

# Reactive Component Injection Control of the Modular Multi-Output Power Electronic Transformer

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**Abstract**—Power Electronic Transformer(PET) is a promising component in the future power system. The modular PET is the most attractive due to its high voltage level and flexible function. Unfortunately, when the modular PET is driving multiple loads, there would be overmodulation issue in the AC-DC stage caused by the unbalanced load power. This paper proposed a reactive component injection control strategy to prevent overmodulation for a three-module PET under unbalanced load. Two specific algorithms are proposed. The effectiveness of the proposed control strategy and the two algorithms are verified by simulation results.

## I. INTRODUCTION

The power electronic transformer(PET), or solid state transformer(SST) is an emerging topic in the past decade [1]. Among various topologies, the module topology, which uses cascade H bridge(CHB) as AC-DC stage and multiple DABs as DC-DC stage has become most attractive for two reasons: the CHB enables the PET to interfacing MV/HV AC grid; the multiple DABs provide various choice of connection between PET and loads which brings flexible functions[2].

One possible configuration of PET is to supply multiple loads with the modules, as shown in Fig.1. This is attractive when the loads are of different voltage rating, or the loads themselves require galvanic isolation. In recent years two PETs of such connection are published [3][4]. Unfortunately, this connection will bring unequal power issue to the CHB stage modules C when the load power is severely unequal, the CHB module power will also be severely unequal. The unequal power will cause unequal distribution of modules AC voltage which brings over-modulation issue.

In the past years, some research work on this issue has already been done on CHB converter by M. Rezaei, H.Iman-Eini, and S.Farhangi in [5], as well as on cascade PV converter by Liming Liu and Hui Li in [6][7][8], but not very complete.

[5] gives a minimum reactive current algorithm, but the operation range of that algorithm limited. In [5], this range is not studied, and no alternative algorithm is provided when the system is operating out of that range.

[6][7] proposes a reactive power sharing algorithm. In their work, two rotation frames needs to be built: a D-Q frame and a D'-Q' frame. The D axis is aligned with the grid voltage

while D' axis is aligned with the grid current. Their algorithm of reactive component distribution is: the Q' axis-voltage of all the modules are set equal, meanwhile, the D' axis voltage of all the modules are set proportional to their power. This algorithm is complicated as it requires two rotational frames. What's more, the idea of sharing q' axis voltage meanwhile setting D' axis voltage proportional to their power, seems not to be the optimized.

Based on [6][7], [8] introduces a novel reactive voltage distribution method which adjusts the Q' axis component for a two-module system. The Q' axis voltages no longer needs to be equal, but re-distributed by some better coefficient. However, the method in [8] is based on a closed-loop trial and error process, but not based on a clear mathematical process. Consequently, without enough mathematical process, the derived distribution coefficient is not proved to be the optimized.

In this paper, the authors proposed a reactive component injection control strategy to handle the over-modulation issue under the unbalanced-load condition. Three specific algorithms are proposed: Shared  $U_D$  algorithm, Minimum  $I_Q$  Algorithm and the Maximum  $U_M$  Algorithm.

Although a real PET may consist of N (more than 3) modules, this paper only discusses the three-module PET as a start of this sort of research. The theory and idea in this paper form the fundamental of N module case.

The paper is organized as follows: Part II introduces the topology and the operation range under unity power factor mode; Part III introduces the basic theory of reactive component injection control; Part IV introduces three specific algorithms; Part V shows the simulation results.

## II. PET AC-DC STAGE UNDER UNITY POWER FACTOR CONTROL

The three-module single-phase three-load PET, shown in Fig.1 is the most simple and fundamental case of single-phase multi-load PETs. The input stage is a three-module CHB rectifier; the isolation stage consists of three DAB converters.

The U/I vectors of the PET AC-DC stage with unity power factor ( $i_Q^* = 0$ ) control is shown in Fig.2. For simplicity, the

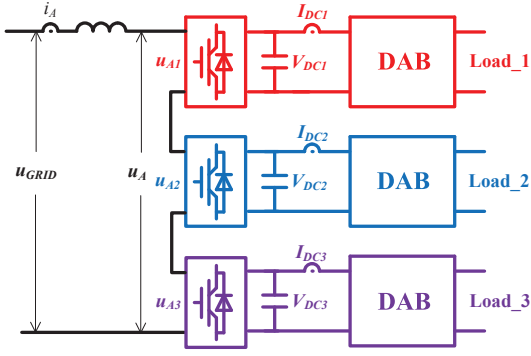


Fig. 1. Multi-Load Power Electronic Transformer

inductor voltage drop is neglected,  $u_A = u_{GRID}$ . The power equation is (1) and voltage equation is (2).

$$\begin{cases} P_1 = I_A \cdot U_{A1} = I_A \cdot m_{A1} \cdot V_{DC} / \sqrt{2} \\ P_2 = I_A \cdot U_{A2} = I_A \cdot m_{A2} \cdot V_{DC} / \sqrt{2} \\ P_3 = I_A \cdot U_{A3} = I_A \cdot m_{A3} \cdot V_{DC} / \sqrt{2} \end{cases} \quad (1)$$

$$U_{GRID} = U_A = U_{A1} + U_{A2} + U_{A3} \quad (2)$$

where  $U_{GRID}$  is the grid RMS voltage;  $I_A$  is the grid RMS current;  $U_{A1}$  is the module #1 AC RMS voltage,  $U_{A2}$  is the module #2 AC RMS voltage and  $U_{A3}$  is the module #3 AC RMS voltage;  $P_1, P_2$  and  $P_3$  are the modules' load power;  $m_{A1}, m_{A2}$  and  $m_{A3}$  are the modules' modulation index.

