



Article Integrated Natural Gas, Heat, and Power Dispatch Considering Wind Power and Power-to-Gas

Jun Ye * and Rongxiang Yuan

School of Electrical Engineering, Wuhan University, Wuhan 430072, China; 00010427@whu.edu.cn * Correspondence: yejun@whu.edu.cn

Academic Editor: Tomonobu Senjyu Received: 9 March 2017; Accepted: 10 April 2017; Published: 13 April 2017

Abstract: A large amount of wind power has to be curtailed due to the inflexibility of the combined heat and power (CHP) system in the heating season in northern China. The power-to-gas (P2G) technology, which uses electricity to produce hydrogen or synthetic natural gas, has become a promising energy conversion option for the utilization of surplus power energy. In this paper, an integrated natural gas, heat, and power dispatch (INGHPD) model which balances natural gas, heat, and power demand considering wind power and a P2G unit, is proposed. A natural gas network and P2G are modeled and integrated into the dispatch model. To demonstrate the effectiveness of the proposed model, an integrated energy system consisting of a six-bus power system, a six-node natural gas system, and a district heating system is simulated. The benefits of P2G are investigated in terms of reducing wind power curtailment, as well as system operation cost and CO₂ emissions. The results in the deterministic model show that with the introduction of 40 MW P2G, the wind power curtailment rate decreases from 24.0% to 9.7%. The daily wind power energy consumed by P2G reaches 256 MWh and the daily CO_2 emissions reduction reaches 46,080 kg. Additionally, the impact of the power and heat demand on the gas production of P2G and of the P2G capacity on the wind power curtailment are also investigated. P2G tends to generate more natural gas when the power demand is low and the heat demand is high.

Keywords: power-to-gas; natural gas system; combined heat and power; economic dispatch; wind power

1. Introduction

Wind energy has achieved a great development all over the world in recent years. In China, the gross installed capacity of wind power reached 97 GW by the end of 2014, representing 27% of the global installed capacity. Moreover, eight wind power generation bases have been planned, mainly located in northern China, each of which is planned to have an installed capacity of more than 10 GW by 2020 [1]. Combined heat and power (CHP) is a technology which can simultaneously satisfy heat and power requirements with a high efficiency. Compared to the separated generation of heat and power by pure heating and power technologies, the efficiency can improve the performance by 10–40% in CHP units [2]. CHP units play an important role in northern China. For example, in the Jilin Province, over 70% of the heat demand is supplied by CHP units [3]. However, in the winter, when the heat demand is high and the power demand is low, CHP units have to meet the heat demand and then generate a considerable amount of electricity, leaving little room for wind power integration. This leads to a high wind power curtailment.

The natural gas-fired units (NGFU) and combined heat and power units, due to their high efficiency, low investment cost, operational flexibility, and low environmental pollution in comparison with conventional coal plants, have grown dramatically in the last decade and play an important

role in the power system [4]. Gas-fired units establish the interdependence of the power system and natural gas system [5,6], while CHP units provide the linkage between the heating system and power system [7]. The economy and security of the three different systems would affect each other. For example, the natural gas supply could influence the dispatch and operation of gas-fired power units and CHP units. The operation of CHP units would then affect the heat supply. The rapid development of natural gas-fired plants strengthens the interdependence of gas, heat, and electricity. Thus, it is significant to investigate the operation optimization of the integrated natural gas, heat, and power system considering their operational constraints.

Power-to-gas (P2G) is a technology which uses electricity to produce hydrogen or synthetic natural gas that can be later utilized for re-electrification or heating [8–12]. Surplus wind power can be utilized in this method and stored in the natural gas system [13,14]. P2G provides the bidirectional energy flow between a power and natural gas system, which can largely increase the efficiency of energy utilization. It provides an important flexibility option for the CHP system in northern China and needs to be further studied.

In this paper, an integrated natural gas, heat, and power dispatch (INGHPD) model which balances the natural gas load, heat load, and power load is proposed, with a consideration of the constraints of the three systems. The benefits of P2G in the integrated energy system are evaluated in terms of reducing the wind power curtailment, system operation cost, and CO_2 emissions.

The main contributions of this paper are illustrated as follows:

- (1) A novel framework of an integrated energy system considering wind power and P2G is proposed (as depicted in Figure 1), in which a natural gas system, heating system, and power system are included. The INGHPD model, aimed at minimizing the system operation cost, is proposed.
- (2) A natural gas network is modeled and its system constraints are taken into account in the optimal dispatch model.
- (3) P2G is integrated into the dispatch model and its benefits in reducing the wind power curtailment, system operation cost, and CO₂ emissions are evaluated. Factors influencing the performance of P2G are also investigated.

This paper is organized as follows: The related work is briefly reviewed in Section 2. The key components of the integrated natural gas, heat, and power system are modeled in Section 3. The INGHPD model considering wind power and P2G is formulated in Section 4. In Section 5, a case study is simulated to demonstrate the effectiveness of the proposed method. Conclusions are drawn in Section 6.

2. Related Work

The integration of a power system and natural gas system has recently been investigated [15–19]. A mixed-integer linear programing security-constrained optimal power and gas flow is formulated in [16]. A coordinated stochastic model is proposed in [19] for studying the interdependence of electricity and natural gas transmission networks. In [20], the security-constrained unit commitment is modeled considering natural gas transmission constraints. Reference [21] explores the impact of the electricity demand response in the integrated electricity and natural gas network. Firming the variability of wind power is analyzed in [22], with the consideration of interdependent power and natural gas infrastructures.

