

# Model-based Robust Adaptive Control for Power-generating Systems in the Presence of Long Time Delay

Lei Pan\*, Jiong Shen\*, Xiao Wu\*, Li Sun\*, Kwang. Y. Lee\*\*, Haitao Wang\*\*\*

\* Key Laboratory of Energy Thermal Conversion and Control of Ministry of Education, Southeast University, Nanjing, China (Tel: 86-25-83792379; e-mail: leipan@seu.edu.cn; shenj@seu.edu.cn;).

\*\* Department of Electrical & Computer Engineering, Baylor University, Waco, TX 76798-7356, USA (e-mail: Kwang\_Y\_Lee@baylor.edu)

\*\*\* Jiangsu Power Design Institute Co., Ltd. of China Energy Engineering Group, Nanjing, China, (e-mail: wanghaitao@jspdi.com.cn)

**Abstract:** This paper proposes a model-based robust adaptive control (MB-RAC) which is derived from the  $L_1$  robust adaptive control ( $L_1$ -RAC). By inheriting excellent control performance from the  $L_1$ -RAC for systems with nonlinearity and uncertain conditions, the MB-RAC offers its own feature for dealing with a long time delay by using dual-feedback adaptive law from the built-in model and the plant. A nonlinear boiler-turbine-generator unit augmented with time delays is adopted as the plant for verifying the MB-RAC. Simulation results present good control performances of the MB-RAC in a wide-range load-following process with long time delays and show its strong robustness to inner model mismatches from the plant on both dynamics and time delays. The MB-RAC is shown to be reliable and easy to implement for industrial processes.

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**Keywords:** robust adaptive control, time delay, uncertainty, boiler-turbine system, nonlinearity, disturbance, load following.

## 1. INTRODUCTION

Nowadays, boiler-turbine power-generating systems are facing more and more challenges in operations, such as fast load-following demands, wide-range nonlinear operations, unmeasured disturbances (e.g., heat rate influenced by flue emission control), unknown time-varying uncertainties related to frequent fuel quality variation, and the last but not the least, frequency and voltage disturbances when it is connected to grid involving much uncertain power supply from renewable energy resources (Pan et al., 2015). In dealing with these issues, the controllers for boiler-turbine power systems should achieve fast, adaptive, robust and stable control performance.

Improving load-following capability of boiler-turbine-generator systems in the presence of wide and rapid load changes has been a hotspot and drawn much attention in recent years. Many different kinds of advanced control methods have been studied for the issue, such as robust and optimal control (Park and Lee, 1996), gain-scheduling control (Zhang et al., 2005), multivariable model predictive control (Keshavarz et al., 2010), genuine nonlinear control (Yang et al., 2012), intelligent control (Li et al., 2012), and  $L_1$  robust adaptive control (Pan et al., 2015), and have achieved much more improved control performance than conventional approaches in wide-range load-following processes.

Among above control methods,  $L_1$  robust adaptive control ( $L_1$ -RAC) is a class of new adaptive control approach. It provides some distinctive and attractive features, including

fast and robust adaptation, ensuring closed-loop stability and permitting transient analysis for both control signals and system responses (Hovakimyan and Cao, 2010; Luo and Cao, 2014). In our previous study (Pan et al., 2015), the  $L_1$  robust adaptive controller is designed as the coordinated controller of a boiler-turbine unit for rapid load demand tracking in the presence of nonlinearities, internal un-modelled dynamics, time-varying unknown disturbances and parameters, and small time delay. The closed-loop stability of the boiler-turbine control system has been verified under unknown uncertainties, along with fast-varying load demand in a wider range, showing strong robustness, fast response and large stability margins.

Although the  $L_1$ -RAC has been verified superior to many other control methods in handling nonlinearities and uncertainties, it is greatly inferior to model predictive control in dealing with time delays. As presented in the paper (Pan et al., 2015), the  $L_1$ -RAC can tolerate some extent of uncertain dead time within its time-delay margin, usually several seconds, but even a larger time-delay margin cannot satisfy long time delays like 30~100 seconds, which often exist in many boiler-turbine power-generating systems, or like much longer ones in other industrial chemical loops. The limited time-delay margin is a crucial obstacle to hinder  $L_1$ -RAC from being applied in many industrial processes. Unlike model predictive control, the  $L_1$ -RAC doesn't require model of controlled plant to design its parameters, namely it is not model-based control approach. This principle leads to its poor ability to predict future behaviour of the plant as well as time

delay. What if we incorporate a model into the  $L_1$ -RAC? To answer this question, we study a model-based robust adaptive controller (MB-RAC) which is derived from the  $L_1$ -RAC but with more focus on long time delay in this paper. Comparing to the  $L_1$ -RAC, the main change of the MB-RAC architecture is in the adaptive law which uses a dual-feedback error-generating mechanism based on a built-in plant model for adaptive compensation.

