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# Optimization-based reactive power control in HVDC-connected wind power plants

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## Abstract

One application of high-voltage dc (HVdc) systems is the connection of remotely located offshore wind power plants (WPPs). In these systems, the offshore WPP grid and the synchronous main grid operate in decoupled mode, and the onshore HVdc converter fulfills the grid code requirements of the main grid. Thus, the offshore grid can be operated independently during normal conditions by the offshore HVdc converter and the connected wind turbines. In general, it is well known that optimized reactive power allocation might lower the component loading and power losses. This paper aims to propose and assess a reactive power allocation optimization within HVdc-connected WPPs. For these systems, the offshore converter operates the adjoining grid by imposing frequency and voltage. The reference voltage magnitude is used as additional control variable for the optimization algorithm. The loss function incorporates both the collection grid and the

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converter losses. The use of the proposed strategy results in an effective reduction of losses compared to conventional reactive power dispatch strategies alongside with improvements of the voltage profile. A case study for a 500 MW-sized WPP demonstrates an additional annual energy production of 6819 MWh or an economical benefit of 886 k€yr<sup>-1</sup> when using the proposed strategy.

*Keywords:* Reactive power, Optimal power flow (OPF), High voltage direct current (HVdc), Wind power

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## 1. Introduction

The use of wind energy at offshore locations is growing, especially in European waters. By the end of 2015 the cumulative grid connected offshore wind power installations raised to more than 11 GW, on top of an additional capacity of 63.5 GW in the planning phase [1]. Currently, wind turbines (WTs) are variable-speed machines using partly or fully-scaled voltage-source converter (VSC) to interface with the electrical grid [2]. These converters allow to control the active and reactive power exchange at their ac terminals independently within specific capability limits [3].

Most offshore wind power plants (WPPs) require a dedicated grid connection to the onshore grid. Depending on the project characteristics, namely the distance to shore and the total power rating, either an ac or dc-based technology is selected to connect the generation units to the transmission grid [4, 5].

In the case that the offshore WPP is connected via a high-voltage dc (HVdc) link, the collection grid is usually operated by the offshore high-

17 voltage dc voltage–source converter (VSC–HVdc) in islanded mode whereas  
18 the VSC–HVdc provides reference for both voltage and frequency. The on-  
19 shore converter fulfills grid code (GC) requirements imposed by the trans-  
20 mission grid operator (TSO) of the main grid [4]. Amongst others, GCs  
21 define rules for the connection of generation units to a power system, such  
22 as operation characteristics, active and reactive power control, frequency re-  
23 sponse, fault behavior and ancillary services [6]. Besides the necessity of GC  
24 compliance, offshore wind power is exposed to the market competition with  
25 other energy sources. Therefore, it remains subject to significant pressures  
26 to improve its cost of energy (COE) and lower the associated risks [7]. One  
27 option to lower the COE is the increase of the annual energy production  
28 (AEP). This might be solved, among others, by e.g. alternative topologies  
29 [8, 9, 10, 11], WPP layout optimization [12] and/or concepts to lower losses  
30 due to wake effects [13]. Another option, which is investigated in this pa-  
31 per, is the implementation of appropriate reactive power control operation  
32 strategies to reduce steady–state losses in the collection grid and the power  
33 converters with the objective to boost the AEP.

34 System operators use optimization algorithms to minimize electrical losses  
35 by tuning set–points of on–load tap changer (OLTC) of transformers or other  
36 electrical equipment which can control voltage or reactive power (e.g. WPPs,  
37 static compensator (STATCOM) capable assets and reactive power compen-  
38 sators) [14, 15, 16, 17, 18]. The same approach can be applied to an internal  
39 WPP grid which has been studied for ac–connected WPPs in [19, 20, 21, 22]  
40 and dc–connected WPPs in [23, 24]. Based on the particle swarm opti-  
41 mization (PSO) algorithm of [25], the operation principle was investigated

42 for doubly fed induction generator (DFIG)–based WPPs in [20]. In [21] a  
43 feasible solution search PSO algorithm was applied to the reactive power  
44 allocation problem of a DFIG–based WPP. Different control principles are  
45 analyzed concluding that a higher loss reduction is achieved for lower WPP  
46 power outputs. In terms of practicability for an online optimal reactive power  
47 allocation, the authors of [26, 27] propose optimal power flow (OPF) con-  
48 trollers based on mean–variance mapping optimization (MVMO) aiming to  
49 minimize losses while complying with the GC at the point of common cou-  
50 pling (PCC). In [28] the suggested OPF controller additionally considers to  
51 minimize the switching actions of the OLTC and uses a neural–network–  
52 theory–based wind speed prediction. In [22], the authors discuss a complete  
53 loss calculation including generator and converter losses for a DFIG–based  
54 WPP to solve the optimal reactive power allocation problem. The analysis  
55 made in [29] provides a fruitful insight of the necessity to include the WT  
56 converter losses in the problem formulation of these systems.

57 The authors of this article challenged the optimal reactive power alloca-  
58 tion problem in HVdc–connected WPPs for the first time in [23]. Here, an  
59 optimization–based algorithm is used to perform the reactive power dispatch  
60 to the WTs comparable to similar algorithms proposed for ac–connected  
61 WPPs but under consideration of converter losses and the reactive power  
62 sharing between the WTs and the VSC–HVdc. Specifically, the influence  
63 of wake effects on the total active and reactive power production in the off-  
64 shore grid is analyzed. Nevertheless, the reference voltage imposed by the  
65 VSC–HVdc is continuously contained to 1 p.u.. Besides this publication, the  
66 general characteristics regarding reactive power control in HVdc–connected

67 WPPs are briefly commented in the technical brochures of *CIGRE* [30, 31].  
68 The main difference to high-voltage ac (HVac)-connected WPPs is that the  
69 reactive power requirement demanded by the main grid does not constrain  
70 the reactive power allocation within the offshore grid because of the earlier  
71 mentioned decoupled operation. Additionally, a change of the reference volt-  
72 age in the offshore grid is possible by means of the VSC-HVdc control. This  
73 study extends the methodology for HVdc-connected WPPs introduced in  
74 [23] by the same authors and proposes the inclusion of the reference voltage  
75 as a control variable in the optimization-based control algorithm.

76 The main aim of this paper is to propose a reactive power control strategy  
77 to optimize the operation of HVdc-connected WPPs in terms of losses. The  
78 optimization determines reactive power set-points for the WTs and the PCC  
79 reference voltage set-point imposed by the VSC-HVdc based on a combined  
80 converter losses and load flow model. A case study is defined to analyze  
81 the performance of the proposed strategy and variations thereof against con-  
82 ventional control concepts. A 500 MW-sized WPP which employs full-scale  
83 power converter-based wind turbines (type 4) [FSC-WTs] is used for this  
84 analysis. Six control principles are evaluated: two conventional and four  
85 optimization-based strategies, respectively. The result shows an improved  
86 performance specifically for the variable optimization-based strategies for  
87 both the total power losses and the voltage profile. The incorporation of the  
88 reference voltage as control variable inherently reduces the power losses in  
89 the system without harming the overall operation.

90 The remainder of this paper is organized as follows: Section II describes  
91 the methodology to analyze reactive power control in HVdc-connected WPPs

92 and proposes suitable optimization-based strategies. Section III defines a  
 93 case study for a reference WPP. The results and discussion are outlined in  
 94 Section IV. Finally, Section V provides the conclusions and recommendations.

## 95 **2. Methodology**

96 A possible HVdc-connected WPP system is shown in Figure 1 [30]. The  
 97 full-scale converter (FSC) of the WTs comprises a machine-side converter  
 98 (MSC) in back-to-back (B2B) arrangement with a grid-side converter (GSC)  
 99 system. The GSC connects to the low-voltage (LV)-side of the WT trans-  
 100 former through a coupling inductance and a harmonic filter. A number of  
 101 WTs is interconnected by medium-voltage (MV) submarine cables to form a  
 102 string and interface the high-voltage ac offshore substation (HVac-OS). Here,  
 103 high-voltage (HV) transformer(s) step up the voltage from MV to HV. The  
 104 HVac-OS is linked to the high-voltage dc offshore substation (HVdc-OS)  
 105 by HVac submarine cable(s). The HVdc-OS consists of the HVdc trans-  
 106 former(s), possible harmonic filter(s) and the offshore VSC-HVdc. The off-  
 107 shore VSC-HVdc station links to any dc-capable interface via submarine  
 108 dc cables, in the usual execution a point-to-point connection to an onshore  
 109 VSC-HVdc to connect to the main ac grid.

