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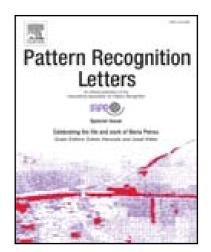
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## **Research Highlights (Required)**

- We propose a new facial recognition system which learns the multi-channel and multi-model facial representations.
- A new autoencoder with ADMM optimization which increases the recognition rates is designed.
- The new system learns facial representations that promote to capture intra-facial-region changes more precisely.
- The face recognition rates are boosted using unsupervised and hand-crafter features.
- We achieve the state-of-the-art results on several facial datasets.

# Multi-Channel Multi-Model Feature Learning for Face Recognition

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#### Abstract

Different modalities have been proved to carry various information. This paper aims to study how the multiple face regions/channels and multiple models (e.g., hand-crafted and unsupervised learning methods) answer to the face recognition problem. Hand crafted and deep feature learning techniques have been proposed and applied to estimate discriminative features in object recognition problems. In our Multi-Channel Multi-Model feature learning (McMmFL) system, we propose a new autoencoder (AE) optimization that integrates the alternating direction method of multipliers (ADMM). One of the advantages of our AE is dividing the energy formulation into several sub-units that can be used to paralyze/distribute the optimization tasks. Furthermore, the proposed method uses the advantage of K-means clustering and histogram of gradients (HOG) to boost the recognition rates. McMmFL outperforms the best results reported on the literature on three benchmark facial data sets that include AR, Yale, and PubFig83 with 95.04%, 98.97%, 95.85% rates, respectively.

Keywords: Unsupervised learning, face recognition, autoencoder, sparse estimation, ADMM.

### 1. Introduction

Ideally, object and face identification has four procedures - feature learning, feature extraction using labeled data, supervised training, and testing. Representative and discriminative features are desired to be learned and extracted from the object of interests. To boost the identification rate and to accelerate the learning process, many hand-crafted and unsupervised learning techniques have been developed that we will review a few of them below.

Since global representation methods, such as Eigenface (1) and Fisherface (2), fail to capture high-order statistics, local feature extraction techniques have been proposed such as local binary pattern (LBP) (3), scaleinvariant feature transform (SIFT) (4), histograms of oriented gradients (HOG) (5), rotation-and scale-invariant, line-based color-aware descriptor (RSILC) (6), and correlation based features (7). Although those techniques have proved that they are capable of obtaining good classification accuracy in limited scenarios, they are incapable of extracting the non-linear features.

Deep learning methods are designed to learn hierarchical representations in deep architectures for classification (8). Traditional unsupervised models such as sparse Restricted Boltzmann Machine (RBM) (9), and sparse auto-encoder (10) have shown improved results in many classification tasks. Hierarchical model for sparse representation learning was proposed to build high level features (11). Greedy layer wise pre-training (12; 13) approach in deep learning (8) became very popular for deep hierarchical frameworks. Multi-layer of stacked sparse auto-encoder (SAE) (13; 14; 11), sparse deep belief net (DBN), and convolutional deep belief net (CDBN) (15) are few frameworks for learning sparse representation.

Several methods have been proposed in the literature that combines multiple modalities to enhance the face recognition performance. Ngiam et al. (16) proposed a multimodel learning technique that combines the features of the visual and audio information. Srivastava et al. (17) proposed a generative model of data that consists of multiple and diverse input modalities. They used a Deep Boltzmann Machines (DBM) to handle multimedia data feature learning such as image database with tags. Their model generates a fused representation from multiple data modalities. Shekhar et al. (18) proposed a multimedia or multi-biometric identification method that combines the information from different biometric modalities. Nilsback et al. (19) made a representative analysis on combining hand-crafted features (e.g., HOG, SIFT, and Hue-saturation-value) on flower classification. Huang et al. (20) proposed an idea that combines features from their deep learning system and hand-crafted techniques. The combination of multiple modalities slightly increased the face verification accuracy.

