranty in model MM, even if its warranty period is shorter than that offered by the retailer in RR, the higher warranty cost and the double-marginalization nature of cost transfer to the retailer tend to push higher the retail price of remanufactured products in model *MM*. Conversely, if the retailer offers warranty in model *RR*, as it is closer to the market and can directly influence market demand by offering warranty and setting the retail price of remanufactured products, this channel structure allows the retailer to offer a longer warranty period for remanufactured products at a lower retail price in model *RR*. Therefore, the coupling effect of the cost advantage and channel structure leads to $t^{MM-h*} < t^{RR-h*}$ (Proposition 5.2.3) and $p_r^{MM-h*} > p_r^{RR-h*}$ when $\bar{\beta}_{M2}^h < \beta_w^M < \bar{\beta}_{M3}^h$. Similarly, the structural insight on the retail price of remanufactured products remains intact regardless of the manufacturer's remanufacturing strategy.

5.3. Analysis of profitability and consumer surplus

We first compare individual profitability between the two warranty models MM and RR.

PROPOSITION 5.3.4 Under scenario I when $c_w^M = c_w^R = c$, the manufacturer achieves higher profitability in model RR than MM, but the retailer reaches higher profitability in model MM than RR.

The proof of Proposition 5.3.4 is furnished in Appendix G.

When the linear warranty cost parameters are the same in models MM and RR $(c_w^M = c_w^R = c)$, the manufacturer's provision of warranty allows it to charge a higher wholesale price (leading to a higher unit profit margin) of remanufactured products in model MM than RR. When the manufacturer commits to partial remanufacturing, the unit profit margin for new products stays the same in models MM and RR in both periods. The quantities of new products in period 1 are the same in both models and the quadratic warranty cost for new products is only occurred in model MM, leading to a lower profit contribution from new products in period 1 in model MM for the manufacturer. In period 2, if $\beta_w^M < (\beta_w^R/2)$, the manufacturer warranty in model MM has a significant relative quadratic cost advantage; this advantage outweighs the double-marginalization effect of transferring warranty cost down to the retailer and results in a higher demand for remanufactured products but a lower demand for new products in model MM than that in model RR. Hence, the profit contribution from remanufactured products is higher for the manufacturer in model MM than that in model RR. On the other hand, the unit profit margin of new products for the manufacturer stays the same in model MM and RR. This leads to a lower profit contribution from new products for the manufacturer in model MM than that in model RR. And the reduced profitability from new products in the two periods outweighs the increased profitability from remanufactured products in model MM and the net effect is that the manufacturer achieves higher profitability in model RR, and this remains true when $\beta_w^M = (\beta_w^R/2)$. If the manufacturer warranty model *MM* has no significant relative quadratic cost advantage $(\beta_w^M > (\beta_w^R/2))$, the retailer's offering warranty boosts an even higher demand for remanufactured products and cannibalises more demand for new products in model RR. The heightened demand, in this case, is more than enough to offset the decreased unit profit margin of remanufactured products for the manufacturer in model RR. As such, the profit contribution from remanufactured products in model RR is higher than that in model MM. This increased profitability from remanufactured products outweighs the change in profitability from new products and the net effect is that the manufacturer achieves higher profitability in model RR.

When the manufacturer commits to complete remanufacturing, if the manufacturer warranty model MM has a significant relative quadratic cost advantage $(\beta_w^M < (\beta_w^R/2) < \bar{\beta}_{M2}^C)$, a longer warranty period offered in the MM model (as per Proposition 5.2.3) boosts more demand for remanufactured products (and the complementary new products in period 1) in model MM than RR. In addition, the manufacturer obtains higher unit profit margins of new products in period 1 and remanufactured products in model MM than those in model RR. However, the increased demand for remanufactured products produces more severe cannibalisation of new products in period 2, leading to significantly lower profitability from new products in period 2 in model MM. The increased profitability from new products in period 1 and remanufactured products is insufficient to recover the reduced profitability from new products in period 2 in model MM and the net effect is that the manufacturer achieves higher profitability in model *RR* and this remains true when $\beta_w^M = (\beta_w^R/2)$. If the manufacturer war-ranty model *MM* has no significant relative quadratic cost advantage $\beta_w^M > (\beta_w^R/2)$, the manufacturer's unit profit margin and calca quantity of new and the interval of the second and sales quantity of new products in period 1 are lower in model MM than those in model RR. On the other hand, the sale quantity of remanufactured products is lower in model MM than RR in this case; the impact of the manufacturer's higher unit profit margin of remanufactured products cannot counterbalance that of the lower demand in model MM compared to model RR, leading to a lower profit contribution from remanufactured products for the manufacturer in model MM. It is noted that the manufacturer's profit difference between models MM and RR from new products in period 2 increases in β_w^M . At the lower end when $\beta_w^M > (\beta_w^R/2)$, the manufacturer's profit from new products in period 2 under model MM is lower than that under model RR. At the higher end when β_w^M is sufficiently large, the manufacturer achieves a higher profit from new products in period 2 in model MM than RR. However, the higher profit from new products in period 2 is insufficient to recover the reduced profitability from new products in period 1 and remanufactured products for the manufacturer in model