### 110 *2.1. Calculation of relevant losses*

111 In general, there are multiple electrical losses occurring in the operation of  
 112 generators, converters, filters, transformers and cables. For the steady-state  
 113 power flow analysis, lines, filters and transformers are modeled as lumped  
 114 circuits ( $\pi$ -models) [32]. In a  $\pi$ -model, the series admittance between two  
 115 nodes 1 and 2 is defined as:

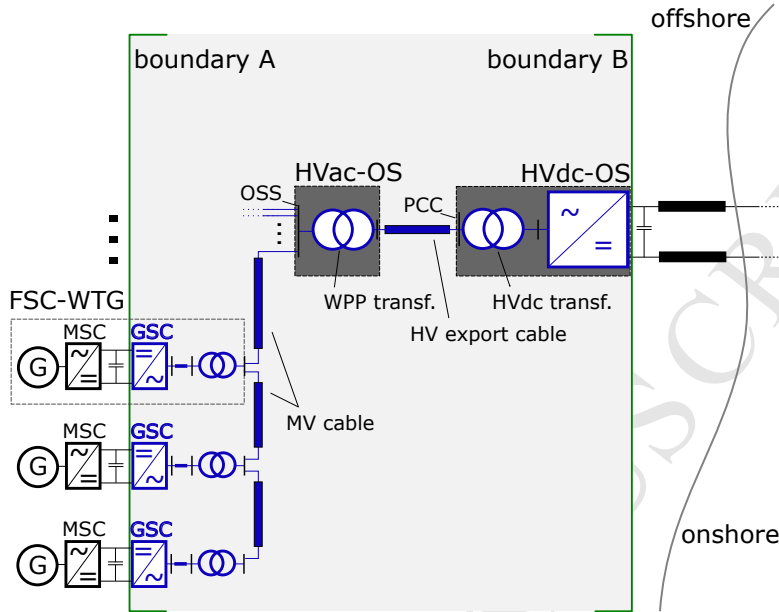


Figure 1: Typical arrangement of an HVdc-connected offshore WPP and system boundaries for loss assessment.

$$\underline{y}_{12} = g_{12} + j \cdot b_{12} = \frac{r_{12}}{r_{12}^2 + x_{12}^2} - j \frac{x_{12}}{r_{12}^2 + x_{12}^2} \quad (1)$$

116 where  $g_{12}$  and  $b_{12}$  are the series conductance and susceptance between the  
 117 nodes 1 and 2, respectively, and  $r_{12}$  and  $x_{12}$  represent the series resistance  
 118 and reactance, respectively.

The shunt admittance is calculated as:

$$\underline{y}_1^{sh} = \underline{y}_2^{sh} = g^{sh} + j \cdot b^{sh} \quad (2)$$

When considering power cables and lines the shunt conductance is very small ( $g^{sh} \approx 0$ ) and can be neglected. Values for the series resistance  $r_{12}$ , series reactance  $x_{12}$  and shunt susceptance  $b^{sh}$  are chosen according to manufacturer data. For transformers, the series resistance  $r_{12}$  models the copper losses



(load losses) in the windings having the reactance  $x_{12}$ . The iron/core losses (no-load) due the magnetizing current can be represented by a shunt element. The active power imbalance or loss  $\Delta p$  can be calculated using (3) and the reactive power imbalance  $\Delta q$  composed of the reactive power generation by the shunt susceptance and reactive power loss is described in (4):

$$\Delta p = g_{12} \cdot (u_1^2 + u_2^2 - 2u_1u_2 \cos \theta_{12}) \quad (3)$$

$$\Delta q = -b^{sh} \cdot (u_1^2 + u_2^2) - b_{12} \cdot (u_1^2 + u_2^2 - 2u_1u_2 \cos \theta_{12}) \quad (4)$$

119 where  $u_1$  and  $u_2$  are the voltages of node 1 and 2, respectively, and  $\theta_{12} =$   
120  $\theta_1 - \theta_2$  is the phase angle difference between the two nodes.

121 The compilation of losses is limited to the boundaries of the offshore  
122 grid as shown in Figure 1: boundary A is the interface between dc link  
123 of the GSCs and boundary B is the dc terminal the offshore VSC–HVdc.  
124 These boundaries are set following that the reactive power control at the ac  
125 terminal of a VSC is independent from the dc–side [3]. Therefore, the control  
126 of reactive power at the GSC does not cause additional currents (or losses) in  
127 the dc link, the MSC or even the generator. This is also valid for the offshore  
128 VSC–HVdc with respect to the HVdc interface. However, the injection of  
129 active and reactive power,  $P_c$  and  $Q_c$ , respectively, influences the converter  
130 current  $I_c$  according to (5):

$$I_c = \frac{\sqrt{P_c^2 + Q_c^2}}{\sqrt{3} \cdot U_{LL,rms}} \quad (5)$$

131 The switching and conduction losses  $P_{conv}^{loss}$  of a VSC might be approx-  
132 imated by a quadratic polynomial function in dependence of the converter  
133 current  $I_c$ , considering three parts [33]: constant, linear and quadratic losses.

$$P_{\text{conv}}^{\text{loss}} = \left[ a + b \cdot \frac{I_c}{I_r} + c \cdot \left( \frac{I_c}{I_r} \right)^2 \right] \cdot S_n \quad (6)$$

134 where  $I_r$  is the rated converter current,  $S_n$  represents the nominal apparent  
135 power.

136 Typical loss data for a system rated to  $U_{\text{dc}} = \pm 300$  kV,  $S_n = 600$  MVA  
137 based on a two-level VSC-HVdc (HVdc-2L) can be found in [34]. For a mod-  
138 ular multi-level VSC-HVdc (HVdc-MMC) the current-dependent losses in  
139 the converter valves are approximately halved compared to a HVdc-2L [35].  
140 Figure 2 shows the relative power losses of the considered power convert-  
141 ers deploying (6) with the parameter values from Table 1. The effect of  
142 the absolute loss increase due to a reactive power exchange in comparison  
143 to exclusively active power injection is represented in Figure 3. The addi-  
144 tional converter losses in the HVdc-MMC are up to 0.9 MW when operated  
145 at  $p = 0$  p.u. and  $q = 1$  p.u.. For  $q = 1$  p.u., an equally scaled GSC system  
146 causes a value of 1 MW additional losses at full power and up to 2.8 MW  
147 additional losses for  $p = 0$  p.u..

Table 1: Typical converter loss parameter values used in [33, 34, 35].

System	a	b	c
GSC	0.0005	0.0097	0.0048
HVdc-2L	0.0083	0.0030	0.0032
HVdc-MMC	0.0042	0.0015	0.0016

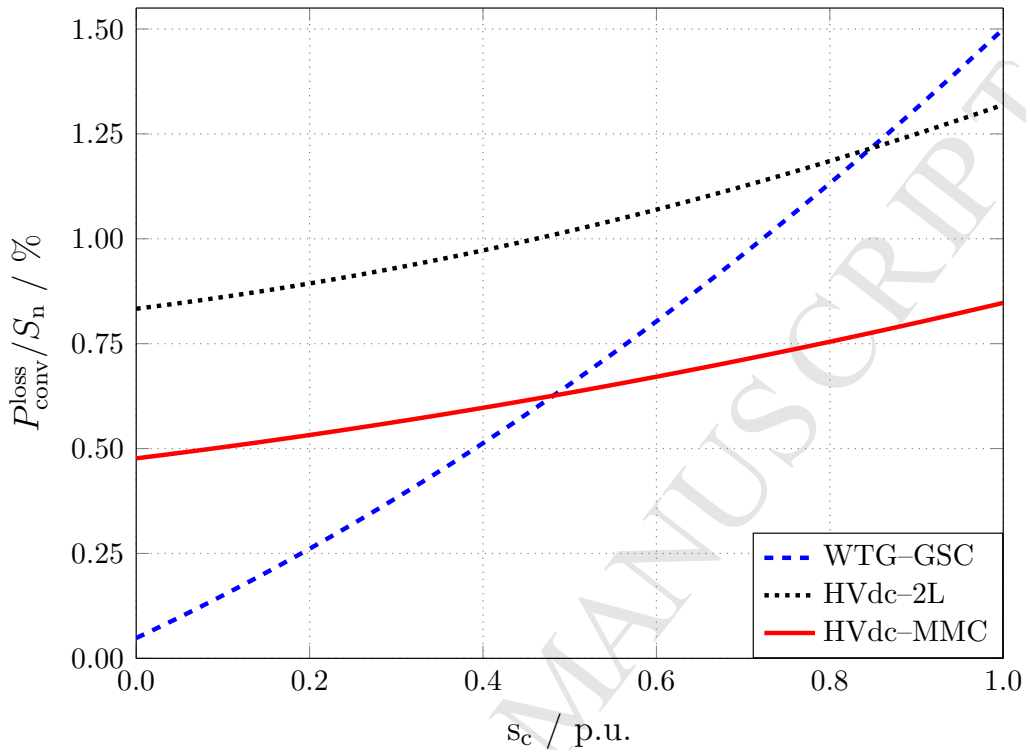


Figure 2: Relative losses of VSC systems based on their technology and power output.

## 148 2.2. Reactive power allocation strategies

149 The reactive power allocation strategies considered in this paper focus  
 150 on the normal operation of the HVdc-connected WPP. During system dis-  
 151 turbances (e.g. under or over-voltage events) each converter would oper-  
 152 ate based on a predefined control procedure usually according to the GC.  
 153 Nonetheless, local reactive power limitations due to the availability and PQ  
 154 capability curve of the WT have to be respected.