In this paper, we combine features extracted from multiple regions that are processed with multiple models such as hand-crafted and unsupervised feature learning methods. The main contributions are summarized as follows:

- (1) We propose a new AE optimization and draw upon the idea from the alternating direction method of multipliers (ADMM) formulation (21). Our proposed encoder-decoder module efficiently extracts sparse representation of facial regions. One of the most important advantages of the ADMM-based optimization is the ability to divide the energy formulation into several units that can be used to paralyze/distribute the optimization tasks.
- (2) The multi-channel learning procedure extracts representations that capture intra-region changes more precisely. Additionally, the unsupervised learning methods obtain specialized bases for corresponding regions. Instead of estimating a single centroid of a face region, feature learning for multi-region increases the detailed representation that learns more representative information as we assess this point in our experiments.
- (3) Finally, fusing various features from multiple techniques enables us to achieve promising results.

The paper is organized as follows: Section 2 introduces the proposed method in details. The experimental setup

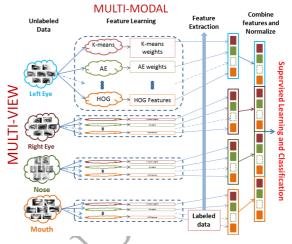


Figure 1: Architecture of the proposed Multi-Channel Multi-Model feature learning (McMmFL) system.

and results are explained and discussed in Section 3. Finally, we conclude in Section 4.

# 2. Methods

Our system, as shown in Fig. 1, first extracts essential sub-regions from images, and applies preprocessing and normalization steps, followed by running the handcrafted and unsupervised feature learning methods. After the system learns the bases, the features are extracted from the testing data. In this section, we will describe feature learning methods that we propose and employ.

#### 2.1. The Proposed Autoencoder (AE)

We introduce a new encoder-decoder system for unsupervised feature learning. While learning, for given *n* data samples in  $R^m$  represented by matrix  $\mathbf{X} = [\mathbf{x}_1, \dots, \mathbf{x}_n] \in R^{m \times n}$ , we want to learn a dictionary  $\mathbf{W}_{\mathbf{d}} = [\mathbf{w}_{d_1}, \dots, \mathbf{w}_{d_k}] \in R^{m \times k}$ , sparse representation code vectors  $\mathbf{Z} = [\mathbf{z}_1, \dots, \mathbf{z}_n] \in R^{k \times n}$ , and latent weight matrix  $\mathbf{W}_c$ , so that each input sample  $\mathbf{x}_j$  can be approximated by  $\mathbf{W}_d \mathbf{z}_j$ . A non-linear encoding function  $f(\mathbf{x}; \mathbf{W}_c)$  has been used to map  $\mathbf{X} \to \mathbf{Z}$ , where  $\mathbf{W}_c = [\mathbf{w}_{c_1}, \dots, \mathbf{w}_{c_k}]^T \in R^{k \times m}$ . The decoder module reconstructs the input sample approximately by  $\mathbf{X} \approx \mathbf{W}_d \mathbf{Z}$ . This leads to the following optimization problem over  $\mathbf{W}_d$ ,  $\mathbf{Z}$  and  $\mathbf{W}_c$ :

$$\arg\min_{\mathbf{W}_{\mathbf{d}}, \mathbf{Z}, \mathbf{W}_{\mathbf{d}}} \frac{1}{2} \|\mathbf{X} - \mathbf{W}_{\mathbf{d}}\mathbf{Z}\|_{F}^{2} + \lambda \|\mathbf{Z}\|_{1} + \frac{\alpha}{2} \|\mathbf{Z} - f(\mathbf{X}; \mathbf{W}_{\mathbf{c}})\|_{F}^{2},$$
(1)

subject to : 
$$\|\mathbf{w}_{\mathbf{d}_{i}}\|_{2}^{2} \le 1$$
 for  $i = 1, ..., k$ ,

where  $\lambda > 0$  is a parameter that controls the sparsity of the code vectors (features) and  $\alpha$  is a penalty parameter. We consider  $\|.\|_F$  and  $\|.\|_1$  to represent Frobenius norm and element-wise  $L_1$ -norm respectively. In our experiment, we use sigmoid activation function,  $f(\mathbf{X}; \mathbf{W_c}) =$  $(1 + exp^{-(\mathbf{W_c}\mathbf{X})})^{-1}$ , and set  $\alpha$  equals to 1. One can use different nonlinear activation functions, such as, hyperbolic tangent function and rectifier linear unit.