MM and the net effect is that the manufacturer achieves higher profitability in model RR than MM. In summary, under the scenario I when $c_w^M = c_w^R = c$, the manufacturer achieves higher profitability when the retailer offers a warranty in model *RR* than the case when the manufacturer offers a warranty in model *MM*.

Following a similar logic, Proposition 5.3.4 confirms that the retailer always obtains higher profitability when the manufacturer provides warranty for new and remanufactured products regardless of the manufacturer's remanufacturing strategy. In summary, Proposition 5.3.4 demonstrates that under scenario I when models MM and RR have the same linear cost parameter $(c_w^M = c_w^R = c)$, each member in the CLSC prefers the other to offer warranty for new and remanufactured products, and the CLSC may enter an impasse.

PROPOSITION 5.3.5 Under scenario I when $c_w^M = c_w^R = c$, the following results hold.

- (i) If φ_{R3} ≤ φ̄^h_{R3} and β^R_w > β̄^h_{R2} (φ_{R3} > φ̄^h_{R3}), there exists β̄^h_{M4} > β̄^h_{M1} such that a higher channel profit is attained in model MM than RR if β̄^h_{M1} < β^M_w < β̄^h_{M4}; a higher channel profit is attained in model RR than MM if β^M_w > β̄^h_{M4}; and an equal channel profit is achieved if β^M_w = β̄^h_{M4}, h ∈ {P, C}.
 (ii) If φ_{R3} < φ̄^h_{R3} and β̄^h_{R1} < β^R_w < β̄^h_{R2}, a higher channel profit is attained in model RR than MM, h ∈ {P, C}.

The proof of Proposition 5.3.5 is furnished in Appendix H.

Proposition 5.3.5 shows that the comparison of the channel profit between models MM and RR depends on the net benefit of offering warranty for remanufactured products (ϕ_{i3}) and quadratic warranty cost parameters regardless of the manufacturer's remanufacturing strategy if $c_w^M = c_w^R = c$. When the net benefit of the retailer offering warranty for reman-ufactured products is low ($\phi_{R3} \le \bar{\phi}_{R3}^h$) and it has a high quadratic warranty cost parameter ($\beta_w^R > \bar{\beta}_{R2}^h$), or the net benefit of the retailer offering warranty for remanufactured products is high ($\phi_{R3} > \bar{\phi}_{R3}^h$), even if the manufacturer is farther away from the market compared to the retailer, its relative quadratic warranty cost advantage $(\bar{\beta}_{M1}^h < \beta_w^M < \bar{\beta}_{M4}^h)$ outweighs the double-marginalization effect, leading to a higher channel profit in model *MM* than that in model *RR*. As β_w^M increases from the lower end, the manufacturer's relative quadratic warranty cost advantage shrinks. When β_w^M increases to $\bar{\beta}_{M4}^h$, the channel profit reaches parity for models *MM* and *RR*. When β_w^M exceeds $\bar{\beta}_{M4}^h$, the retailer has a relative quadratic warranty cost advantage, the warranty efficiency for remanufactured products in model MM turns lower than that in model RR and, then, a higher channel profit is attained in model RR. When the net benefit of the retailer offering warranty for remanufactured products is low $(\bar{\phi}_{R3} < \bar{\phi}_{R3}^h)$ but it has an advantageous quadratic warranty cost parameter $(\bar{\beta}_{R1}^h < \beta_w^R < \bar{\beta}_{R2}^h)$, the retailer's proximity to the market and direct influence on market demand by offering warranty lead to a higher channel profit in model *RR* than *MM*.