155 In principle, two conventional strategies might emerge to control reactive  
 156 power in an HVdc-connected WPP when the control variable are limited to  
 157 be the reactive power set-points:

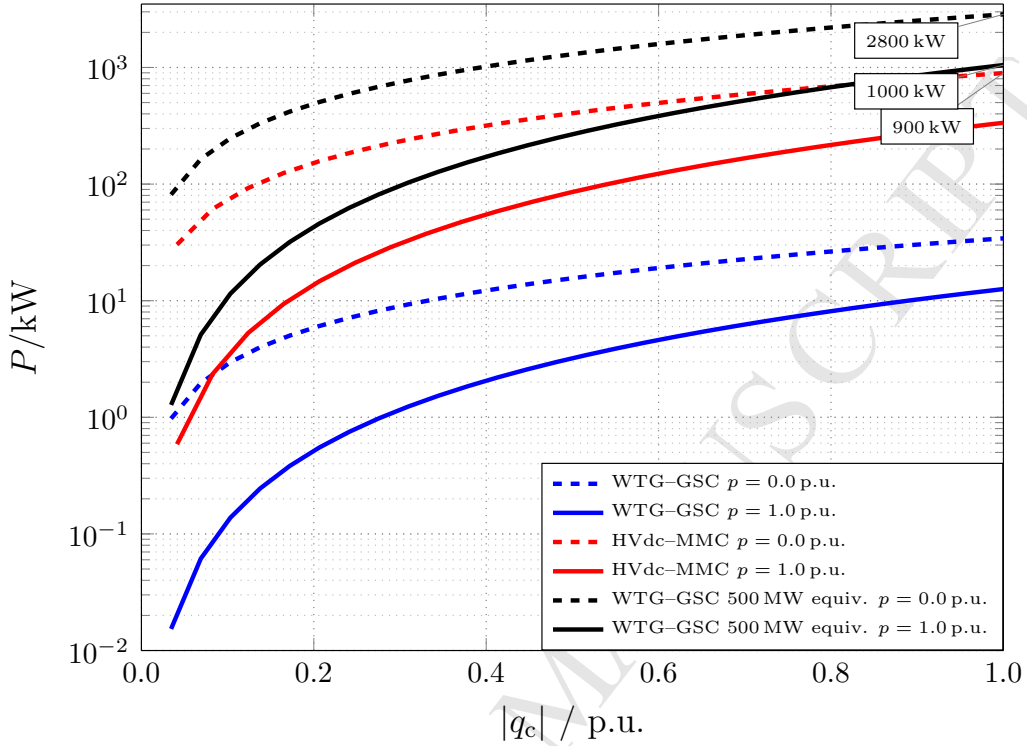


Figure 3: Absolute increase of losses caused by the reactive power injection of VSCs. GSC rating:  $S_n = 6.67$  MVA,  $\cos \varphi = 0.9$ ,  $u_{ac} = 0.9$  kV; HVdc-MMC  $S_n = 555.6$  MVA,  $\cos \varphi = 0.9$ ,  $u_{ac} = 333$  kV ( $u_{dc} = \pm 320$  kV, modulation index:  $m = 0.85$ ); GSC 500 MW equivalent to compare with the VSC-HVdc.

- 158 1. Strategy 1 (S1): Each GSC operates locally with zero reactive power  
 159 injection, thus  $Q_i = 0$  Mvar. This is equal to a unity power factor (PF)  
 160 operation of the GSCs for  $P_i \neq 0$  MW.
- 161 2. Strategy 2 (S2): The VSC-HVdc aims to operate with zero reactive  
 162 power injection ( $Q_{PCC} = 0$  Mvar) by adjusting remotely the reactive  
 163 power set-points  $Q_i$  of the WTs. The VSC-HVdc is operated at a  
 164 unity PF for  $P_{PCC} \neq 0$  MW.

165 Furthermore, the optimization-based strategy as presented in [23] is consid-  
 166 ered:

167 3. Strategy 3 (S3): An optimization algorithm aims to maximize the  
 168 power output of the system and calculates reactive power set-points  
 169 for the GSCs according to the actual operating point of the complete  
 170 system.

171 The strategies S1 to S3 are studied with a fixed PCC voltage reference of  
 172  $\underline{u}_{PCC} = 1$  p.u. which is continuously controlled by the VSC-HVdc. Finally,  
 173 the three initial strategies are extended by the varying voltage reference and  
 174 introduced as variable strategies:

175 4. Variable strategy 1 (S1var): Optimization-based with the PCC voltage  
 176 magnitude  $u_{PCC}$  as control variable whereas the WT inject  $Q_i = 0$  Mvar  
 177 ( $i \in N_{WT}$ ).

178 5. Variable strategy 2 (S2var): Optimization-based with the PCC voltage  
 179 magnitude  $u_{PCC}$  as control variable and a unique set-point for  $Q_i$  of  
 180 the WTs.

181 6. Variable strategy 3 (S3var): Optimization-based similar to S3 adjust-  
 182 ing the individual reactive power set-points for the GSCs as well as the  
 183 PCC voltage magnitude  $u_{PCC}$  controlled by the offshore VSC-HVdc.

184 Strategy S1var to S3var allow a variable PCC voltage set-point within  
 185 the continuous voltage operation boundaries. For all strategies, the VSC-  
 186 HVdc injects or absorbs the active and reactive power to fulfill the power  
 187 imbalance equations (acting as a reference bus).

188 Regarding data exchange requirements, the implementation of S1 does  
 189 not necessarily use the communication system between the local WT control

190 and the central WPP control. In contrast, S2 deploys a closed-loop control  
 191 to adjust the set-points  $Q_i$  controlling the measured  $Q_{PCC}$  to the reference of  
 192 0 Mvar. The reactive power set-point for S1, S2, S1var and S2var is the same  
 193 for all WTs. The strategies S3, S1var, S2var and S3var necessarily require a  
 194 communication system as either inputs (active power measurements, opera-  
 195 tion status of WTs) and outputs (reactive power set-points,  $u_{PCC}$  set-point  
 196 in case of the variable strategies) have to be transferred between WT control  
 197 and central WPP control.

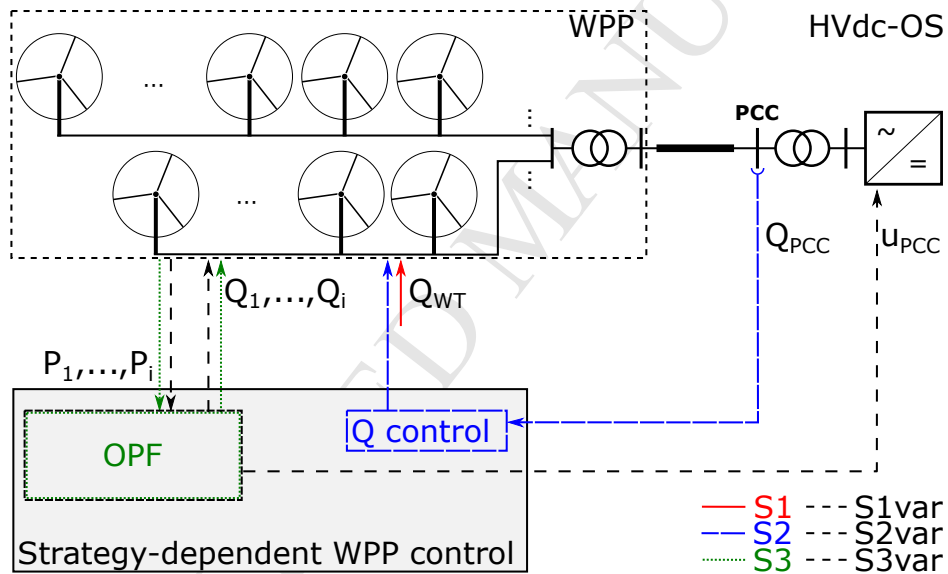


Figure 4: Schematic of control concepts and communication paths for each strategy.

198 Figure 4 sketches the communication and measurement needs for the  
 199 presented strategies. To sum up, the six strategies and their characteristics  
 200 are listed in Table 2.

Table 2: Overview of considered reactive power allocation strategies.

	S1	S2	S3	S1var	S2var	S3var
Objective:	unity PF WTs	unity PF VSC- HVdc	min $P_{\text{total}}^{\text{loss}}$			
Communication:	local	remote				
$Q_i$ set-points:	0 Mvar	WPP control	OPF	0 Mvar	OPF	OPF
$Q_i$ distribution:	uniform	uniform	variable	uniform	uniform	variable
$Q_{\text{PCC}}$ set-point: <sup>1</sup>	power flow	0 Mvar	power flow			
$u_{\text{PCC}}$ set-point:	fixed			variable		
Average execu- tion time OPF: <sup>2</sup>	n/a	n/a	188.8 s	1.9 s	9.8 s	243.9 s

### 201 2.3. Formulation of the optimization problem

202 The total active power losses  $P_{\text{total}}^{\text{loss}}$  in the system are calculated as:

$$P_{\text{total}}^{\text{loss}} = \sum_{\forall i} P_{\text{GSC}_i}^{\text{loss}} + P_{\text{grid}}^{\text{loss}} + P_{\text{VSC-HVdc}}^{\text{loss}}. \quad (7)$$

203 where  $P_{\text{grid}}^{\text{loss}}$  are the total losses in the system including collection grid, export  
 204 cable(s) and transformer(s),  $P_{\text{GSC}_i}^{\text{loss}}$  reflects the GSC losses and  $P_{\text{VSC-HVdc}}^{\text{loss}}$   
 205 represents the losses of the HVdc converter.

<sup>1</sup>The reactive power at the PCC is determined by the power flow in the offshore grid.

<sup>2</sup>Data is given for the case study performed in this paper.