To solve Eq. 1, we propose to use the ADMM form (21), which is used for the convex optimization, to solve the general  $L_1$  regularized loss optimization, and the stochastic gradient descent. Z is estimated using the ADMM optimization, and  $W_d$  and  $W_c$  are estimated using the stochastic gradient descent. In the ADMM form, the problem can be written as:

minimize : 
$$f(\mathbf{Z}) + g(\mathbf{Y})$$
, (2)

subject to : 
$$\mathbf{Z} - \mathbf{Y} = 0$$
, (3)

where

$$f(\mathbf{Z}) = \frac{1}{2} \|\mathbf{X} - \mathbf{W}_{\mathbf{d}}\mathbf{Z}\|_{F}^{2} + \frac{\alpha}{2} \|\mathbf{Z} - f(\mathbf{X}; \mathbf{W}_{\mathbf{c}})\|_{F}^{2}, \quad (4)$$
$$g(\mathbf{Y}) = \lambda \|\mathbf{Z}\|_{1}.$$

The augmented Lagrangian will be

$$L(\mathbf{X}, \mathbf{W}_{\mathbf{d}}, \mathbf{W}_{\mathbf{c}}, \mathbf{Z}, \mathbf{Y}) = f(\mathbf{Z}) + g(\mathbf{Y}) + \frac{\rho}{2} \|\mathbf{Z} - \mathbf{Y}^{k} + \mathbf{U}^{k}\|_{F}^{2}.$$
 (6)

Then, the ADMM solution becomes

$$\mathbf{Z}^{k+1} = \frac{1}{2} \|\mathbf{X} - \mathbf{W}_{\mathbf{d}} \mathbf{Z}\|_{F}^{2} + (0.5) \|\mathbf{Z} - f(\mathbf{X}; \mathbf{W}_{\mathbf{c}})\|_{F}^{2} + \frac{\rho}{2} \|\mathbf{Z} - \mathbf{Y}^{k} + \mathbf{U}^{k}\|_{F}^{2}, \quad (7)$$

$$\mathbf{Y}^{k+1} = \lambda \|\mathbf{Y}\|_1 + \frac{\rho}{2} \|\mathbf{Z} - \mathbf{Y}^k + \mathbf{U}^k\|_F^2, \tag{8}$$

$$\mathbf{U}^{k+1} = \mathbf{U}^k + \mathbf{Z}^{k+1} - \mathbf{Y}^{k+1}.$$
 (9)

From here,  $\mathbf{Z}^{k+1}$  and  $\mathbf{Y}^{k+1}$  are estimated using the gradient descent and soft-thresholding (21), respectively. In the same iteration loop, we, then, estimate and update  $\mathbf{W}_{d}$ ,  $\mathbf{W}_{c}$  using stochastic gradient descent method.

$$\mathbf{W}_{\mathbf{d}} \leftarrow \mathbf{W}_{\mathbf{d}} - \eta_1 \nabla_{\mathbf{W}_{\mathbf{d}}} J(\theta), \tag{10}$$

$$\mathbf{W}_{\mathbf{c}} \leftarrow \mathbf{W}_{\mathbf{c}} - \eta_2 \nabla_{\mathbf{W}_{\mathbf{c}}} J(\theta), \tag{11}$$

where gradient calculations are given by  $\nabla_{\mathbf{D}} J(\theta)$  and  $\nabla_{\mathbf{W}} J(\theta)$  with respect to **D** and **W** correspondingly.