Most of the studies on boiler-turbine power systems are based on a boiler-turbine-generator nonlinear dynamic model developed by Bell and Åström (1987). Although this model is in a simplified form and thus easy for control study, it involves the key characteristics of real boiler-turbine-generator systems, including nonlinearity, coupled variables, large inertia, unmeasured internal state, non-minimum phase and unstable plant, etc., and therefore, it has often been chosen as the benchmark for coordinated control studies in literature. We have developed and verified the  $L_1$ -RAC (Pan et al., 2015a, b) approach on this Bell and Åström (B-A) model. For a subsequent study, we also use the B-A model for developing and verifying the MB-RAC approach. To handle the time-delay characteristics, a delay-augmented boiler-turbine-generator nonlinear model will be proposed based on the B-A model in this paper. The time delay will be augmented as an output delay which would not influence any inner state, but only make the outputs to be delayed.

In the rest of the paper, we propose the model-based robust adaptive control for long time delays in Section 2, and two kinds of models for the design of MB-RAC in Section 3. One model is a delay-augmented classic nonlinear boiler-turbine-generator model as the simulation model. Another one is the linearized model with time delay for controller design. For verify the robustness of the MB-RAC in the presence of long time delay, several simulation experiments are made in Section 4 and then the conclusions for the study is drawn in Section 5.

## 2. MODEL-BASED ROBUST ADAPTIVE CONTROL FOR A LONG TIME DELAY

### 2.1 Problem Formulation

The dynamics of the controlled plant can be described as following:

$$\begin{aligned}\dot{x}_D(t) &= A_D x_D(t) + B_D u(t) + f(x_D, z, t), x_D(0) = x_0, \\ \dot{z}(t) &= g(z, x_D, t), z(0) = z_0, \\ x(t) &= x_D(t - T_d) \\ y(t) &= C_D^T x(t) + D u(t)\end{aligned}\quad (1)$$

where  $x_D(t) \in R^n$  is the system state vector (immeasurable),  $x(t) \in R^n$  is the system measurable state vector with time delay  $T_d \geq 0$ ,  $u(t) \in R^m$  denotes the input ( $m \leq n$ ),  $y(t) \in R^m$  denotes the output,  $A_D \in R^{n \times n}$  is a known Hurwitz matrix,  $B_D \in R^{n \times m}$  is a known full-rank constant matrix,  $(A_D, B_D)$  is controllable,  $C_D \in R^{m \times n}$  is a known full-rank constant matrix,  $(A_D, C_D)$  is observable,  $C_D^T (sI - A_D)^{-1} B_D$  defines the desired dynamics for the closed-loop system and its zeros lie in the open left-half  $S$ -plane,  $z(t) \in R^p$  denotes the immeasurable state i.e., internal

un-modeled dynamics, and function  $f: R^n \times R^p \times R \rightarrow R^n$  and function  $g: R^n \times R^p \times R \rightarrow R^p$  denote unknown nonlinearities.

Let  $X = [x_D^T z^T]^T$ , and  $f(X, t) = f(x_D, z, t)$ . The following assumptions are essential for maintaining stability of the  $L_1$ -RAC as well as its derivative algorithms like MB-RAC:

**Assumption 1:** For any  $\delta > 0$ , there exist,  $L(\delta) > 0$  and

$B_f > 0$  such that

$$\|f(X, t) - f(\bar{X}, t)\|_{\infty} \leq L(\delta) \|X - \bar{X}\|_{\infty}, \|f(0, t)\|_{\infty} \leq B_f, \quad (2)$$

for all  $\|X\|_{\infty} \leq \delta$  and  $\|\bar{X}\|_{\infty} \leq \delta$  uniformly in  $u$  and  $t$ .