206 The design vector  $\mathbf{x}$  accommodates the voltage set-point  $u_{\text{PCC}}$  and the  
 207 reactive power set-points  $q_i$  of the GSCs:

$$\mathbf{x} = [u_{\text{PCC}}, q_1, q_2, \dots, q_i]^T \quad i \in \mathbf{N}_{\text{WT}} \quad (8)$$

where  $\mathbf{N}_{\text{WT}}$  is a vector of all WT elements. The optimization problem is stated as follows:

$$\text{Minimize } f(\mathbf{x}) = P_{\text{total}}^{\text{loss}}(\mathbf{x}) \quad (9)$$

*s.t.* :

$$\text{Power flow equations} \quad (10)$$

$$\mathbf{u}_{k,\min} \leq \mathbf{u}_k(\mathbf{x}) \leq \mathbf{u}_{k,\max}, \quad k \in \mathbf{N}_{\text{bus}} \quad (11)$$

$$|\mathbf{i}_l(\mathbf{x})| \leq \mathbf{i}_{l,\max}, \quad l \in \mathbf{N}_{\text{branch}} \quad (12)$$

$$q_{\text{PCC},\min} \leq q_{\text{PCC}}(\mathbf{x}) \leq q_{\text{PCC},\max} \quad (13)$$

$$u_{\text{PCC}} \in [u_{\text{PCC},\min}, u_{\text{PCC},\max}] \quad (14)$$

$$\mathbf{q}_i \in [\mathbf{q}_{i,\min}, \mathbf{q}_{i,\max}], \quad i \in \mathbf{N}_{\text{WT}} \quad (15)$$

208 where  $\mathbf{N}_{\text{bus}}$  and  $\mathbf{N}_{\text{branch}}$  are vectors of all buses (except PCC bus) and  
 209 branches, respectively. The voltages  $\mathbf{u}_k(\mathbf{x})$  at the buses  $\mathbf{N}_{\text{bus}}$  are limited  
 210 to the minimum and maximum voltages  $\mathbf{u}_{k,\min}$  and  $\mathbf{u}_{k,\max}$  being a devi-  
 211 ation of  $\pm 10\%$  of the nominal voltage. The current in a branch  $\mathbf{i}_l(\mathbf{x})$   
 212 represents the highest absolute value of the current at both ends of the  
 213 branch. It is limited to the corresponding rating  $\mathbf{i}_{l,\max}$ . The reactive power  
 214 limitations at the PCC,  $q_{\text{PCC},\min}$  and  $q_{\text{PCC},\max}$ , and for the WTs,  $\mathbf{q}_{i,\min}$   
 215 and  $\mathbf{q}_{i,\max}$ , correspond to a PF of 0.9 at full power. The different PCC



216 voltage constraints between the optimization-based strategies (S3, S1var,  
 217 S2var and S3var) are reflected by  $u_{\text{PCC},\min} = u_{\text{PCC},\max} = 1.0$  p.u. for S3 and  
 218  $u_{\text{PCC},\min} = 0.9$  p.u. and  $u_{\text{PCC},\max} = 1.1$  p.u. for S1var to S3var in (14). Strat-  
 219 egy S1var is further restricted by  $q_i = q_{i,\min} = q_{i,\max} = 0$  p.u. ( $i \in \mathbf{N}_{\text{WT}}$ )  
 220 in (15). For strategy S2var the reactive power at the PCC is restricted  
 221 to  $q_{\text{PCC}} = q_{\text{PCC},\min} = q_{\text{PCC},\max} = 0$  p.u. (13) and additionally  $q_i = q_j$   
 222 ( $i, j \in \mathbf{N}_{\text{WT}}$ ) meaning that all WTs receive an equal reactive power set-  
 223 point.

#### 224 2.4. Implementation of the optimization-based strategies

225 The implementation of the optimization-based strategies is made by the  
 226 combination of the Matlab-based power flow solver package Matpower [36]  
 227 and the fmincon function of the Matlab Optimization Toolbox. For the  
 228 purpose of this study, lines and transformers are sufficiently modeled as a  
 229  $\pi$ -section model [37]. In Matpower, every GSC<sub>*i*</sub> is defined as static gener-  
 230 ator G<sub>*i*</sub> connected to a load bus (PQ bus), injecting active power  $P_i$  and  
 231 reactive power  $Q_i$  ( $i \in \mathbf{N}_{\text{WT}}$ ). The VSC-HVdc, which sets the PCC voltage  
 232 reference, is introduced as the reference bus (slack bus). The integration of  
 233 the converter losses is made sequentially: the GSC losses caused by  $Q_i$  are  
 234 considered as real power demand at the corresponding WT load bus whereas  
 235 the VSC-HVdc and HVdc transformer losses are calculated by (6) after each  
 236 load flow computation. The fmincon function uses the interior-point al-  
 237 gorithm. The optimization is deterministic as the interior-point algorithm  
 238 reaches local minimums. Nevertheless, the solver runs from multiple starting  
 239 points to increase the number of solutions. Furthermore, the total execution  
 240 time is limited. The best solution is selected and verified through load flow

241 calculation afterwards.

## 242 *2.5. Conceptual implementation in the industrial application*

243 A feasible implementation of the optimization-based strategies might con-  
244 sider a variable refresh rate between 5 min to 10 min. The optimization algo-  
245 rithm itself might have a maximum execution time (here set to 300 s). The  
246 average execution times recored for the case study in this paper are listed  
247 in the last row of Table 2. Obviously, the number of the control variables  
248 increases the calculation time. For S1var and S2var average calculation times  
249 below 10 s are reached (simulations are run on a 3.5 GHz-system with 16 GB  
250 RAM). New set-points might be sent as soon as the optimization algorithm  
251 ends. Further time requirements are: the communication times for the active  
252 power measurements of the WTs and the reference voltage/reactive power  
253 set-points, respectively, and the settling time after receiving the new set-  
254 points. The communication delays are negligible on the time frame of the  
255 proposed controller as modern communication systems in offshore WPPs con-  
256 sider refresh rates of a few hundreds of ms [38]. The settling times might be  
257 established as required for normal reactive power set-point changes in WPPs  
258 (e.g. 30 sec [39]). Fast voltage support to counteract voltage dips acts inde-  
259 pendently from this and supersedes the previous reactive power set-points  
260 during activation. For the variable strategies, the reference voltage might be  
261 changed first and afterwards the reactive power injections by the WTs. Real-  
262 time implementation might be improved by either short-term power or wind  
263 forecast to offset the time delay [27] or offline calculation of the optimization  
264 algorithm.

### 265 3. Case study

266 The analysis made in this paper aims to draw conclusions relied upon  
267 realistic data. Therefore, the WPP characteristics were derived from the  
268 French 498 MW Fécamp project [40, 41]. This WPP is planned with 83  
269 individual FSC-WTs with a nameplate capacity of 6 MW each. For the sake  
270 of simplicity, it is assumed that each GSC can provide the equivalent reactive  
271 power of a PF of  $\cos \varphi = \pm 0.9$  at full power.

272 The graphical data offered in [40] allows to estimate individual cable  
273 lengths and to define the distribution of the turbines as well as how they are  
274 interconnected (visualized in Figure 5). Further relevant reference data, in-  
275 cluding component parameters and voltage levels, are provided in Table A.4  
276 in the Appendix. The array cable lengths were calculated according to the  
277 distance between the turbines and an additional offset of  $l = 100$  m to incor-  
278 porate the cable routing from the sea bed to the transition piece of the WTs.  
279 Table A.5 gives data for the cross-linked polyethylene (XLPE) submarine  
280 cables considered in this study.

281 Contrary to the reference project, the transmission grid connection is  
282 adapted to an HVdc connection for the purpose of this paper. Loss data  
283 for the offshore VSC-HVdc are calculated according to (6) and Table 1. An  
284 HVdc-MMC system is assumed as it presents the state-of-the-art solution  
285 in this application [30].

286 To compute an approximate value of the total energy losses of the WPP,  
287 the annual wind speed distribution of the specific site is required. In gen-  
288 eral, a Weibull probability distribution approximates the distribution of wind  
289 speed for WPP studies. The parameters for the case study are the mean wind

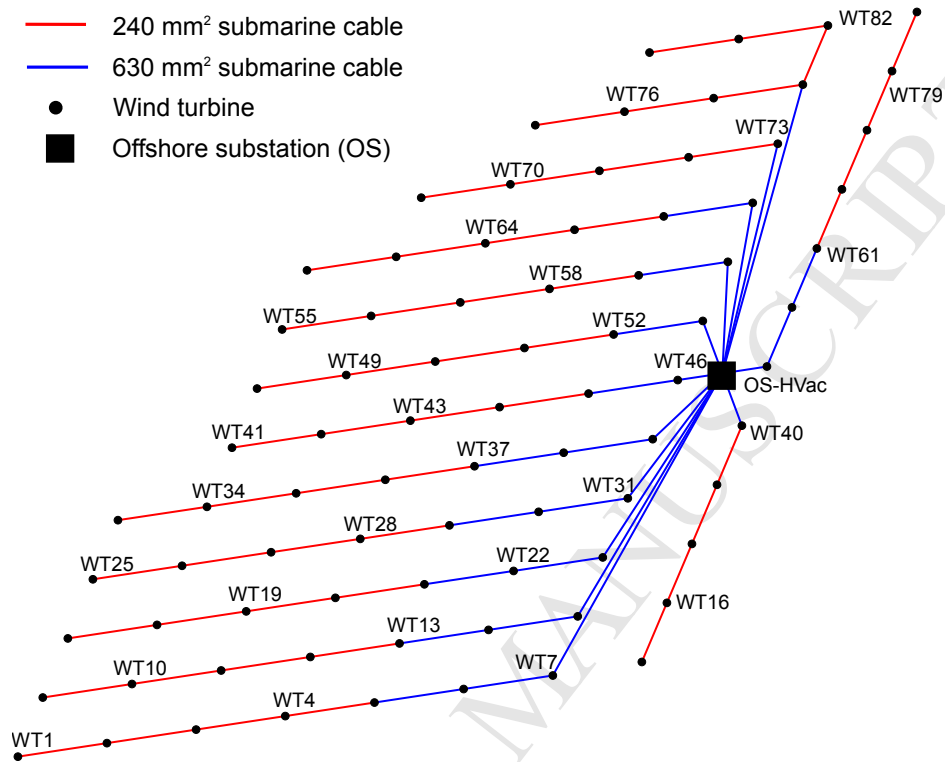


Figure 5: Layout of the 498 MW Fécamp reference WPP.