#### 2.2. K-means and Hand-crafted Features

The K-means clustering method obtains specialized bases for the corresponding region of data. Coates et al. (22) proved that the K-means method can achieve comparative or better results than other possible unsupervised learning methods. The algorithm takes the dataset **X** and outputs a function  $f : \mathbb{R}^n \to \mathbb{R}^k$  that maps an input vector **x** to a new feature vector of *k* features. We follow to minimize the following equation:

$$f_a(x) = \max\{0, \mu(q) - q_a\},$$
 (12)

where  $q_d = ||\mathbf{x} - \mathbf{C}^{(a)}||_2$  and  $\mu(q)$  is the mean of the elements of q. Refer to (22) for more description of this method.

In our system, one of the most powerful hand-crafted feature descriptors is employed to boost the rates. We believe that in addition to original gray-level information, image gradient will also contribute to the multi-model object feature learning and classification. The traditional HOG features are estimated on gradient information of images. We refer to this method hereafter as *HOGgrad*. In our experiments, the HOG and HOGgrad features were obtained every 8 pixels on each image view; and the dimension of each HOG descriptor for an image view is 128.

#### 2.3. Feature Extraction

In the unsupervised learning process, we calculate new bases for each method (i.e., K-means and our AE). In the testing stage, the new projected data is calculated using the correlation information between the labeled data and estimated bases.

Let  $\mathbf{X}_i$  be any image region and  $\mathbf{C}_i$  and  $\mathbf{W}_{\mathbf{d}_i}$  are the corresponding bases using the K-means and our AE methods, respectively. The features of labeled data corresponding to image regions are calculated as  $\mathbf{Y}_i = \mathbf{X}_i \mathbf{C}_i^t$  (for K-means features) and  $\mathbf{A}_i = \mathbf{X}_i \mathbf{W}_{\mathbf{d}_i}^t$  (for AE features). Then, the extracted features are combined together one by one to get the multi-model representation as  $\mathbf{Y} = [\mathbf{Y}_1; \mathbf{Y}_2; \dots; \mathbf{Y}_M]$  and  $\mathbf{A} = [\mathbf{A}_1; \mathbf{A}_2; \dots; \mathbf{A}_M]$ , where M equals to the number of image region (and sometimes

multimedia data such as speech). HOG and HOGgrad features can be represented as  $\mathbf{H} = [\mathbf{H}_1; \mathbf{H}_2; ...; \mathbf{H}_M]$  and  $\mathbf{G} = [\mathbf{G}_1; \mathbf{G}_2; ...; \mathbf{G}_M]$ . Finally, the feature vector that represents a whole image is represented as  $\mathbf{V} = [\mathbf{Y}; \mathbf{A}; \mathbf{H}; \mathbf{G}]$ . In our experiment, each method estimates 128 feature units for each image region.

#### 3. Experiments and Result

In our experiments, we assess the performance of our proposed method on three data sets: AR (23), Yale (2), and wild PubFig83 (24) data. All images in our experiments are locally normalized to have the Gaussian distribution and whitened as in (22). In the unsupervised learning part, we train the entire labeled training set of images before the classification step. One of the most important detail is the feature normalization procedure. To be more specific, while each channel-feature and each model-feature are normalized using  $L_2$ -norm individually, we observe improved results. We use the linear support vector machine (SVM) for the classification.

#### 3.1. Evaluation on AR Face Database

The aligned AR database (23) contains 100 subjects (50 men and 50 women), with 14 different images per subject which totals to 1,400 images (excluding the occluded images) taken in two sessions. There are facial expression (neural, smile, anger, scream) and illumination challenges. We segment four essential facial regions with sizes of 39 x 51 (left eye and right eye), 30 x 60 (mouth), and 45 x 42 (nose). We conduct 10 runs for train-test procedure to get the average recognition rate for each partition.