However, P2G is not taken into consideration in the aforementioned studies. The impacts of P2G on reducing the operation cost and CO₂ emissions, and relieving electricity and natural gas congestions, are evaluated in [23]. Reference [24] analyzes the optimal capacity and spatial distribution of P2G plants in an 85% renewable energy scenario. Reference [25] assesses the potential of P2G with the integration of gas seasonal storage in terms of gas production from renewable energy, as well as its impact on natural gas prices. Reference [26] focuses on a steady-state analysis of the integrated natural gas and power system considering P2G. A unified energy flow formulation is developed to describe

the nodal balance and branch flow in both systems. However, the heat supply is not considered and its impact on P2G is not investigated in previous studies.

The combined operation of integrated electricity and heat systems is also investigated in the recent papers. In [27], heat storage tanks and electric boilers are introduced into the CHP system to increase the wind power integration. In [28], the energy storage capability of a district heating network is investigated to improve the overall efficiency of the integrated heat and power system. In [29], the electric heat pump and building thermal inertia are considered to decouple the strong linkage of electric power and heat supplies in the CHP system.

In contrast to the previous work, we jointly optimize the natural gas, heat, and power supplies to promote wind power integration with the consideration of P2G. This work is a beneficial supplement for the previous works.

3. Model of Integrated Natural Gas, Heat and Power System

3.1. Structure of Integrated Natural Gas, Heat, and Power System

The structure of an integrated natural gas, heat, and power system is depicted in Figure 1. Natural gas is provided for the CHP units, NGFUs, and residential gas loads. The power load is satisfied by the CHP units, NGFUs, and wind power, while the heat load is satisfied by the CHP units. Surplus power energy can be utilized to produce hydrogen or synthetic natural gas by power-to-gas plants, which is then inputted into the natural gas network. It should be noted that other heat sources such as a gas-fired boiler and heat storage could also be introduced to the system, but they are not the focus of this paper and are not modeled here.



Figure 1. Structure of an integrated natural gas, heat, and power system.

3.2. CHP Unit

A typical feasible operation region [30] of the CHP is shown in Figure 2. The heat and power productions of the CHP are restricted by the boundary curve ABCD. The power and heat production of the CHP unit are constrained by three operational limits: minimum fuel consumption, maximum fuel consumption, and maximum heat extraction [31]. The corners of the operating region are called the extreme characteristic points of the CHP unit. The power production, heat production, and gas

cost of each point within the feasible operation region can be represented by the convex combination of extreme characteristic points [32]. The relationship can be presented by:

$$p_{i,t} = \sum_{j \in J} \alpha_j x_{j,t}$$

$$q_{i,t} = \sum_{j \in J} \beta_j x_{j,t}$$

$$C_{i,t}^{\text{CHP}} = \sum_{j \in J} \gamma_j x_{j,t}, \quad i \in \Omega_{\text{CHP}}, j \in J$$

$$\sum_{j \in J} x_{j,t} = 1$$

$$x_j \ge 0$$
(1)

It should be noted that the dispatch of one CHP unit may have an impact on the remaining capacity of the heat pipelines and electrical lines, and thus have an influence on the feasible region of other CHP units. In this paper, it is assumed that the capacities of the heat pipelines and electrical lines are large enough and the impact is not considered.



Figure 2. Feasible operation region of a typical CHP unit.

3.3. Natural Gas Network

The main components of a natural gas system include natural gas wells, transmission pipelines, and natural gas loads. In this paper, the model of a natural gas system is presented by using the steady-state mathematical model.

Natural gas supply: In general, natural gas suppliers are gas wells, which are seen as positive gas injections at related nodes. The gas supplies are restricted by their upper and lower limits:

$$S_i^{\min} \le S_{i,t} \le S_i^{\max} \qquad i \in \Omega_{\rm GS} \tag{2}$$

Natural gas loads: The gas loads are seen as negative injections at related nodes. Natural gas loads can be classified into residential, commercial, and industrial loads. Natural gas-fired units are the industrial load. The gas loads are restricted by their upper and lower limits:

$$L_i^{\min} \le L_{i,t} \le L_i^{\max} \qquad i \in \Omega_{\rm GL} \tag{3}$$

Pipelines: The pipelines are used to transmit natural gas from the gas wells to gas customers. The pipelines can be classified into active pipelines and passive pipelines. The active pipelines are comprised of compressors, which are equipped to increase the gas pressure of the pipelines and thus increase the transmission capacity. In this paper, we only consider the passive pipelines. The natural gas flow in the pipelines can be modeled by the Weymouth equation [33]:

$$f_{mn} = sgn(\pi_m, \pi_n) \times C_{mn} \sqrt{|\pi_m^2 - \pi_n^2|}$$

$$sgn(\pi_m, \pi_n) = \begin{cases} 1 & \pi_m \ge \pi_n \\ -1 & \pi_m < \pi_n \end{cases}$$
(4)

$$\pi_m^{\min} \le \pi_m \le \pi_m^{\max} \tag{5}$$

where C_{mn} is the pipeline constant which depends on the temperature, length, friction, diameter, and natural gas compositions. The function of $sgn(\pi_m, \pi_n)$ represents the direction of the gas flow through the pipeline. When the pressure of node *m* is higher than node *n*, it is equal to one; otherwise, it is -1. The pressure of each node should be maintained within a certain interval, as depicted in (5).