**Assumption 2:** The internal un-modeled dynamics are Bounded-Input Bounded-Output (BIBO) stable with respect to both initial conditions  $z_0$  and input  $x_D(t)$ , i.e., there exist positive  $L_z$  and  $B_z$  such that for all  $t \geq 0$

$$\|z_t\|_{L_{\infty}} \leq L_z \|x_{D,t}\|_{L_{\infty}} + B_z. \quad (3)$$

The control objective is to generate an adaptive state feedback control signal  $u(t)$  to drive the system output  $y(t)$  tracking the desired system output  $y_{des}(t)$  rapidly, while all other signals remain bounded. The desired closed-loop system is described by

$$\begin{aligned}\dot{\bar{x}}_{des}(t) &= A_D \bar{x}_{des}(t) + B_D K_g r(t), \\ \bar{x}_{des}(t) &= \bar{x}_{des}(t - T_d), \\ y_{des}(t) &= C_D^T \bar{x}_{des}(t),\end{aligned}\quad (4)$$

where  $r(t)$  is a given bounded reference input signal, and  $K_g = -(C_D^T A_D^{-1} B_D)^{-1}$ .

### 2.2 Control Algorithm

The main components of the model-based robust adaptive controller for long output delay are shown in Fig. 1 and given specifically below:

#### 1) Plant Model:

Assume that the plant with long time delay (1) can be approximately expressed by the following linear model:

$$\begin{aligned}\dot{\bar{x}}(t) &= A_m \bar{x}(t) + B_m u(t), \bar{x}(0) = x_0, \\ \bar{x}_e(t) &= \bar{x}(t - T_m), \\ \bar{y}(t) &= C_m^T \bar{x}_e(t) + D_m u(t),\end{aligned}\quad (5)$$

where the state vector  $\bar{x}(t)$  and  $\bar{x}(t - T_m)$ , input vector  $u(t)$  and output vector  $\bar{y}(t)$  has the same dimensions with their corresponding vectors in (1), and  $T_m \geq 0$  is the time delay of the model. The immeasurable state vector  $z(t)$  in (1) is not necessary here. The model (5) can be obtained by using many modeling methods like linearization from a known nonlinear math model or identification from field data of a plant. Model (5) provides an explicit expression of output delay separate from its dynamic part, which is required by the MB-RAC algorithm.

#### 2) State Predictor:



intensity, which contributes significantly to the stability of the whole control system.

### 3. MODELS USED BY DESIGN AND SIMULATION OF THE MB-RAC

#### 3.1 A Nonlinear Boiler-turbine-generator Unit Augmented with Time Delay

For verifying the performance of the MB-RAC, the nonlinear B-A model (1987) is chosen as the controlled boiler-turbine-generator plant in this study. Because the model represents many key characteristics of real boiler-turbine-generator systems, including nonlinearity, strong coupling variables, large inertia, unmeasured internal state, non-minimum phase and unstable plant etc., many different kinds of advanced control algorithms for boiler-turbine-generator systems have been tested on this model, but it does not have any time delay. In order to verify the MB-RAC algorithm, we augment it with multiple output delays without changing its inner dynamics. Based on the original third-order nonlinear dynamic equations which are described in (Bell and Åström, 1987), the delay-augmented boiler-turbine-generator nonlinear model is described in the following:

$$\begin{cases} \dot{x}_{D1}(t) = -0.0018u_2(t)x_{D1}(t)^{9/8} + 0.9u_1(t) - 0.15u_3(t) \\ \dot{x}_{D2}(t) = (0.073u_2(t) - 0.016)x_{D1}(t)^{9/8} - 0.1x_{D2}(t) \\ \dot{x}_{D3}(t) = [141u_3(t) - (1.1u_2(t) - 0.19)x_{D1}(t)] / 85 \\ x_1(t) = x_{D1}(t - T_d) \\ x_2(t) = x_{D2}(t - T_d) \\ y_1(t) = x_1(t) \\ y_2(t) = x_2(t) \\ \bar{y}_3(t) = 0.05(0.1307x_{D3}(t) + 100a_{cs}(t) + q_e(t) / 9 - 67.975) \\ x_3(t) = \bar{y}_3(t - T_d) \\ y_3(t) = x_3(t) \end{cases} \quad (13)$$

where the state  $x_{D1}$  (kg/cm<sup>2</sup>) is drum steam pressure,  $x_{D2}$  (MW) is electric power and  $x_{D3}$  (kg/cm<sup>3</sup>) is drum/riser fluid density. The output variables  $y_1$  and  $y_2$  denote the same quantities as  $x_{D1}$  and  $x_{D2}$  but delayed by  $T_d$  seconds; the output  $y_3$  (meter) is the  $T_d$  - delayed drum water level deviation  $\bar{y}_3$ , where evaporation rate  $a_{cs}$  (kg) and steam quality  $q_e$  (kg/s) are given by

$$\begin{aligned} q_e(t) &= [0.854u_2(t) - 0.147]x_{D1}(t) + 45.59u_1(t) - 2.514u_3(t) - 2.096, \\ a_{cs}(t) &= \frac{[1 - 0.001538x_{D3}(t)][0.8x_{D1}(t) - 25.6]}{x_{D3}(t)[1.0394 - 0.0012304x_{D1}(t)]}. \end{aligned} \quad (14)$$