Table 1 presents the detailed experimental results and comparison between our system and some of representative methods. We follow the same framework (26; 22) for each method to obtain a fair comparison. We achieved 81.35% and 94.42% recognition accuracy using 2 and 5 training images per subject, respectively. The best results were obtained using the features of K-means, HOG, HOG (Gradient), and the proposed AE. The closest rates were achieved by Wang et al. (28) that are 75.5% (using 2 training and 180 feature units), 94.71% (using 7 training images per subject and 540 feature units). We also assess the feature dimensions of the K-means and AE. Using the 256 units for each method increased the recognition accuracy more than 0.6%.

Table 1: Comparison of face recognition rates on AR database with some of the representative methods and individual feature learning methods that we use/propose in this paper. In the table T represents 'Train'.

	Acc. (%)	<b>^</b>
Methods	2 Train	5 Train
PCA (25)	34.94	56.13
NPE (25)	40.45	61.12
LPP (25)	55.07	71.58
ONPP (25)	62.20	81.76
EPP (25)	72.45	86.23
Sparse Filtering (26)+SVM	63.14	84.56
Coates et al. (22)	65.24	85.56
McDFR (27)	70.92	91.54
Wang et al. (28)	75.50	(94.71) 7 <i>T</i>
$\sim$ $>$	180 d.	540 d.
K-means	75.56	89.40
HOG	71.96	89.67
HOGgrad	67.32	86.60
AE (128)	74.60	90.13
AE (256)	78.07	91.33
AE (128) + K-means	75.23	90.73
AE (256) + K-means	78.40	91.87
HOG + HOGgrad	77.20	91.33
K-means + HOG	82.61	93.91
K-means + HOGgrad	83.06	93.42
AE + HOG	82.38	93.40
AE + HOGgrad	80.76	92.26
<b>McMmFL</b> ( <i>128</i> )	81.35	94.42
<b>McMmFL</b> (256)	82.12	95.04

We assess the response of our method to missing facial region/information as shown in Table 2. Results show that eye regions contains the most effective, important, discriminative information. Missing nose and mouth features decreases the rates around 1.5%, whereas missing both eyes decreases the original rates more than 20%. However, achieving 81.80% should not be underestimated using just nose and mouth regions in one hundred subjects. Shekhar et al. (18) obtained 75.0% recognition accuracy on sun-glass occluded database. Naseem et al. (29) achieved only 26% correct classification rates on subjects that were wearing scarf that closes only mouth region.

We also test our system on various signal-to-noise ratio

Table 2: Classification in AR database on missing information.

Missing Region	Acc. (%) with 5 Train
Mouth	93.69
Nose	94.06
Right Eye	91.78
Left Eye	91.91
Mouth and Nose	93.00
Right and Left Eye	81.80

Table 3: Comparison of face recognition rates on AR database with respect to the dimension.

	Acc. (%) with 5 Train			
Methods	32 d.	64 d.	128 d.	256 d.
K-means	86.93	88.18	89.40	89.75
Our AE	85.67	88.87	90.13	91.33
McMmFL	93.71	93.89	94.42	95.04

(SNR). Table 4 shows the results using images with 20db and 10db SNR versus features with 128 and 256 dimensions. We use the same data trough all steps, i.e., in unsupervised and supervised learning and hand-crafted feature extraction stages. It is observed that the more dimensions the features, the more robust the recognition to the noise.

To explore how the multi-region unsupervised learning extracts more representative features rather than the learning features from the whole facial region. The whole faces are in the sizes of  $110 \times 80$ . Since the dimension is bigger than each facial region, we choose to learn 1028 dimensional features. Although the learned feature dimension of whole facial region is doubled, the multi-region technique achieves much better recognition rates as shown in Table 5.

In terms of the execution time, the proposed AE method learns 128 dimensional features in 334 seconds whereas the sparse coding method (30) extracts the same dimensional features in 2565 seconds for one eye region that is in 39 x 51 size.

#### 3.2. Face Recognition on Yale Database

The Yale database contains 165 images with 15 subjects and 11 frontal images per subject. Each image has Table 4: Noise test on AR.