To improve the computation efficiency, the Weymouth equation is linearized by a piecewise linear function [33,34]. First, Equation (4), when $\pi_m \ge \pi_n$, can be expressed as (6).

$$f_{mn}^2 = C_{mn}^2 \left(\pi_m^2 - \pi_n^2 \right)$$
(6)

Then, in the optimization model, the pressure variable of each node can be defined by $p_m = \pi_m^2$, which could eliminate the nonlinearity on the right side of the equation. Moreover, the quadratic term on the left side of Equation (6) can be piecewise-linearly approximated, as shown in (7).

$$f_{mn}^{2} = \underline{f_{mn}^{2}} + \sum_{l=1}^{N_{l}} \alpha_{mn,l} \times F_{mn,l}$$

$$0 \le F_{mn,l} \le f_{mn,l+1} - f_{mn,l}$$

$$f_{mn} = \sum_{l=1}^{N_{l}} F_{mn,l} + \underline{f_{mn}}$$
(7)

Natural gas flow conservation: With respect to node *m*, the gas injected into the node should be equal to the gas extracted from the node. Thus, natural gas flow conservation can be depicted as:

$$\sum_{i \in \Omega_{\rm GS}} AS_{i,t} - \sum_{i \in \Omega_{\rm GL}} BL_{i,t} - \sum_{n \in \Omega_{\rm GC(m)}} f_{mn} = 0$$
(8)

The first term represents the gas supply from the gas suppliers to node m. The second term represents the gas load at node m. The third term represents the gas flow rate in the pipelines which are connected with node m.

3.4. Power to Gas

The power-to-gas technology utilizes surplus power energy from renewable energy to produce hydrogen by the process of electrolysis. The produced hydrogen can be injected into the natural gas network or further converted to synthetic natural gas by additional methanation combined with carbon dioxide. However, the amount of hydrogen injected into the natural gas system should be limited, since blending hydrogen into the natural gas network will reduce the energy density of the gas and have a bad effect on the pipeline material. In the UK, the maximal level of hydrogen in the natural gas network is currently limited to 0.1% (by volume) [25]. Therefore, in this paper, we assume that all of the produced hydrogen is converted to natural gas. The conversion from power to natural gas production has a 60–65% efficiency [35].

In this paper, a power-to-gas plant is modeled to covert the power to natural gas with a certain efficiency [36], as demonstrated in (9). The volumetric quantity of natural gas can be converted by Equation (10). The P2G power is restricted by its installed power capacity, as shown in (11). The incremental power consumption of P2G is restricted by its maximum ramping rate, as depicted in (12).

$$E_{i,t}^{P2G} = \eta_i^{P2G} \times p_{i,t}^{P2G} \qquad i \in \Omega_{P2G}$$
(9)

$$L_{i,t}^{P2G} = E_{i,t}^{P2G} / HHV_{NG} \qquad i \in \Omega_{P2G}$$
(10)

$$p_{i,t}^{\text{P2G}} \le \overline{p_i^{\text{P2G}}} \qquad i \in \Omega_{\text{P2G}}$$
(11)

$$-RAMP_{i}^{P2G,down} \le p_{i,t}^{P2G} - p_{i,t-1}^{P2G} \le RAMP_{i}^{P2G,up}$$
(12)

3.5. Natural Gas-Fired Unit

NGFUs consume gas to generate power according to the flexible gas contracts and can be regarded as gas loads in the natural gas network. The power production derived from natural gas consumption is modeled in (13). Then, the natural gas consumption cost can be represented as (14).

$$P_{i,t} = \eta_i^{\text{NGFU}} \times L_{i,t} \times HHV_{\text{NG}} \qquad i \in \Omega_{\text{NGFU}}$$
(13)

$$C_{i,t}^{\text{NGFU}} = \rho_{gas} \times L_{i,t} \qquad i \in \Omega_{\text{NGFU}}$$
(14)

4. Formulation of INGHPD Model

In this section, the INGHPD model is formulated considering wind power and P2G, which seeks the optimal dispatch of natural gas, power, and heat sources, while satisfying the physical and security constraints of the natural gas, heat, and power system. It is assumed that the power units remain on during the scheduling horizon.

4.1. Objective Function

The objective of the dispatch model is to minimize NGFUs, the operating cost of the CHP units, and the revenue of the natural gas produced by P2G over the scheduling horizon, which can be expressed as:

minimize
$$\sum_{t \in T} \sum_{i \in \Omega_{\text{NGFU}}} C_{i,t}^{\text{NGFU}} + \sum_{t \in T} \sum_{i \in \Omega_{\text{CHP}}} C_{i,t}^{\text{CHP}} - \sum_{t \in T} \sum_{i \in \Omega_{\text{P2G}}} \rho_{gas} \times L_{i,t}^{\text{P2G}}$$
(15)

4.2. Constraints

(1) Power balance constraints: The power demand is satisfied by NGFUs, CHP units, and wind power.

$$\sum_{i \in \Omega_{\text{NGFU}}} p_{i,t} + \sum_{i \in \Omega_{\text{CHP}}} p_{i,t} + \sum_{i \in \Omega_{\text{WP}}} p_{i,t}^{\text{w}} = p_t^{\text{Load}}$$
(16)

(2) Heat balance constraints: The heat demand is satisfied by the CHP units only.

$$\sum_{i \in \Omega_{\text{CHP}}} q_{i,t} = q_t^{\text{Load}} \tag{17}$$

(3) Power output constraints of NGFUs: The power outputs of the NGFUs are constrained by their technical limits.

$$\underline{P}_i \le p_{i,t} \le \overline{P}_i \qquad i \in \Omega_{\text{NGFU}} \tag{18}$$

(4) Ramping rate constraints of NGFUs and CHP units: The incremental power outputs of the power generation units are restricted by their maximum ramping rates.