290 speed of  $8.8 \text{ m s}^{-1}$  [41] and a commonly used shape parameter for offshore  
 291 locations of 2.2 [7]. The consideration of outages of WTs or the HVdc sys-  
 292 tem due to maintenance or failure and wake effects is beyond the scope of  
 293 this study. Thus, the wind speed and active power injection are assumed to  
 294 be equal for each WT. In order to estimate the monetary value of the total  
 295 energy losses, the French offshore feed-in tariff of  $130 \text{ € MWh}^{-1}$  is considered  
 296 [42].

## 297 4. Results

298 The analysis was performed for the six strategies and active power values  
 299 ranging from zero to full power ( $p = 0.0$  p.u. to  $1.0$  p.u.). The first case, S1, is  
 300 taken as a reference to evaluate the other strategies. The relative loss value  
 301 shows the increase or reduction of losses for a strategy  $S_n$  in comparison to  
 302 the strategy S1 and is calculated according to:

$$P_{\text{rel}}^{\text{loss}} = \frac{P_{S_n}^{\text{loss}}}{P_{S_1}^{\text{loss}}} \cdot 100 \% \quad (16)$$

303 where  $n \in \{1, 2, 3, 1\text{var}, 2\text{var}, 3\text{var}\}$  is used to compare the strategies to  
 304 S1. Figure 6 depicts the total relative losses for all strategies according  
 305 to (16). The results demonstrate that S2 causes higher losses than S1 for  
 306  $0.0 < p < 0.6$  p.u. and less losses for  $p > 0.6$  p.u.. Here, it is worth mention-  
 307 ing that an equal relative loss reduction along the whole power range reflects  
 308 more valuable absolute loss reductions for higher powers. As expected, the  
 309 employment of the optimization algorithm in S3 has the lowest loss values  
 310 over the whole power range within the strategies with a fixed PCC voltage  
 311 reference. Nevertheless, the difference of the total losses between the best  
 312 conventional strategy (S1 or S2) for individual active power operating points  
 313 against S3 is of maximal  $0.57\%$  (at  $p = 0.63$  p.u.). The variable strategies  
 314 S1var to S3var demonstrate that the PCC voltage as control variable has an  
 315 important impact on the power losses. Specifically in the higher power range  
 316 for  $p > 0.4$  p.u. the variable strategy performs better than its fixed voltage  
 317 reference counterpart (S1var with respect to S1, etc.). It is remarkable that  
 318 S1var causes a similar result as S3var although the latter uses a more com-  
 319 plex optimization incorporating the individual reactive power set-points of

320 the WTs.

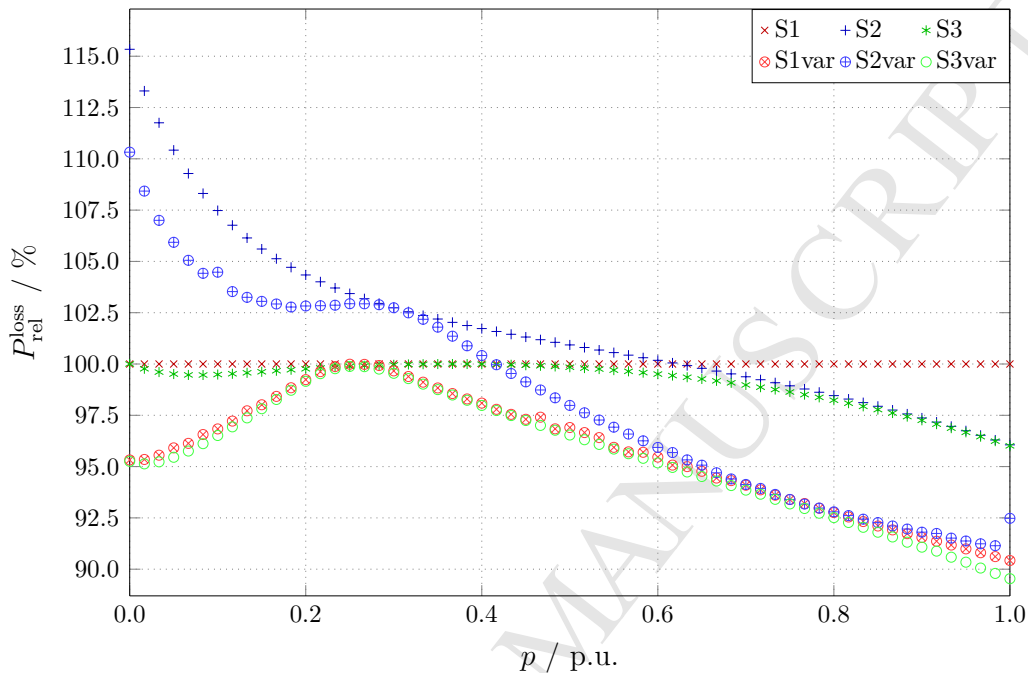


Figure 6: Relative total system losses respective to S1 (set equal to 100%).

321 The total amount of consumption and generation of reactive power by  
 322 transformers, filters and submarine cables in the system has to be balanced  
 323 by the GSCs and VSC–HVdc. In the following the reactive power injections  
 324 by the VSC–HVdc  $q_{\text{PCC}}$  and by two GSCs  $q_{\text{WT}}$  are presented in Figure 7  
 325 and Figure 8 for the whole power range, respectively. For both graphs,  
 326  $q = 1 \text{ p.u.}$  is equal to a  $\text{PF} = 0.9$  at full power. The most remote WT from  
 327 the PCC busbar, WT1, and the closest one, WT46, have been selected for  
 328 visualization.

329 The results of S1 indicate that the VSC–HVdc absorbs reactive power  
 330 for lower powers and injects reactive power for higher powers. Similarly, for

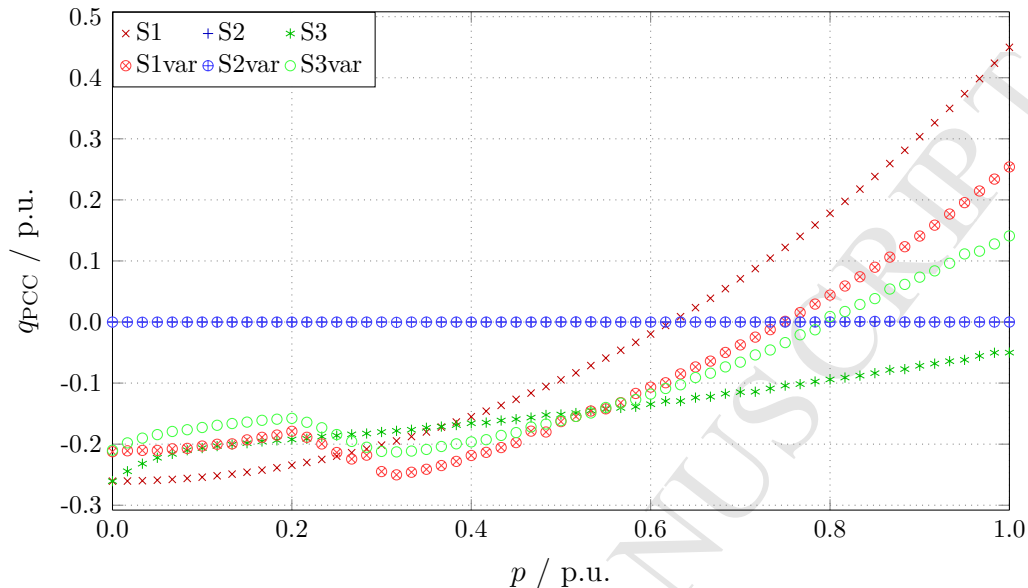
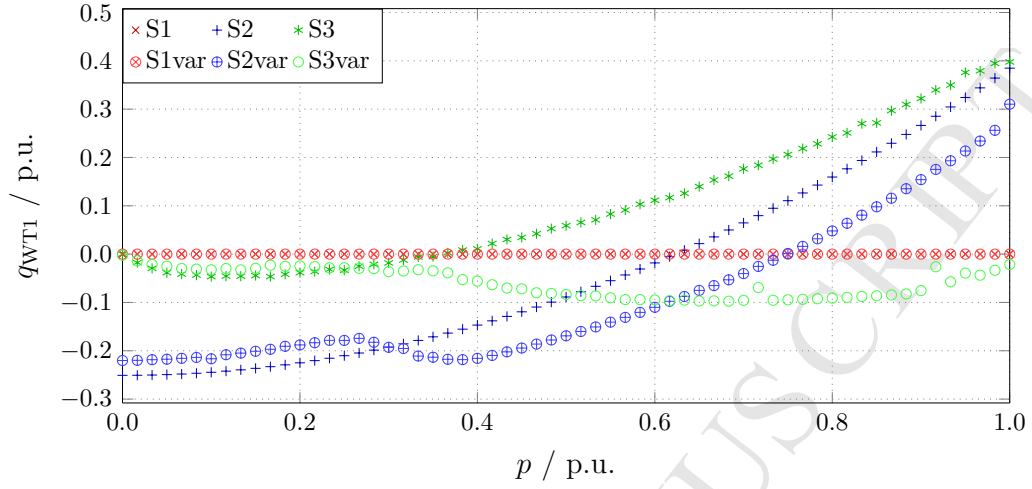
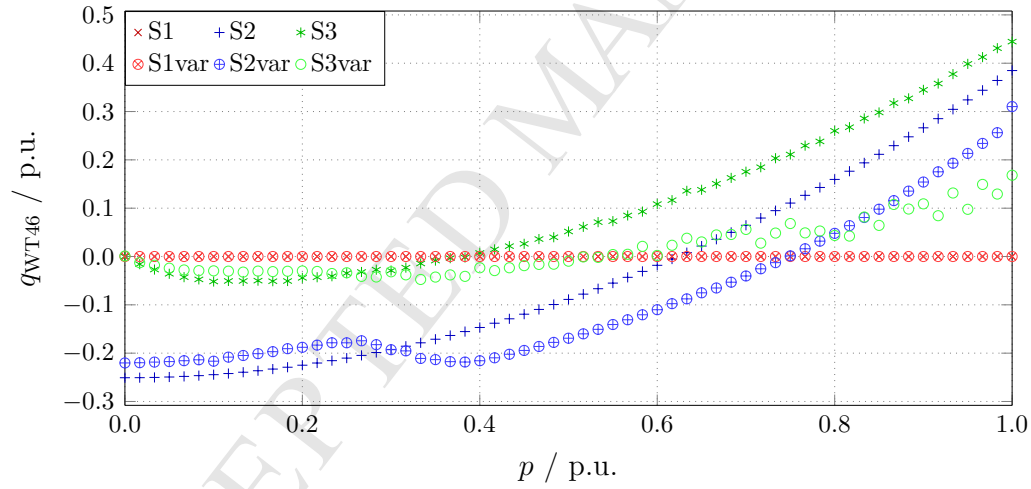