SNR			
dim.	Original	20db	10db
128	94.42	93.72	86.86
256	95.04	94.83	90.15

Table 5: Learning on multi-region versus whole facial region on AR.

Training				
Region	Input dim.	Feat. dim.	2 T	5 T
Whole Face	8800	1028	68.12	86.26
Multi-region	5679	512	75.23	90.73

one type of facial expressions and configurations. Four essential facial regions are segmented as 40 x 60 (left eye and right eye), 32 x 46 (mouth), and 60 x 48 (nose). The analysis of the experimental results on Yale database is shown in Table 6. We compare the recognition accuracy with various number of training images per subject. For example, K-means obtains 90.22% classification rate, whereas our AE achieves 91.12% when using 8 training images. In the same situation, HOG and HOGgrad get 93.78% and 89.34%, respectively. Perhaps, the less number of training samples for the unsupervised learning methods (i.e., K-means and our AE) should be the reason of the lower classification rates than HOG features. When we combine the features from all techniques, the rate is increased to 98.97%. The closest rate to our results was achieved by Chen et al. (27) that is 97.78%.

#### 3.3. Face Recognition on selected PubFig Database

Unlike the traditional controlled databases, unconstrained databases contain unrestricted varieties of expression, pose, lighting, occlusion, resolution, etc. We use the PubFig83 database (33) with 83 subjects and at least 100 images per subject. Figure 2 shows some random images from this data. We randomly select 90 images per subject as the training set, and the rest of the images are used as the testing set in the supervised learning step. The facial regions are in the sizes of 32 x 52 (eyes), 48 x 76 (mouth), and 60 x 48 (nose).



Figure 2: Some example images from the aligned PubFig83 database with various real-world changes on facial expression, pose, illumination, occlusion, resolution, etc.

We present our recognition results on Table 7. Chiachia et al. (33) and Chen et al. (27) achieved 92.28% and 90.14% recognition rates, respectively. Chen et al. used the discriminative features learned from the supervised deep neural network. Our system outperforms and achieves 95.87% rate. This comparison also shows that each region and each model contribute unique and discriminative features.

#### 4. Conclusion

We have presented the analysis on multi-channel multimodel feature learning for face recognition. Our experiments verify again that learning features from various techniques and regions boost the classification rates. Although recent convolutional neural network (CNN) techniques that have more than 6 convolutional layers may be the best candidate to achieve the state-of-the-art results on many large scale databases, they have some drawbacks to be used in all applications. One is their time consuming training process that can end up days. Our new AE system can be applied to solve energy formulations with a time and cost efficient parallelized system that will be our one of future search. The other drawback of recent CNNs is that they need high number of samples to avoid over-fitting whereas it can be difficult to find many labeled samples as in this paper.

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Table 6: Comparison of face recognition rates on Yale database (See (31;
32) for the abbreviations).

	<b>Recognition rate(%)</b>		
Methods	2 T	4 T	8 T
LocLDA (31)	55.30	73.80	-
PCA (32)	42.63	52.86	64.33
LPP (32)	57.19	75.14	84.11
LPDP (32)	56.74	78.90	90.67
DLPP/MMC (32)	58.19	78.14	89.56
LDA (32)	45.19	68.95	83.22
SNPE1 (32)	66.77	73.61	79.33
DSNPE1 (32)	72.33	86.85	96.00
McDFR (27)	76.58	89.90	97.78
K-means	66.2	82.7	90.22
HOG	73.18	84.38	93.78
HOGgrad	69.94	80.13	89.34
AĚ	68.87	83.13	91.12
McMmFL	85.34	93.87	98.97

Table 7: Analysis of face recognition rates on the PubFig83 database. The unit number is 96 for the unsupervised learning methods.

	Acc. (%)
Methods	90 Train
McDFR (27)	90.14
Chiachia et al. (33)	92.28
McMmFL	95.87

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