$$-RAMP_{i}^{\text{down}} \leq p_{i,t} - p_{i,t-1} \leq RAMP_{i}^{\text{up}} \qquad i \in \Omega_{\text{NGFU}} \cup \Omega_{\text{CHP}}$$
(19)

(5) Power output constraints of wind farms: The integrated wind power should not exceed its forecasted wind power.

$$0 \le p_{i,t}^{\mathsf{w}} \le p_{i,t}^{\mathsf{fore}} \quad i \in \Omega_{\mathsf{WP}} \tag{20}$$

(6) Spinning reserve constraints: A certain level of spinning reserve capacity is required to deal with the system contingencies.

$$\sum_{i \in \Omega_{CHP} \cup \Omega_{NGFU}} \overline{P}_i - \sum_{i \in \Omega_{CHP} \cup \Omega_{NGFU}} p_{i,t} \ge SR^{up}$$

$$\sum_{i \in \Omega_{CHP} \cup \Omega_{NGFU}} p_{i,t} - \sum_{i \in \Omega_{CHP} \cup \Omega_{NGFU}} \underline{P}_i \ge SR^{down}$$
(21)

(7) Power transmission constraints: Transmission flow should not exceed the transmission capacity.

$$\left|\sum_{n\in\Omega_{\text{bus}}} PDTF_{l,n} \times \left(\sum_{i\in\Omega_{\text{CHP}}\cup\Omega_{\text{NGFU}}} p_{i,t} + \sum_{i\in\Omega_{\text{WP}}\cup\Omega_{\text{P2G}}} p_{i,t} - D_{n,t}\right)\right| \le F_l$$
(22)

The other constraints are expressed in (1)-(14).

4.3. Robust Optimization Model

When uncertainty is taken into consideration, the optimization model can be formulated by using stochastic optimization, interval optimization, or robust optimization. In this paper, a robust optimization model is formulated to verify the feasibility of the proposed method when the uncertainties of wind power, power demand, and heat demand are considered. The objective of the robust optimization model is to minimize the worst-case total cost. The objective function can be formulated as:

$$\underset{u}{\text{minimize}} \underset{p^{\widetilde{w}}, p^{\widetilde{\text{Load}}}, q^{\widetilde{\text{Load}}} t \in T}{\text{minimize}} \sum_{i \in \Omega_{\text{NGFU}}} C_{i,t}^{\text{NGFU}} + \sum_{t \in T} \sum_{i \in \Omega_{\text{CHP}}} C_{i,t}^{\text{CHP}} - \sum_{t \in T} \sum_{i \in \Omega_{\text{P2G}}} \rho_{gas} \times L_{i,t}^{\text{P2G}}$$
(23)

where *u* represents the decision variables, p^{w} , p^{Load} , q^{Load} are the uncertain parameter vectors that represent the available wind power, power demand, and heat demand, respectively.

The uncertainty sets define the range of the uncertain wind power, power demand, and heat demand:

$$\Omega_{\rm WP,un} = \left\{ p_{i,t}^{\widetilde{W}} \middle| p_{i,t}^{\widetilde{W}} \in \left[p_{i,t}^{\rm fore} - \Delta p_{i,t}^{\rm w,down}, p_{i,t}^{\rm fore} + \Delta p_{i,t}^{\rm w,up} \right] \right\}$$
(24)

$$\Omega_{\text{P,un}} = \left\{ p_{i,t}^{\widetilde{\text{Load}}} \middle| p_{i,t}^{\widetilde{\text{Load}}} \in \left[p_t^{\text{Load}} - \Delta p_t^{\text{Load,down}}, p_t^{\text{Load}} + \Delta p_t^{\text{Load,up}} \right] \right\}$$
(25)

$$\Omega_{\text{Q,un}} = \left\{ q_{i,t}^{\text{Load}} \middle| q_{i,t}^{\text{Load}} \in \left[q_t^{\text{Load}} - \Delta q_t^{\text{Load,down}}, q_t^{\text{Load}} + \Delta q_t^{\text{Load,up}} \right] \right\}$$
(26)

The constraints in the robust optimization model are the same as those in the deterministic model, expect that the certain parameters are substituted by the uncertain parameters.

5. Case Study

5.1. System Description

The six-bus power system [28,30], as shown in Figure 3, consists of a CHP unit, two NGFUs, a P2G plant, and a wind farm. All of the three generation units are gas-fired units. The natural gas price is 30 \$/MWh [23].

The six-node natural gas system, as depicted in Figure 4, includes two gas wells, five pipelines, and six gas loads. NGFU1, NGFU2, and the CHP unit are connected to node 1, 2, and 3, respectively.

The main parameters of the power generation units are listed in Table 1 and the feasible operation region of the CHP unit is shown in Figure 5. The other three gas loads (L4, L5, L6) are fixed residential gas loads. The detailed parameters of the power and natural gas networks can be found in [21]. The difference is the parameters of the natural gas supplier and residential gas load, and they are listed in Table 2. A 40 MW P2G plant is connected to node 5. The efficiency of P2G is set to 65% for natural gas production.

The profiles of power, heat demand, and forecasted wind power are shown in Figure 6. The heat demand can be increased or decreased by 10% of the original heat load. The district heating control of individual heat consumption is not considered in this paper. The simulations are considered for the hourly generation dispatch over 24 h. All of the simulations were implemented in MATLAB R2013a and solved by Gurobi 6.5 on a computer with two Inter Core i5 CPU (2.5 GHz) and 4.0 GB RAM.





P2G



Figure 5. Feasible operation region of the CHP unit.