The normalized manipulated variables are fuel flow rate  $u_1$ , control valve position of steam to the turbine  $u_2$  and feedwater flow rate  $u_3$ . All the manipulated variables have constraints in magnitude and rate as follows:

$$\begin{aligned} 0 &\leq u_i \leq 1, i = 1, 2, 3. \\ -0.007 &\leq \dot{u}_1 \leq 0.007 \\ -2 &\leq \dot{u}_2 \leq 0.002 \\ -0.005 &\leq \dot{u}_3 \leq 0.05 \end{aligned} \quad (15)$$

Table 1 lists some equilibrium working points of the B-A model and point #2 is for the nominal operating condition.

**Remark 2:** For designing the MB-RAC in the case of the delay-augmented nonlinear boiler-turbine system (13)-(15), let measurable state  $x = [x_1 \ x_2 \ x_3]^T$ , and let the internal unmeasured un-modeled dynamics state  $z = x_{D3}$ , i.e., the fluid density which satisfies **Assumption 2**. The measurable state vector  $x$  is corresponding to the output  $y = [y_1 \ y_2 \ y_3]^T$  and will be made error with the output vector of the linear model of the plant as shown in Fig. 1.

**Table 1. Equilibrium points of boiler-turbine-generator unit**

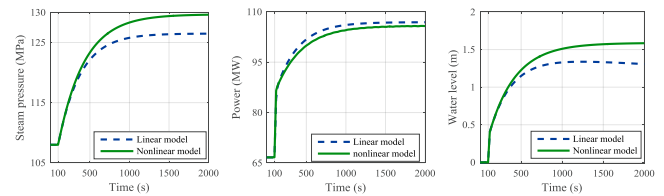
	#1	#2	#3
$x_1$	75.6	108	129.6
$x_2$	15.2	66.65	105.86
$x_3$	-0.97	0	0.64
$u_1$	0.156	0.34	0.505
$u_2$	0.483	0.69	0.828
$u_3$	0.183	0.433	0.663

#### 3.2 Linearization model with time delay

Because MB-RAC requires a mathematical model with separate expression of time delay of the controlled system, we linearize the nonlinear equation group (13)-(15) by taking Taylor's series expansion around the operating point #2 in Table 1 and then obtain the state-space model coefficients in (5) as follows:

$$\begin{aligned} A_m &= \begin{bmatrix} -0.0025 & 0 & 0 \\ 0.0694 & -0.1 & 0 \\ -0.0067 & 0 & 0 \end{bmatrix}, \quad B_m = \begin{bmatrix} 0.9 & -0.349 & -0.15 \\ 0 & 14.155 & 0 \\ 0 & -1.398 & 1.66 \end{bmatrix}, \\ C_m &= \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0.0063 & 0 & 0.0047 \end{bmatrix}, \quad D_m = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0.253 & 0.512 & -0.014 \end{bmatrix}. \end{aligned} \quad (16)$$

The LTI system ( $A_m$ ,  $B_m$ ,  $C_m$ ,  $D_m$ ) approximately represents the dynamics of the plant. The output delay  $T_m$  can be taken as the same value of  $T_d$  in (13), representing the situation of accurately modelling about time delay, or as different values from  $T_d$  for the case of inaccurate modelling.



**Fig. 3. Comparisons of the step responses from the delay-augmented B-A model and its linearized model.**

Fig. 3 shows the comparisons of the step responses from the delay-augmented nonlinear boiler-turbine-generator model and its linearized model with time delay, where the time delay  $T_m = T_d = 60s$ . Let the manipulated vector  $[u_1, u_2, u_3]$  of both models step up at 40s from the original value [0.34, 0.69, 0.433] to the final value [0.505, 0.828, 0.663], i.e., from nominal point #2 to an operating point #3 in Table 1. The result shows that the two models have similar dynamics but

with obvious difference in values, because the linear model cannot describe precisely in a large operating range of the nonlinear process.