Figure 7: Reactive power injection by the VSC–HVdc. Positive values correspond to a reactive power injection (capacitive) by the converter.

331 strategy S2 the reactive powers of the WT's  $q_{WT}$  show the same behavior.  
 332 In both cases, these reactive power sources solely compensate the mentioned  
 333 amount of reactive power generated in the grid. Thus, the contributions by  
 334 the VSC–HVdc for strategy S2 as well as by the WT's for strategy S1 are  
 335 zero as expected. For strategy S1 and S2, respectively, the  $q_{WT}$  of WT1  
 336 and WT46 are identical due to the uniform set–point distribution for these  
 337 strategies. For the strategy S3 the set–points for the closest turbine are only  
 338 up to 0.04 p.u. higher than for the most remote one specifically for active  
 339 powers higher than  $p > 0.8$  p.u.. For lower active powers the difference  
 340 is marginal. In fact, the optimization does not result in a significant non–  
 341 uniform distribution of  $q_{WT}$  set–points. For the optimization-based strategies  
 342 cases without uniform  $q_i$  set–points (S3 and S3var) the results in Figure 7



(a) WT1



(b) WT46

Figure 8: Reactive power injection by (a) the most remote and (b) the closest WT, respectively.

343 and Figure 8 show the contribution to the total amount of necessary reactive  
 344 power by the WTs and the VSC-HVdc. Comparing the total reactive power



345 injection for S3 and S3var results in a lower value for strategy S3var than for  
 346 S3. This effect is due to the additional variable PCC voltage reference  $u_{\text{PCC}}$   
 347 in strategy S3var which lowers the reactive power generation in the low power  
 348 range by decreasing the system voltage. Furthermore, regarding the variation  
 349 of the  $q_{\text{WT}}$  set-points for strategy S3var it can be seen that the values for WT1  
 350 and WT46 differ for active powers  $p > 0.6$  p.u. whereas WT1 is absorbing  
 351 reactive power and WT46 is injecting reactive power. This operation of  
 352 WT1 avoids a local voltage violation due to the higher PCC voltage for this  
 353 strategy in this power range. Due to its vicinity to the PCC WT46 is not  
 354 facing this constraint and injects reactive power to compensate. The other  
 355 variable strategies S1var and S2var lower the reactive power requirement with  
 356 respect to their counterpart S1 and S2, respectively. This holds true expect  
 357 for an intermediate power range  $0.25$  p.u.  $< p < 0.68$  p.u. for S1 against S1var  
 358 whereas  $0.3$  p.u.  $< p < 0.7$  p.u. for S2 versus S2var.

359 Figure 9 shows the PCC voltage set-point  $u_{\text{PCC}}$ . For the strategies S1  
 360 to S3 the  $u_{\text{PCC}}$  is fixed at  $1.0$  p.u.. The variable strategies S1var and S2var  
 361 result in similar  $u_{\text{PCC}}$  profiles as S3var. In the lower power range the system  
 362 voltage is decreased to reduce the reactive power requirements (and related  
 363 power losses) and the associated power losses in the converters whereas for  
 364 higher powers the increase of the system voltage leads to lower losses.

365 The loss distribution in the system appears as component losses of the  
 366 GSC, the WT transformer and filter, the  $33$  kV collection grid, the WPP  
 367 transformers, the HVac export cables and the VSC-HVdc (incl. HVdc transf.).  
 368 The loss distribution results in Figure 10 and Figure 11 consider the cases  
 369 where zero or full power is generated, respectively. The power losses differ-

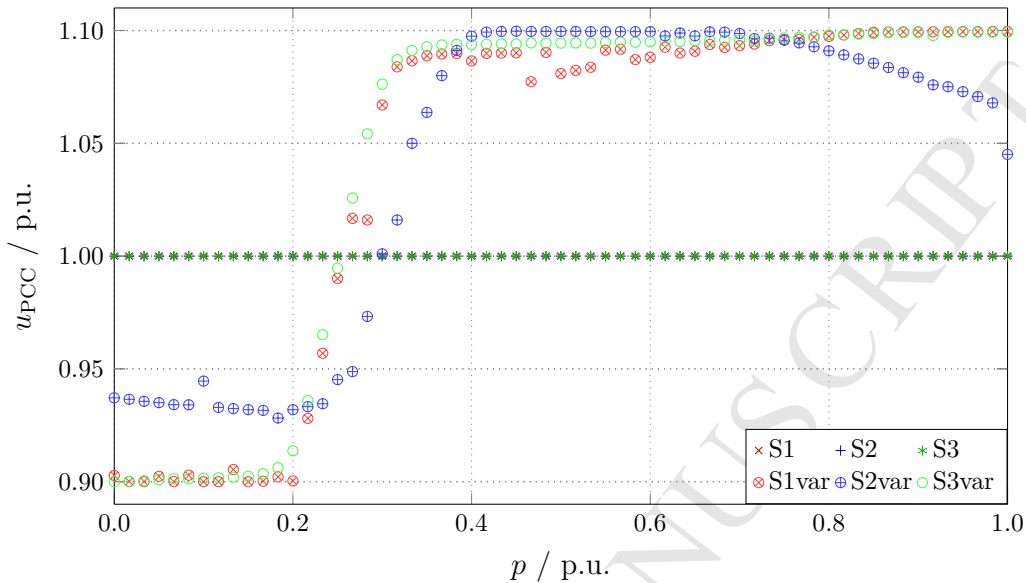


Figure 9: PCC voltage reference set-point imposed by the VSC-HVdc.

ences between the strategies occur mainly in the converters and transformers  
 (no-load losses) for low power (Figure 10) and in the grid components for  
 the full power case (Figure 11). The higher voltage in the offshore grid for  
 S1var to S3var reduces the losses of the grid components in general. From  
 the results for the converter losses for S2 and S2var in the low power scenario  
 it can be concluded that higher losses occur in the GSC and lower losses in  
 the VSC-HVdc compared to the other strategies. Overall, this results in a  
 higher relative loss for strategy S2 compared to S1 in the low power range as  
 depicted in Figure 6.