	NGFU1	NGFU1	СНР
Maximum power capacity (MW)	250	200	350
Minimum power output (MW)	120	80	175
Maximum heat capacity (MW)	-	-	450
Maximum ramping rate (MW/h)	50	50	70

Table 1. Main parameters of the power generation units.

Table 2. Parameters of	f the natural	gas supplier	and resid	lential gas	load

	Gas Well 1	Gas Well 2	L4	L5	L6
Natural gas injected (kcf/h)	1500-5000	2000-5000	-2500	-1700	-1000

5.2. Scenarios

To demonstrate the feasibility and effectiveness of the proposed model, three scenarios are presented:

Scenario 1: Dispatch model is formulated without considering the natural gas system constraints and P2G.

Scenario 2: Dispatch model is formulated considering the natural gas system constraints, but the P2G process is not integrated.

Scenario 3: Both the natural gas system constraints and P2G process are integrated to the dispatch model.

5.3. Results and Analysis

5.3.1. Necessity of Considering Natural Gas System Constraints

The hourly power dispatch results of the CHP unit and NGFU1 in Scenario 1 and Scenario 2 are shown in Figure 7. It can be observed that the power outputs of the CHP unit in the first eight hours are the same in the two scenarios, but at other times, the power outputs in Scenario 2 are less than those in Scenario 1. However, for NGFU1, the results are the opposite and the outputs increase, even in the off-peak hour (at 6:00). The power outputs of NGFU2 have not changed, but the wind power curtailment rate increases from 23.1% to 24.0%. The reason for this lies in the power outputs of the CHP unit between 9:00 and 24:00 in Scenario 2, which are restricted by natural gas transmission and supply constraints. This part of the power is substituted by NGFU1, which has a wider natural gas transmission and supply margin. Additionally, the increased power outputs of NGFU1 hinder part of the wind power integration.



Figure 7. Power dispatch results of (a) the CHP unit and (b) NGFU1.

The daily operation costs in these two scenarios are \$351,360 and \$352,730, respectively. The reason for this lies in the fact that NGFU1 is more frequently dispatched in Scenario 2, but it costs more compared with the CHP unit. The substituted power production by NGFU1 increases the total fuel cost.

Thus, it can be concluded that the natural gas system constraints influence the operation results and must be taken into account in the dispatch model.

5.3.2. Effect of P2G on Wind Power Curtailment, Fuel Cost, and CO₂ Emission

The power dispatch results of the wind power and P2G in Scenario 2 and 3 are depicted in Figure 8. It can be seen that in Scenario 2, the wind power is largely curtailed during the periods when the power demand is low and the heat demand is high. In Scenario 3, the integration of P2G largely promotes the wind power accommodation, decreasing the curtailment rate of the wind power from 24.0% to 9.7%. The reason for this is that the P2G utilizes the surplus wind power to produce natural gas, creating an extra margin for wind accommodation in the off-peak hours.

A comparison of the dispatch results in these two scenarios is summarized in Table 3. It can be observed that the operation cost of the integrated energy system decreases from Scenario 2 to 3. The P2G plant utilizes the free wind power to produce natural gas which can be used later for re-electrification, thereby decreasing the total fuel cost. The daily wind power energy consumed by P2G reaches 256 MWh. Moreover, according to [23], the CO₂ emission reduction factor is 180 kg/MWh. Thus, the daily CO₂ emission reduction reaches 46,080 kg.

Therefore, it can be indicated that the introduction of P2G will promote wind power integration, and reduce the fuel cost and CO₂ emissions of the integrated energy system.

Table 3.	Com	parison	of the	e dispa	atch	results	under	different	scenarios.
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	Scenario 2	Scenario 3
Fuel cost	352,730\$	347,570\$
Wind power consumed by P2G	0	256 MWh
Wind power curtailment rate	24.0%	9.7%



Figure 8. Power dispatch results of the wind power and P2G in (a) Scenario 2 and (b) Scenario 3.

5.3.3. Impact of Power and Heat Demand on P2G

In order to explore the impact of power and heat demand on P2G, the natural gas production of P2G under different power and heat demand levels is investigated. As shown in Figure 9, P2G tends to generate more natural gas when the power demand is lower and the heat demand is higher. It can be attributed to the energy storage capability of P2G: when the heat demand is high and the power demand is low, the heat and power production of the CHP units are deeply coupled. This leads to a high wind energy curtailment. By means of P2G, the surplus wind power will be utilized to produce gas fuel that can be stored in the existing natural gas networks and then be injected back into the power system through gas-fired generators. Thus, it can be indicated that P2G has the potential to increase the flexibility of the integrated energy system.



Figure 9. Impact of the power and heat demand on the gas production of P2G.

5.3.4. Impact of P2G Capacity on Wind Power Integration

The impact of different P2G capacities on wind power integration is investigated in Scenario 3. P2G capacities varying from 0 MW to 70 MW are integrated to the integrated energy system to

accommodate the otherwise curtailed wind power. The effects of P2G in reducing the wind curtailment rate are investigated at three different heat demand levels: 90%, 95%, and 100% of the original heat demand. As shown in Figure 10, the wind curtailment rate declines with the increasing capacity of P2G, independent of the heat demand level. However, there exhibits a declining marginal effect of increased P2G capacity on reducing wind power curtailments. The reason for this lies in the fact that when the P2G capacity increases, the available free wind power is nearly used up, resulting in a declining benefit.



Figure 10. Wind power curtailment rate under different P2G capacities.

5.3.5. Robust Optimization Result

In this section, the uncertainties of the wind power, power demand, and heat demand are considered. For simplicity, the maximum downward/upward deviation levels from the forecasted values are set to $\pm 5\%$, $\pm 2\%$, and $\pm 2\%$ for wind power, power demand, and heat demand, respectively. The robust optimization result is shown in Table 4.