Considering that the robust adaptive control has good ability to deal with model mismatch and nonlinearity, we will incorporate the linear model with output delay into the MB-RAC to feedback the intermediate state  $\bar{x}(t)$  which is unavailable by measurement on real plant. The error caused by model mismatch which is denoted as  $e_1(t)$  in Fig. 1 will be compensated by the adaptive law.

#### 4. SIMULATIONS AND DISCUSSION

Several simulation experiments on the delay-augmented nonlinear boiler-turbine-generator model of Eq. (13)-(15) will be made in this section to validate the MB-RAC algorithm.

The simulations focus on the robustness for load tracking of the boiler-turbine-generator system in the presence of long time delay. The simulations will compare three control performances of using: (1) the  $L_1$ -RAC, (2) the MB-RAC incorporating a linear model followed by matched time delay, and (3) the MB-RAC with linear model followed by unmatched time delay.

First we take the parameters of  $L_1$ -RAC from our previous work (Pan et al., 2015a) which has shown good control performance in a wide load tracking of the boiler-turbine-generator unit in the presences of time-varying parameter variations, input valve nonlinearity, output noise disturbances and small time delay. According to the principle of the MB-RAC, it inherits the same kind of state predictor of the  $L_1$ -RAC, so the state predictor coefficients of both controllers in (6) are given by

$$A_D = \begin{bmatrix} -0.06 & 0 & 0 \\ -0.0287 & -0.1 & 0 \\ 0.0022 & 0 & -0.005 \end{bmatrix}, \quad B_D = \begin{bmatrix} 0.9 & -0.175 & -0.15 \\ 0 & 14.155 & 0 \\ 0 & -1.398 & 1.659 \end{bmatrix},$$

$$C_D = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0.00227 \end{bmatrix}. \quad (17)$$

The filter  $F(s) = 0.1/(s+0.1)$  and the sampling time  $T=0.01$ second are chosen the same for both controllers as well.

Then following (6)-(12), we incorporate the linearized model (5) with coefficients (16) and time delay  $T_m$  into the  $L_1$ -RAC architecture and thus build the MB-RAC as shown in Fig. 2. With the dual feedbacks from the linear model and the plant, the adaptive parameter  $\hat{\sigma}(t)$  of the MB-RAC in (8) is updated at every sampling time, which is different from that generated by  $L_1$ -RAC. Figs. 4-6 show the control results of load tracking of the nonlinear boiler-turbine-generator system (13)-(15) with three different controllers and conditions.

**Case 1:** Load tracking with  $L_1$ -RAC in the presence of time delay.

As presented in our previous work (Pan et al., 2015a), the  $L_1$ -RAC can deal with about 6s time delay, so we gradually increase the value of the output delay  $T_d$  in model (13) till  $T_d=10s$  when it led to instability of the control system. Seen from Fig. 4, the system setpoints step up from the initial state at nominal point #2 to operating point #3 at  $t=40s$ . In the load tracking process, the controlled variable, steam pressure and power, have slow damping meanwhile the manipulated control variables vary severely. Eventually  $L_1$ -RAC cannot keep the stability of the nonlinear boiler-turbine-generator system. The control results denote that the  $L_1$ -RAC has very limited time-delay margin thus it is hard to handle long time delays which power plants always have.

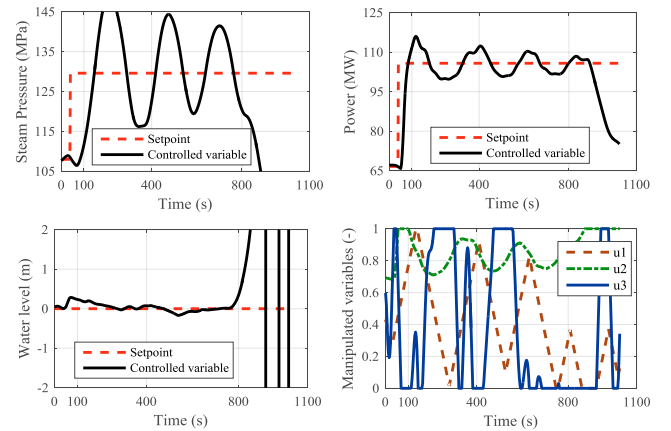


Fig. 4. Control result of the  $L_1$ -RAC ( $T_d=10s$ ).