Figure 12 provides information on voltage values for relevant busbars in  
 the system. The plots use boxplots to display mean, 25 % and 75 % per-  
 centiles as well as minimum and maximum values of the corresponding sets  
 over the whole power range. In Figure 12a the voltage levels are shown

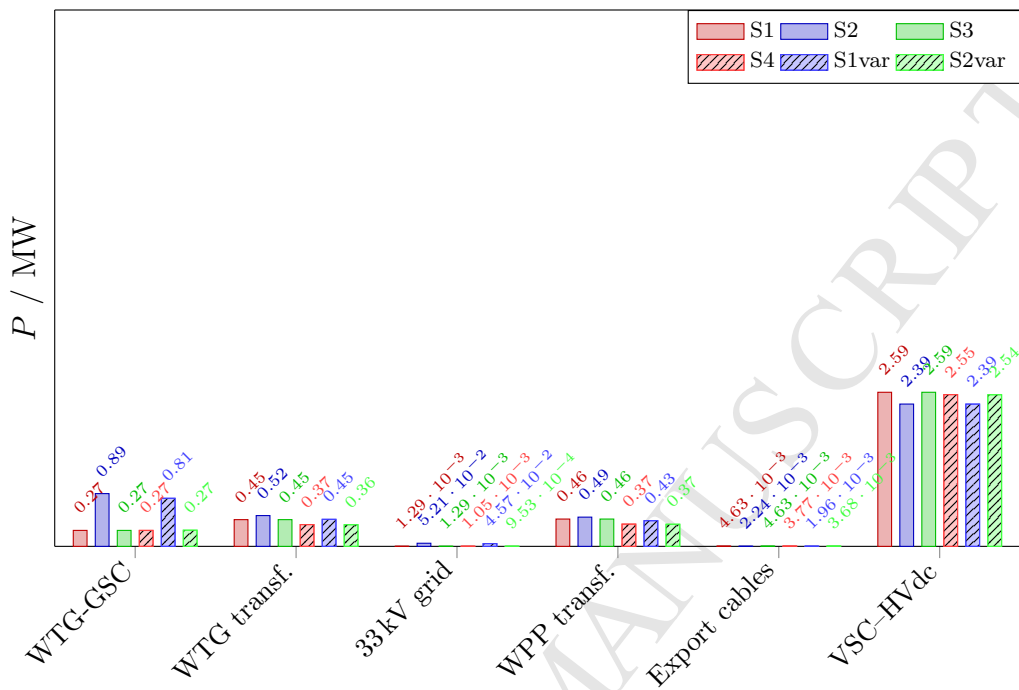


Figure 10: Distribution of losses in the system for  $p = 0.0$  p.u..

383 for strategies S1 to S3 specifically for the busbars of the HV-side of the WT  
 384 transformers, the LV-side of the WPP transformers, denoted as offshore sub-  
 385 station (OSS), and the PCC voltage. Figure 12b displays the voltage levels  
 386 for the variable strategies S1var to S3var. Firstly, the voltages are kept within  
 387 the admissible voltage limitations for all busbars and strategies. Secondly, it  
 388 can be seen that the mean voltages for the WTs are higher for S3 compared to  
 389 S1 and S2 due to the optimization procedure. The variable strategies S1var  
 390 and S2var explore a wider voltage band compared to their counterparts. For  
 391 strategy S1var and S3var the voltages of the WTs are almost exclusively close  
 392 to the upper limit of 1.1 p.u.. Among the fixed reference voltage strategies  
 393 S1 has the most varying voltage profile at the OSS busbar whereas S2 keeps

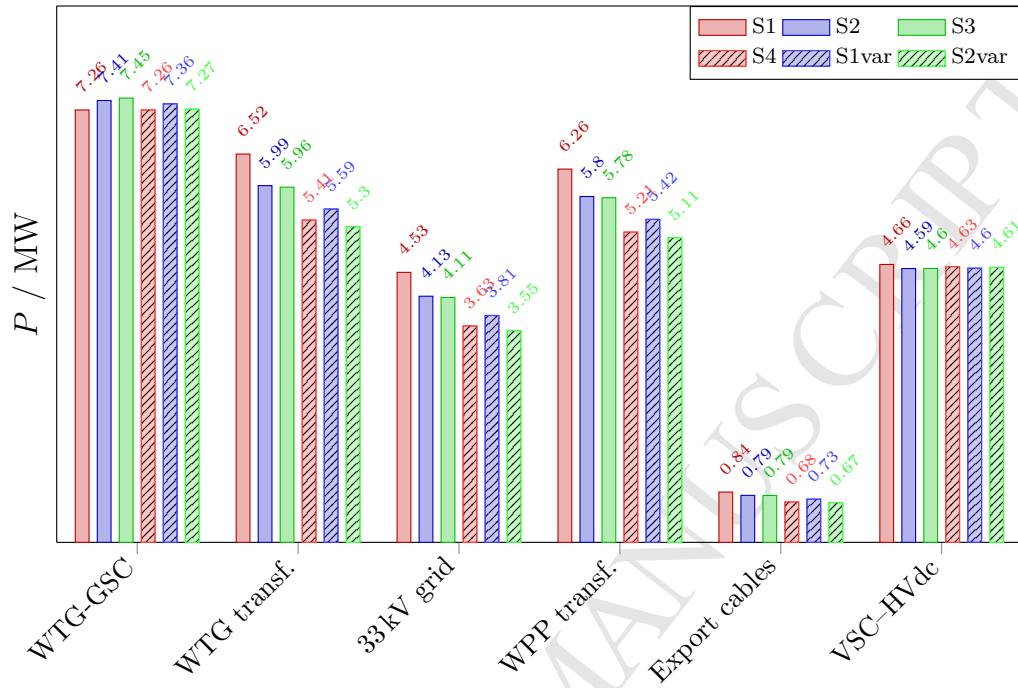


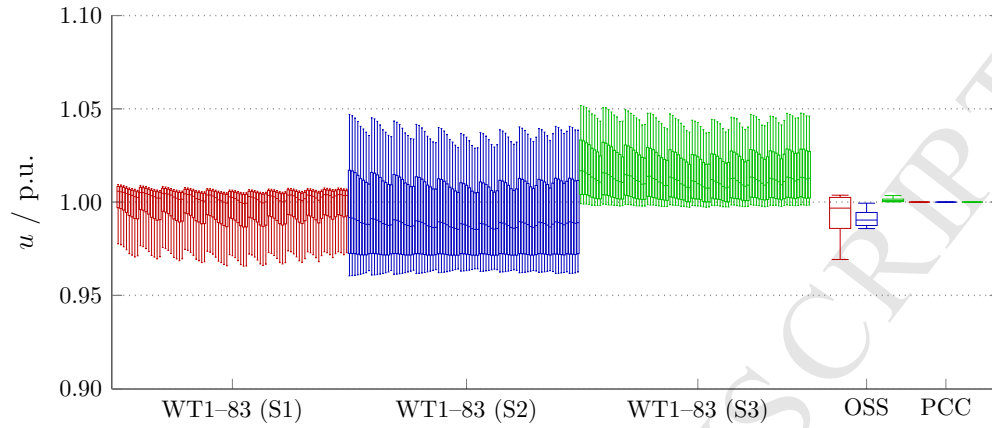
Figure 11: Distribution of losses in the system for  $p = 1.0$  p.u..

394 its values closely below 1 p.u.. The values for S3 show insignificant variation  
 395 for this busbar slightly above 1 p.u.. For the variable strategies this busbar  
 396 voltage correlates with the variable PCC voltage.

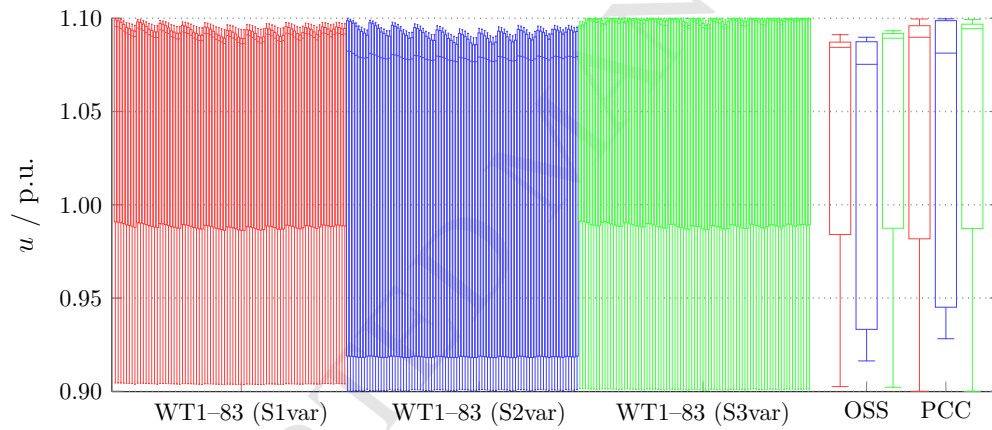
397 Figure 13 depicts the reactive power injections by the GSCs and the VSC-  
 398 HVdc. Again, Figure 13a displays the results for the fixed voltage strategies  
 399 whereas Figure 13b contains the results for the variable strategies. Firstly,  
 400 the plots show that S1 and S2 both cause a uniform reactive power injection  
 401 by the WTs. The values for S3 (for S3var, respectively) vary from each  
 402 other and demonstrate the variable distribution of set-points caused by the  
 403 optimization routine, respectively. For strategy S3, the reactive power values  
 404 of the GSC are mainly injections which result in a generally higher voltage

405 in the WPP grid when compared to S1 and S2. In contrast, for strategy  
406 S3var the use of a high PCC voltage reference results in a partly inductive  
407 operation of the GSCs in order keep the voltage inside the upper limit. This  
408 is especially the case for WTs which are very remote to the PCC busbar such  
409 as WT1 (see also Figure 8a). Secondly, the variation of the reactive power  
410 injection by the VSC–HVdc is the highest for S1 whereas S3 is kept within  
411 a moderate range absorbing reactive power. The plot of S2 consequently  
412 results to zero reactive power exchange. For strategy S3var the VSC–HVdc  
413 operates mainly absorbing reactive power unless for higher powers where it  
414 injects reactive power. Contemplating the combination of both the WT and  
415 the VSC–HVdc results it is obvious that S3 and S3var reach a sharing of  
416 reactive power injection within the WPP. The variable strategies result in  
417 less reactive power injection variation than their respective fixed strategies.  
418 This is caused by the variable PCC voltage which lowers the reactive power  
419 requirements of the converters in the system.