Next, we compare consumer surplus between the two warranty models MM and RR.

PROPOSITION 5.3.6 Under scenario I when $c_w^M = c_w^R = c$, the following results hold.

- (i) When β^R_w ≥ β^h_{R3}, there exists β^h_{M5} ≥ β^h_{M1} such that consumer surplus is higher in model MM if β^h_{M1} ≤ β^M_w < β^h_{M5}; it is the same for models MM and RR if β^M_w = β^h_{M5}; it is higher in model RR if β^M_w > β^h_{M5}, h ∈ {P, C}.
 (ii) When β^h_{R1} ≤ β^R_w < β^h_{R3}, consumer surplus is higher in model RR, h ∈ {P, C}.

The proof of Proposition 5.3.6 is given in Appendix I.

Proposition 5.3.6. (i) shows that consumer surplus is higher in model MM than RR if the retailer's provision of warranty has a sufficiently large quadratic cost parameter ($\beta_{R3}^{R} > \bar{\beta}_{R3}^{h}$) and the manufacturer's provision of warranty has a relative quadratic cost advantage ($\bar{\beta}_{M1}^{h} < \beta_{w}^{M} < \bar{\beta}_{M5}^{h}$. NB: $\bar{\beta}_{M1}^{h}$ is the lower bound of β_{w}^{M} to ensure that $t^{MM-h*} \le n = 1$). Under this condition, if the manufacturer commits to partial remanufacturing, demands for new products in period 1 are the same in models MM and RR, but it is higher in model MM than RR if the manufacturer commits to complete remanufacturing. On the other hand, regardless of the manufacturer's remanufacturing strategy, in period 2, offering warranty by the manufacturer in model MM has a more notable impact on enhancing demand for remanufactured products compared to model RR. Although this causes more severe cannibalisation of demand for new products in period 2, the increase in the quantity of remanufactured products is more rapid than the decrease in the quantity of new products. Therefore, it is natural that consumer surplus is higher in model MM than RR regardless of the manufacturer's remanufacturing strategy.

However, when β_w^M increases to $\bar{\beta}_{M5}^h$, the manufacturer's relative quadratic cost advantage of offering warranty disappears and parity is reached in the quantities of new and remanufactured products, leading to the same consumer surplus in models *MM* and *RR*. When β_w^M further increases beyond $\bar{\beta}_{M5}^h$, the retailer now has a relative quadratic cost advantage of offering a warranty. In this case, if the manufacturer commits to partial remanufacturing, demands for new products in period 1 are the same in models MM and RR, but offering warranty by the retailer in model RR has a more significant impact on enhancing demand for remanufactured products, which outweighs the demand cannibalisation of new products in period 2, leading to higher consumer surplus in model *RR* than *MM*. If the manufacturer is engaged in complete remanufacturing, offering warranty by the retailer in model *RR* is more effective in enhancing demand for remanufactured products and, subsequently, the complementary new products in period 1. On the other hand, offering warranty by the retailer causes more severe cannibalisation of demand for new products in period 2 in model *RR*, but the cannibalisation does not outweigh the increases in demands for remanufactured products in period 2 and new products in period 1, resulting in higher consumer surplus in model *RR* than *MM*. Similarly, Proposition 5.3.6. (*ii*) corresponds to the case that the retailer possesses relative quadratic cost advantage of offering warranty ($\beta_w^R < \overline{\beta}_{R3}^h$) and, hence, higher consumer surplus is achieved when the retailer provides warranty in model *RR*.

6. Numerical experiment

In this section, we present numerical studies to verify the analytical results in Section 5 by comparing equilibrium decisions as well as profits and consumer surplus between different models with a general setting of $c_w^M \neq c_w^R$ and $\beta_w^M \neq \beta_w^R$. Let Q = 220, $c_n = 100$, $c_r = 60$, $\delta = 0.7$, $c_w^R = 5$, $\beta_w^R = 80$, $\varepsilon_n = 10$, $\varepsilon_r = 8$, and we obtain the relevant charts by varying the values of parameters β_w^M and c_w^M . Because the manufacturer's remanufacturing strategy has no significant impact on the main results, the numerical studies are confined to the scenario of partial remanufacturing. We first plot the warranty period and retail price of remanufactured products in models *MM* and *RR* in Figure 1.