**Case 2:** Load tracking with MB-RAC using matched long time delay.

For testing the effect of MB-RAC, we extend the time delay to 60s in this case. It uses the linear model presented in (5) with coefficients (16) and matched time delay  $T_m=T_d=60s$ . In the same load-tracking process as in Case 1, the control result is pretty good as shown in Fig. 5. Except for water level and water flow rate which have a little fluctuation, the other controlled variables and manipulated variables converge to the steady state quickly and steadily. The results denote that MB-RAC has good robustness to mismatch between the linear model and the controlled plant.

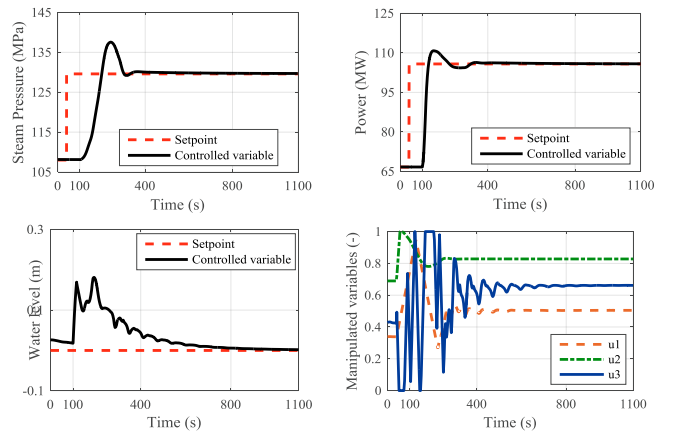




Fig. 5. Control result of the MB-RAC (using linear model with matched time delay,  $T_m=T_d=60s$ ).

**Case 3:** Load tracking with MB-RAC using unmatched long time delay.

In this case, the robustness of MB-RAC is tested further, i.e., let  $T_m=65s$ ,  $T_d=60s$ . This is because in field test the measurement delay always cannot be avoided and then a longer delay will be obtained in modeling. Seen from Fig. 6, the unmatched output delay in MB-RAC results in a little more fluctuation on all variables, but the variables still converges to steady state quickly and the system is far from instability. The results denote that MB-RAC has strong robustness to its inner model mismatch on both dynamics and time delays.

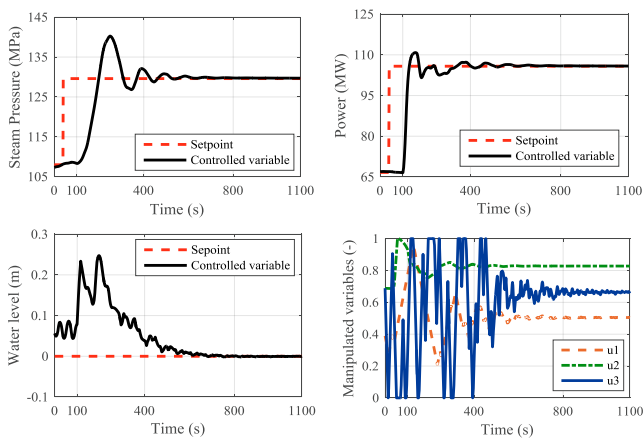


Fig. 6. Control result of the MB-RAC (using linear model with unmatched time delay,  $T_m=65s$ ,  $T_d=60s$ ).

**Remark 3:** Incorporating the internal model theory into robust adaptive controller, the resulting control performance of the MB-RAC is greatly improved. It fits in not only with nonlinear plants under uncertain conditions but also with plants in the presence of long time delays. Seen from the simulation results, the MB-RAC has strong robustness to the inner model mismatch, and it is easy to design and implement for industrial processes.

## 5. CONCLUSIONS

Most of the existing control methods for the boiler-turbine power-generating systems cannot ensure good performance as some uncertainties arise. The  $L_1$  robust adaptive control has been proven to be effective for a wide-range load-tracking of the nonlinear B-A model in the presence of uncertain conditions. But its limited time-delay margin cannot deal with plants in the presence of long time delays which commonly exist in many industrial processes. In order to improve the  $L_1$ -RAC specifically in term of time-delay tolerance capability, this paper introduces the internal model theory into the robust adaptive algorithm, developing a novel model-based robust adaptive control. It not only inherits arbitrarily close tracking performance and fast, robust adaptation of the  $L_1$ -RAC, but also has good ability to deal

with long time delay in control processes. Moreover, it shows strong robustness to inner model mismatches on both the dynamics and the time delays, so it is easy to design and maintain in operation. Because it has multi-abilities to solve the problems in the operations of boiler-turbine-generator systems, MB-RAC may become a promising control approach for power plants in the near future.

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