420 The annual energy loss (AEL) obtained by applying the different strate-  
421 gies is displayed in Table 3. For S2 the absolute energy losses are reduced  
422 by 696 MWh and for S3 by 2131 MWh compared to strategy S1, respectively.  
423 The variable strategies permit a further loss reduction: S1var 6320 MWh,  
424 S2var 4224 MWh and S3var 6819 MWh in comparison to S1, respectively.  
425 The monetary saving of these additional active power in–feeds is of 90 k€ for  
426 S2, 277 k€ for S3 and oscillates between 549 k€ and 886 k€ for the variable  
427 strategies, respectively.



(a)

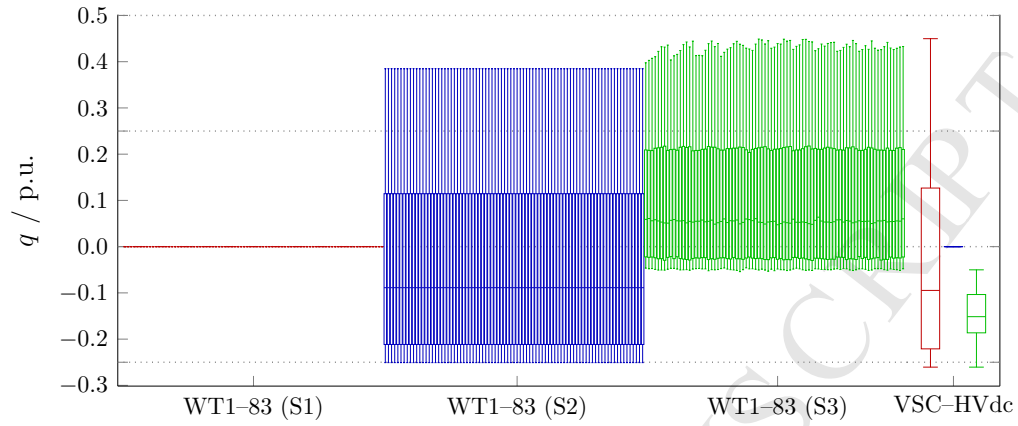


(b)

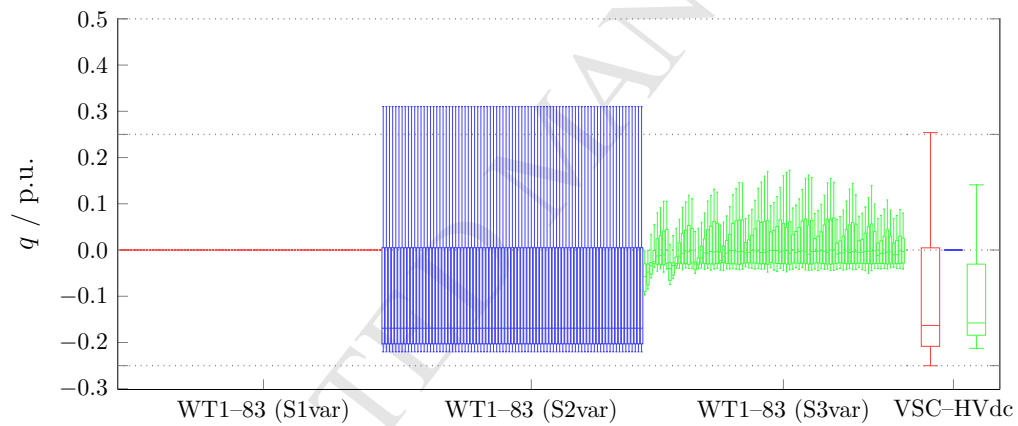
Figure 12: Voltage distribution of (a) fixed reference voltage strategies and (b) variable reference voltage strategies. The boxplots show mean, 25%-, 75%-percentiles, minimum and maximum values. The HV-side busbars of the WT transformers, the LV-side of the WPP transformer (OSS) and the PCC busbar are displayed.

## 428 5. Conclusions and recommendations

429 This work presented reactive power and voltage control concepts to op-  
 430 erate HVdc-connected WPPs aiming to minimize overall system losses. The



(a)



(b)

Figure 13: Reactive power injections of (a) fixed reference voltage strategies and (b) variable reference voltage strategies. The boxplots show mean, 25%-, 75%-percentiles, minimum and maximum values. All GSC and VSC-HVdc reactive power injections are plotted. A positive value expresses to a reactive power injection (capacitive).

431 WT reactive power set-points and the PCC reference voltage imposed by the  
 432 offshore VSC-HVdc are calculated to gain minimal losses in the system by

Table 3: AEL and the monetary equivalent (ME) thereof.

	S1	S2	S3	S1var	S2var	S3var
<i>AEL</i> / GWh	94.54	93.84	92.41	88.22	90.3	87.72
<i>ME</i> / M€ <sub>yr</sub> <sup>-1</sup>	12.29	12.20	12.01	11.47	11.74	11.40

433 means of an optimization-based algorithm. First, a loss assessment has been  
 434 conducted for such HVdc-connected WPPs where the collection grid and  
 435 converter losses of the VSC-HVdc as well as of the WTs are considered. A  
 436 case study for a 500 MW-sized reference WPP was performed for the whole  
 437 active power range to draw conclusions for six different reactive power con-  
 438 trol concepts. From the results it was concluded that the optimization-based  
 439 reactive power control contributes to a reduction of energy losses by up to  
 440 4% for a fixed PCC voltage and up to 10% with the incorporation of a  
 441 variable PCC voltage set-point in comparison to unity PF operation of the  
 442 WTs. Moreover, it was found that in case of the conventional reactive power  
 443 allocation strategies the application of a single reactive power injection re-  
 444 sponsibility for either GSCs or the VSC-HVdc is not optimal considering  
 445 the whole power range. Consequently, the use of an optimization-based  
 446 algorithm results in a share of the reactive power injection responsibility  
 447 between the WT and the VSC-HVdc. The application of the variable strate-  
 448 gies S1var, S2var or S3var result in lower losses and mostly lower reactive  
 449 power injections at the expense of a wider usage of the continuous voltage  
 450 operation band. The deployment of the variable strategy might cause the  
 451 system to operate continuously at its voltage limits which might inherently



452 violate them if the system operating point changes. This drawback might be  
453 counteracted with an additional security margin on the voltage limits in the  
454 optimization algorithm. The results of the optimization-based controllers  
455 motivate the implementation of such into the central WPP control. Fur-  
456 thermore, the involved parties in the system which are generally the offshore  
457 transmission asset owner (HVdc system owner) and the WPP owner could  
458 share the additional benefits of a calculated 886 k€ annual cost reduction for  
459 the 500 MW case study performed in this paper.

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464 project title MEDOW.

#### 465 **Appendix A.**

Table A.4: Reference data and relevant system parameter.

<b>WT grid connection</b>	
Nominal voltage ( $U_{ac}/\text{kV}$ )	0.9
GSC ( $S_n/\text{MVA}$ , $\cos \varphi$ )	6.67, $\pm 0.9$
Coupling impedance ( $r/\text{p.u.}$ , $x/\text{p.u.}$ )	0.004, 0.13
MV transformer ( $LV/HV$ , $S_n/\text{MVA}$ , $r/\text{p.u.}$ , $x/\text{p.u.}$ , <i>no-load losses/p.u.</i> )	0.9/33, 6.7, 0.009, 0.06, 0.0008
<b>MV collection grid</b>	
Nominal voltage ( $U_{ac}/\text{kV}$ )	33
Total cable length ( $l/\text{km}$ )	118
Total number of turbines	83
HV transformer ( $N$ , $LV/HV$ , $S_n/\text{MVA}$ , $r/\text{p.u.}$ , $x/\text{p.u.}$ , <i>no-load losses/p.u.</i> )	2, 33/220, 280, 0.003, 0.15, 0.0004
<b>HV ac export cable</b>	
Nominal voltage ( $U_{ac}/\text{kV}$ )	220
Export cable(s) ( $N$ , $A/\text{mm}^2$ , $l/\text{km}$ )	2, 800, 10
<b>HV dc transmission</b>	
Nominal voltages ( $U_{ac}/\text{kV}$ , $U_{dc}/\text{kV}$ )	333, $\pm 320$
Converter (topology, $S_n/\text{MVA}$ , $\cos \varphi$ )	HVdc-MMC, 555.6, $\pm 0.9$

Table A.5: Data for XLPE submarine cables [43, 44, 45].

$U_r / \text{kV}$	$A / \text{mm}^2$	$I_r / \text{A}$	$R' / \Omega \text{ km}^{-1}$	$L' / \text{mH km}^{-1}$	$C' / \mu\text{F km}^{-1}$
33	240	581	0.098	0.36	0.23
33	630	904	0.041	0.31	0.34
220	800	830	0.032	0.40	0.17

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### Highlights

- Optimization-based reactive power control in HVDC-connected offshore wind power plants
- Algorithm uses individual set-points for reactive power and system reference voltage
- Methodology for loss assessment in such systems
- Annual benefit equaling around 0.8 MEUR for a 500-MW-sized wind power plant