Table 4. Comparison of robust dispa	atch results under different scenarios.
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	Scenario 2	Scenario 3
Fuel cost	359,420\$	355,440\$
Wind power consumed by P2G	0	237 MWh

Compared to the deterministic result, the fuel cost increases while the wind power consumed by P2G decreases, which is attributed to the uncertainties of the wind power, power demand, and heat demand. However, the fuel cost in Scenario 3 is still less than that in Scenario 2. This result reveals the feasibility of the proposed method when the uncertainties are considered.

6. Conclusions

In this paper, an INGHPD model that balances natural gas, heat, and power demands with energy sources including a CHP unit, NGFUs, wind power, and P2G unit is proposed. The natural gas system constraints are introduced to the dispatch model and the results show that the security constraints of the natural gas system influence the dispatch results and should be taken into account in the operation optimization.

P2G is used as a power load to consume surplus wind power and convert electricity to natural gas for a later use. The effects of P2G in the integrated natural gas, heat, and power system are investigated and the results show that P2G could largely promote wind power accommodation, as well as reduce the fuel cost and CO_2 emissions. With the introduction of 40 MW P2G in the deterministic model, the wind power curtailment rate decreases from 24.0% to 9.7%. The daily wind power energy consumed by P2G reaches 256 MWh. Moreover, the daily fuel cost and CO_2 emissions reduction reach

516\$ and 46,080 kg in the integrated energy system, respectively. In addition, the impact of the power and heat demand on the output of P2G and the impact of P2G capacity on the wind power curtailment are also investigated. P2G tends to generate more natural gas when the power demand is low and the heat demand is high. With the increase of P2G capacity, the wind curtailment rate declines, but exhibits a declining marginal effect.

Based on the proposed INGHPD model, many interesting issues could be further investigated. For instance, P2G facility can be used to relieve the power transmission limitations by consuming the power at certain nodes and transforming the energy by the natural gas system. Additionally, P2G can be utilized to produce natural gas at vulnerable nodes in the natural gas system, which could reduce the natural gas congestions. Utilizing the produced natural gas to directly generate heat and help decouple the heat and power production of CHP will also be analyzed in our future work.

Acknowledgments: This work was supported by the research funding of School of Electrical Engineering, Wuhan University. This sponsorship is gratefully acknowledged.

Author Contributions: Jun Ye and Rongxiang Yuan conceived and designed the experiments; Jun Ye performed the experiments; Jun Ye and Rongxiang Yuan analyzed the data; Jun Ye wrote the paper.

Conflicts of Interest: The authors declare no conflict of interest.

Nomenclature

Index set of CHP units
Index set of gas supplies
Index set of natural gas loads
Index set of buses
Index set of gas nodes connected with <i>m</i>
Index set of P2G units
Index set of NGFUs
Index set of wind power units
Uncertainty set of available wind power
Uncertainty set of power demand
Uncertainty set of heat demand
Index set of dispatch time steps
Index set of extreme characteristic points
x.
Power production, heat production and gas consumption cost of extreme
characteristic point <i>j</i>
Gas consumption cost of CHP i at time t
Lower/upper limit of gas supplier <i>i</i>
Lower/upper limit of gas load <i>i</i>
Pipeline constant
Lower/upper limit of nodal pressure
Lower bound of gas flow in the pipeline
Gas flow of block <i>l</i>
Slope of block <i>l</i>
Lower limit of block <i>l</i> of piecewise linear function
Node-gas supplier/load incidence matrix
Conversion efficiency of P2G unit <i>i</i>
Capacity of P2G unit <i>i</i>
Higher heating value of natural gas $(39.5 \text{ MJ}/\text{m}^3)$
Maximum downward/upward ramping rate of P2G unit <i>i</i>
Power plant efficiency of NGFU unit <i>i</i>
Natural gas cost of NGFU unit <i>i</i> at time <i>t</i>
Price of natural gas

p_t^{Load}	Forecasted power demand of the system at time step t
$\underline{P}_i/\overline{P}_i$	Minimum/maximum power output of NGFU unit <i>i</i>
$RAMP_i^{\text{down}}/RAMP_i^{\text{up}}$	Maximum downward/upward ramping rate of unit <i>i</i>
p_{it}^{fore}	Forecasted wind power at time <i>t</i>
q_t^{Load}	Forecasted heat demand of the system at time t
$D_{n,t}$	Power load at bus <i>n</i> at time <i>t</i>
F_{l}	Transmission capacity limit of line <i>l</i>
SR ^{up} /SR ^{down}	System upward/downward spinning reserve capacity requirement
$PDTF_{l,n}$	Power transfer distribution factor from bus n to line l
$\Delta p_{i,t}^{\mathrm{w,down}} / \Delta p_{i,t}^{\mathrm{w,up}}$	Maximum downward/upward deviation of wind power from the forecasted value
$\Delta p_t^{ m Load,down}/\Delta p_t^{ m Load,up}$	Maximum downward/upward deviation of power demand from the forecasted value
$\Delta q_t^{\text{Load,down}} / \Delta q_t^{\text{Load,up}}$	Maximum downward/upward deviation of heat demand from the forecasted value
Decision Variables:	
$p_{i,t}$	Power production of thermal power unit <i>i</i> at time t
q _{i,t}	Heat production of thermal power unit <i>i</i> at time <i>t</i>
$p_{i,t}^{\mathrm{W}}$	Wind power integrated to the power system at time <i>t</i>
x_i	Combination coefficient of extreme characteristic point <i>j</i>
S _{i,t}	Gas supply of node <i>i</i> at time <i>t</i>
L _{i,t}	Gas load of node <i>i</i> at time <i>t</i>
fmn	Gas flow between node <i>m</i> and <i>n</i>
π_m/π_n	Pressure of node m/n
E_{it}^{P2G}	Energy content of produced natural gas from P2G unit <i>i</i> at time <i>t</i>
L_{it}^{P2G}	Volumetric quantity of natural gas produced by P2G <i>i</i> at time <i>t</i>
$p_{i,t}^{P_2G}$	Consumed electric power of P2G unit <i>i</i> at time <i>t</i>
Uncertain Parameters:	-
$p_{i,t}^{\mathbf{W}}$	Actual available wind power of wind farm i at time t
$p_{i,t}^{\text{Load}}$	Actual power demand at time <i>t</i>
$q_{i,t}^{\text{Load}}$	Actual heat demand at time <i>t</i>