It can be seen from Figure 1 that, when β_w^M and c_w^M are small and the manufacturer warranty has significant cost advantage, the *MM* model has a longer warranty period and higher retail price for remanufactured products than the *RR* model does, and the higher the β_w^M and c_w^M , the shorter (longer) the warranty period and the lower (higher) the retail price for remanufactured products in model *MM* (*RR*). When the warranty cost parameters meet the condition

$$\frac{(c_w^M - 8)(0.7c_w^M + 3)}{(c_w^M - 8)^2 - 0.84\beta_w^M} < \frac{c_w^R(0.35c_w^R - 1.3) - 12}{(c_w^R - 8)^2 - 0.42\beta_w^R} \quad \left(\frac{8208 + c_w^M((0.175c_w^M + 134.05)c_w^M - 2109.6) - 109.62\beta_w^M}{(c_w^M - 8)^2 - 0.84\beta_w^M}\right) < \frac{8304 + c_w^R((0.175c_w^R + 131.25)c_w^R - 2099.2) - 54.81\beta_w^R}{(c_w^R - 8)^2 - 0.42\beta_w^R}\right),$$

the retailer warranty cost advantage becomes significant and, hence, the warranty period (retail price) of remanufactured products in model *MM* becomes shorter (lower) than that in model *RR*. By fixing $c_w^M = c_w^R = 5$, it is confirmed that, if $\beta_w^M > \bar{\beta}_{M2}^P = -10.714 + \beta_w^R$ ($\beta_w^M > \bar{\beta}_{M3}^P = -13.187 + 1.115\beta_w^R$), the warranty period (retail price) of remanufactured products in model *MM* is shorter (lower) than that in model *RR*. These results verify the conclusions in Proposition 5.2.3 and Corollary 5.2.2.

Next, under the same settings, we plot the individual and channel profits as well as consumer surplus against the two parameters β_w^M and c_w^M in Figure 2.

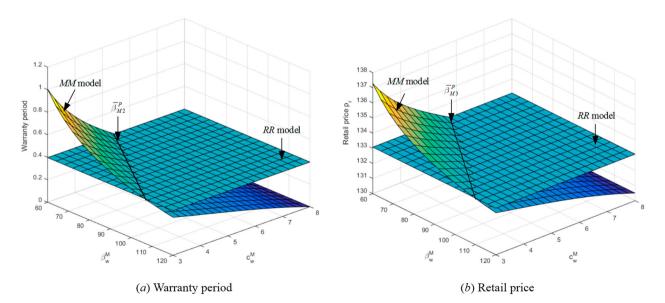
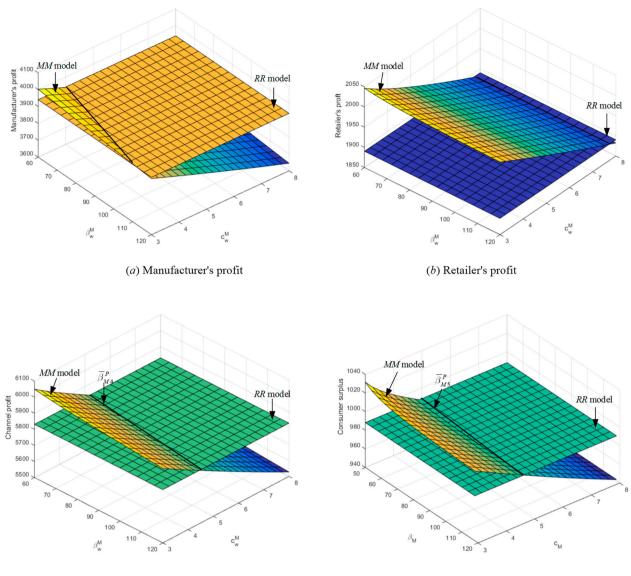


Figure 1. The warranty period and retail price of remanufactured products in the two warranty models.



(c) Channel profit

(d) Consumer surplus

Figure 2. Comparisons of individual and channel profits, and consumer surplus between the two warranty models.