References

- 1. Feng, Y.; Lin, H.Y.; Ho, S.L.; Yanc, J.H.; Dong, J.N.; Fang, S.H.; Huang, Y.K. Overview of Wind Power Generation in China: Status and Development. *Renew. Sustain. Energy Rev.* **2015**, *50*, 847–858. [CrossRef]
- 2. Madlener, R.; Schmid, C. Combined Heat and Power Generation in Liberalised Markets and a Carbon-Constrained World. *GAIA-Ecol. Perspect. Sci. Soc.* **2003**, *12*, 114–120.
- 3. Jiang, L.P.; Wang, C.X.; Huang, Y.H.; Pei, Z.Y.; Xin, S.X.; Wang, W.S.; Ma, S.; Brown, T. Growth in Wind and Sun Integrating Variable Generation in China. *IEEE Power Energy Mag.* **2015**, *13*, 40–49. [CrossRef]
- 4. Cong, L.; Shahidehpour, M.; Zuyi, L.; Fotuhi-Firuzabad, M. Component and Mode Models for the Short-Term Scheduling of Combined-Cycle Units. *IEEE Trans. Power Syst.* **2009**, *24*, 976–990. [CrossRef]
- 5. Shahidehpour, M.; Yong, F.; Wiedman, T. Impact of Natural Gas Infrastructure on Electric Power Systems. *Proc. IEEE* **2005**, *93*, 1042–1056. [CrossRef]
- 6. Li, T.; Eremia, M.; Shahidehpour, M. Interdependency of Natural Gas Network and Power System Security. *IEEE Trans. Power Syst.* **2008**, *23*, 1817–1824. [CrossRef]
- Zhang, N.; Lu, X.; McElroy, M.B.; Nielsen, C.P.; Chen, X.; Deng, Y.; Kang, C. Reducing Curtailment of Wind Electricity in China by Employing Electric Boilers for Heat and Pumped Hydro for Energy Storage. *Appl. Energy* 2015, 184, 987–994. [CrossRef]
- De Boer, H.S.; Grond, L.; Moll, H.; Benders, R. The Application of Power-to-gas, Pumped Hydro Storage and Compressed Air Energy Storage in an Electricity System at Different Wind Power Penetration Levels. *Energy* 2014, 72, 360–370. [CrossRef]

- 9. Reiter, G.; Lindorfer, J. Global Warming Potential of Hydrogen and Methane Production from Renewable Electricity via Power-to-gas Technology. *Int. J. Life Cycle Assess.* **2015**, *20*, 477–489. [CrossRef]
- 10. Parra, D.; Patel, M.K. Techno-economic Implications of the Electrolyser Technology and Size for Power-to-gas Systems. *Int. J. Hydrogen Energy* **2016**, *41*, 3748–3761. [CrossRef]
- 11. Qadrdan, M.; Abeysekera, M.; Chaudry, M.; Wu, J.Z.; Jenkins, N. Role of Power-to-gas in an Integrated Gas and Electricity System in Great Britain. *Int. J. Hydrogen Energy* **2015**, *40*, 5763–5775. [CrossRef]
- 12. Schiebahn, S.; Grube, T.; Robinius, M.; Tietze, V.; Kumar, B.; Stolten, D. Power to gas: Technological Overview, Systems Analysis and Economic Assessment for a Case Study in Germany. *Int. J. Hydrogen Energy* **2015**, *40*, 4285–4294. [CrossRef]
- 13. Estermann, T.; Newborough, M.; Sterner, M. Power-to-gas Systems for Absorbing Excess Solar Power in Electricity Distribution Networks. *Int. J. Hydrogen Energy* **2016**, *41*, 13950–13959. [CrossRef]
- 14. Buchi, F.N.; Hofer, M.; Peter, C.; Cabalzar, U.D.; Bernard, J.; Hannesen, U.; Schmidt, T.J.; Closset, A.; Dietrich, P. Towards Re-electrification of Hydrogen Obtained from the Power-to-gas Process by Highly Efficient H-2/O-2 Polymer Electrolyte Fuel Cells. *RSC Adv.* **2014**, *4*, 56139–56146. [CrossRef]
- 15. Correa-Posada, C.M.; Sanchez-Martin, P. Security-Constrained Optimal Power and Natural-Gas Flow. *IEEE Trans. Power Syst.* **2014**, *29*, 1780–1787. [CrossRef]
- 16. Correa-Posada, C.M.; Sanchez-Martin, P. Integrated Power and Natural Gas Model for Energy Adequacy in Short-Term Operation. *IEEE Trans. Power Syst.* **2015**, *30*, 3347–3355. [CrossRef]
- Zhang, X.; Che, L.; Shahidehpour, M.; Alabdulwahab, A.; Abusorrah, A. Electricity-Natural Gas Operation Planning with Hourly Demand Response for Deployment of Flexible Ramp. *IEEE Trans. Sustain. Energy* 2016, 7, 996–1004. [CrossRef]
- 18. Alabdulwahab, A.; Abusorrah, A.; Zhang, X.; Shahidehpour, M. Stochastic Security-Constrained Scheduling of Coordinated Electricity and Natural Gas Infrastructures. *IEEE Syst. J.* **2015**, *3*, 1–10. [CrossRef]
- 19. Liu, C.; Lee, C.; Shahidehpour, M. Look Ahead Robust Scheduling of Wind-Thermal System with Considering Natural Gas Congestion. *IEEE Trans. Power Syst.* **2015**, *30*, 544–545. [CrossRef]
- 20. Cong, L.; Shahidehpour, M.; Yong, F.; Zuyi, L. Security-Constrained Unit Commitment with Natural Gas Transmission Constraints. *IEEE Trans. Power Syst.* **2009**, *24*, 1523–1536. [CrossRef]
- 21. Zhang, X.; Shahidehpour, M.; Alabdulwahab, A.; Abusorrah, A. Hourly Electricity Demand Response in the Stochastic Day-Ahead Scheduling of Coordinated Electricity and Natural Gas Networks. *IEEE Trans. Power Syst.* **2016**, *31*, 592–601. [CrossRef]
- 22. Alabdulwahab, A.; Abusorrah, A.; Zhang, X.; Shahidehpour, M. Coordination of Interdependent Natural Gas and Electricity Infrastructures for Firming the Variability of Wind Energy in Stochastic Day-Ahead Scheduling. *IEEE Trans. Sustain. Energy* **2015**, *6*, 606–615. [CrossRef]
- 23. Stephen, C.; Pierluigi, M. Integrated Modeling and Assessment of the Operational Impact of Power-to-Gas (P2G) on Electrical and Gas Transmission Networks. *IEEE Trans. Sustain. Energy* **2015**, *6*, 1234–1244.
- 24. Jentsch, M.; Trost, T.; Sterner, M. Optimal Use of Power-to-Gas Energy Storage Systems in an 85% Renewable Energy Scenario. *Energy Procedia* **2014**, *46*, 254–261. [CrossRef]
- 25. Clegg, S.; Mancarella, P. Storing Renewables in the Gas Network: Modelling of Power-to-gas Seasonal Storage Flexibility in Low-carbon Power Systems. *IET Gener. Transm. Distrib.* **2016**, *10*, 566–575. [CrossRef]
- 26. Zeng, Q.; Fang, J.; Li, J.; Chen, Z. Steady-state Analysis of the Integrated Natural Gas and Electric Power System with Bi-directional Energy Conversion. *Appl. Energy* **2016**, *184*, 1483–1492. [CrossRef]
- 27. Chen, X.Y.; Kang, C.Q.; Mark, O.; Xia, Q. Increasing the Flexibility of Combined Heat and Power for Wind Power Integration in China Modeling and Implications. *IEEE Trans. Power Syst.* **2015**, *30*, 1848–1857. [CrossRef]
- Li, Z.G.; Wu, W.C.; Shahidehpour, M.; Wang, J.H.; Zhang, B.M. Combined Heat and Power Dispatch Considering Pipeline Energy Storage of District Heating Network. *IEEE Trans. Sustain. Energy* 2016, 7, 12–22. [CrossRef]
- 29. Yang, Y.L.; Wu, K.; Long, H.Y.; Gao, J.C.; Yan, X.; Kato, T.; Suzuoki, Y. Integrated Electricity and Heating Demand-side Management for Wind Power Integration in China. *Energy* **2014**, *78*, 235–246. [CrossRef]
- 30. Yuan, R.; Ye, J.; Lei, J.; Li, T. Integrated Combined Heat and Power System Dispatch Considering Electrical and Thermal Energy Storage. *Energies* **2016**, *9*, 474. [CrossRef]
- 31. Alipour, M.; Zare, K.; Mohammadi-Ivatloo, B. Short-term Scheduling of Combined Heat and Power Generation Units in the Presence of Demand Response Programs. *Energy* **2014**, *71*, 289–301. [CrossRef]

- 32. Lahdelma, R.; Hakonen, H. An Efficient Linear Programming Algorithm for Combined Heat and Power Production. *Eur. J. Oper. Res.* **2003**, *148*, 141–151. [CrossRef]
- 33. Li, G.; Zhang, R.; Jiang, T.; Chen, H.; Bai, L.; Cui, H.; Li, X. Optimal Dispatch Strategy for Integrated Energy Systems with CCHP and Wind Power. *Appl. Energy* **2017**, *192*, 408–419. [CrossRef]
- 34. Miguel, C.; José, M. A Computationally Efficient Mixed-integer Linear Formulation for the Thermal Unit Commitment Problem. *IEEE Trans. Power Syst.* **2006**, *21*, 1371–1378.
- 35. Bailera, M.; Lisbona, P.; Romeo, L.M.; Espatolero, S. Power to Gas-biomass Oxycombustion Hybrid System: Energy Integration and Potential Applications. *Appl. Energy* **2016**, *167*, 221–229. [CrossRef]
- Li, G.; Zhang, R.; Jiang, T.; Chen, H.; Bai, L.; Li, X. Security-constrained Bi-level Economic Dispatch Model for Integrated Natural Gas and Electricity Systems Considering Wind Power and Power-to-gas Process. *Appl. Energy* 2016, 194, 696–704. [CrossRef]



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