It is clear from Figure 2 that when manufacturer warranty has a significant relative cost advantage at sufficiently small β_w^M and c_w^M , individual and channel profit, as well as consumer surplus, are all higher in model *MM* than those in model *RR*. However, as β_w^M and c_w^M increase, these metrics in model *MM* decrease and turn lower than those in model *RR*. In terms of individual profit, we find that the manufacturer achieves a higher profit in model *RR* than that in *MM* regardless of β_w^M if $c_w^M \ge c_w^R$, and the retailer attains a higher profit in model *MM* than that in model *RR* regardless of β_w^M if $c_w^R \ge c_w^R$, and the retailer attains a higher profit in model *MM* than that in model *RR* regardless of β_w^M if $c_w^R \ge c_w^R$. This result indicates that, if c_w^M is significantly larger than c_w^R , both members are better off in profitability when the retailer offers warranty for new and remanufactured products. In terms of the channel profit, by setting $c_w^M = c_w^R = 5$, one can confirm that $\bar{\beta}_{M4}^P = 74.9396$ exists if $\phi_{R3} < (2/3)\phi_{R1}$ and $\beta_w^R > \bar{\beta}_{R2}^P = 46.5356$. When $\beta_w^M < \bar{\beta}_{M4}^P = 74.9396$ ($\beta_w^M > \bar{\beta}_{R3}^P = 67.8571$ and $\beta_w^M < \bar{\beta}_{M5}^P = 40$ ($\beta_w^R > \bar{\beta}_{R3}^P = 67.8571$ and $\beta_w^M > \bar{\beta}_{M5}^P = 40$), consumer surplus, if $\beta_w^R > \bar{\beta}_{R3}^P = 67.8571$ and $\beta_w^R < \bar{\beta}_{M5}^P = 40$), consumer surplus is higher (lower) in model *MM* than that in model *RR*. These results verify the conclusions in Propositions 5.3.4, 5.3.5 and 5.3.6.

In general, these numerical studies allow us to infer that individual and channel profits, as well as consumer surplus in model *MM*, are higher than those in model *RR* when both the manufacturer's quadratic and linear warranty $\cos(\beta_w^M \operatorname{and} c_w^M)$

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are sufficiently efficient compared to those in the retailer warranty model *RR*. Otherwise, they are lower in model *MM* than those in model *RR*.

7. Conclusions

For a two-period CLSC consisting of a manufacturer and a retailer, this study establishes four Stackelberg game models to incorporate the warranty policies for new and remanufactured products. The manufacturer is modelled as the leader and the retailer is the follower. We consider two warranty models where either the manufacturer or the retailer offers warranty for new and remanufactured products and two corresponding benchmark models with a warranty for new products only. We derive the optimal wholesale and retail pricing as well as warranty period decisions for the models. By analysing and comparing equilibrium solutions and the resulting sales quantities, individual and channel profits as well as consumer surplus, the following results are obtained.

Firstly, the conditions are identified to guarantee the offering of warranty for remanufactured products: the manufacturer in model *MM* and the retailer in model *RR* are willing to offer warranty for remanufactured products if and only if they can benefit from it (Lemma 5.1.1). Secondly, the remanufacturing strategy (partial or complete remanufacturing) and warranty for remanufactured products do not affect the pricing strategies of new products in the second period, but they influence the pricing of new products in the first period and remanufactured products in the second period (Proposition 5.1.1). Thirdly, offering warranty for remanufactured products improves the sales quantity of remanufactured products, thereby enhancing individual and channel profits, and consumer surplus in the CLSC (Proposition 5.1.2); meanwhile, it also attains a more equitable channel profit distribution between the two members if the manufacturer provides warranty for remanufactured products (Corollary 5.1.1). Finally, by comparing the two warranty models *MM* and *RR*, we find that the member who has a relative warranty cost advantage offers a longer warranty period for remanufactured products (Proposition 5.2.3). If the manufacturer (retailer) has a significant linear and quadratic warranty cost advantage over the retailer (the manufacturer), the manufacturer (retailer) should be entrusted to offer the warranty for new and remanufactured products, which can lead to higher individual and channel profitability as well as consumer surplus (Figure 2).

This paper only considers a CLSC consisting of one manufacturer and one retailer where the manufacturer produces new products in two periods and remanufactures used products in the second period, and sells them to the retailer. In practice, remanufacturing may be performed by a third-party remanufacturer, and products may be sold to multiple retailers. Therefore, future research can be extended to consider warranty policies for new and remanufactured products with competition and cooperation among multiple agents.

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Supplemental data

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