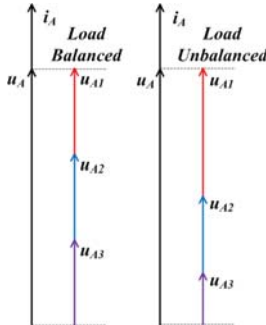


Fig. 2. U/I Vectors Under Unity Power Factor

The operation range of the system is related to another coefficient: the rated modulation index  $m_{rated}$ .  $m_{rated}$  is a pre-designed value which represents the systems DC voltage utilization rate (3). In most applications, the rated modulation is set within the range of (0.7, 0.95). The modulation indexes should not exceed 1. For simplicity, we always assume  $P_1 > P_2 > P_3$  and  $P_1 = 1$  in this paper. The operation range can be easily derived as (4) and can be drawn in Fig.3. The red triangle shows all possible range of unbalanced load power, and the purple region is the available region of unity power factor control.

$$U_{GRID} = 3m_{rated}V_{DC} / \sqrt{2} \quad (3)$$

$$\frac{P_2 + P_3}{P_1} > 3m_{rated} - 1 \quad (4)$$

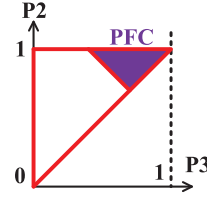


Fig. 3. Operation Range Under Unity Power Factor

### III. REACTIVE COMPONENT INJECTION CONTROL

From section II, it is seen that when the system is using PFC control, the module voltage is always forced to be proportional to the load power. There is no degree of control freedom to avoid overmodulation. In order to handle the overmodulation issue when the load is too unbalanced, the PFC has to be sacrificed. A reactive current and a reactive module voltage are introduced as new control freedoms to handle the overmodulation issue. When the reactive current and reactive module voltage are injected, the U/I vectors are then as Fig.4 and the power equation is as (5)

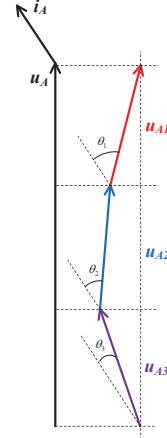


Fig. 4. U/I Vectors Under Reactive Component Injection Control

$$\begin{cases} P_1 = I_A \cdot U_{A1} \cdot \cos\theta_1 \\ P_2 = I_A \cdot U_{A2} \cdot \cos\theta_2 \\ P_3 = I_A \cdot U_{A3} \cdot \cos\theta_3 \end{cases} \quad (5)$$

The basic idea is to increase the amplitude of grid current by injecting a reactive component. When  $I_A$  is increased, the  $U_{A1}$  will have a chance to decrease. If we let the  $I_A \cos\theta_1$  term in (5) be larger than the  $I_A$  term in (1), the  $U_{A1}$  will decrease thus avoiding overmodulation.

### IV. THREE SPECIFIC ALGORITHMS

In this paper, three specific algorithms of the reactive component injection control strategy are proposed.

### A. The Shared $U_D$ Algorithm

This subsection introduces a easy-implemented algorithm—the Shared  $U_D$  algorithm. Which always sets equal D-axis voltage to each module, as (6)

$$U_{D1} = U_{D2} = U_{D3} = \frac{U_{GRID}}{3} \quad (6)$$

where  $U_{D1}$ ,  $U_{D2}$  and  $U_{A3}$  are the modules' D axis RMS voltage.

The reactive current is set by the following steps: 1, measure the load powers and derive the average load power as (7); 2, find the difference between each load power and the average load power,  $\Delta P$ , as (8); 3, set the reactive current according to (9), so the module which has the maximum  $\Delta P$  will operate with a full AC output voltage, while the other two modules will generate an AC voltage smaller than full voltage, which avoids overmodulation.

$$P_{AVR} = \frac{P_1 + P_2 + P_3}{3} \quad (7)$$

$$\Delta P_k = P_k - P_{AVR} \quad k = 1, 2, 3 \quad (8)$$

$$I_Q = \frac{\max(|\Delta P_1|, |\Delta P_2|, |\Delta P_3|)}{\sqrt{\frac{V_{DC}^2}{2} - (\frac{1}{3}U_{GRID})^2}} \quad (9)$$

The control block diagram is shown in Fig.5. It should be noted that, there are two methods to achieve DC voltage balancing: the first method is just as Fig.5 shows, by setting D axis voltage at  $1/3$  for each module while trimming the Q axis voltage through a DC voltage balancing loop; the second method, in contrast, is to set the Q axis voltage by some mathematical calculation while trimming the D axis voltage through a DC voltage balancing loop. Both the two methods will lead to a same final steady state result. Comparing these two methods, the first one is easier implemented; the second one is a little more complicated, but it tends to have a better performance in cases when  $I_Q$  is too small to achieve DC voltage balancing.

The Shared  $U_D$  algorithm is full-range available, which is an advantage over the two other algorithms in the latter part.

### B. The Minimum $I_Q$ Algorithm

The Minimum  $I_Q$  Algorithm always ensure  $u_{A1}$  be in phase with  $i_A$  meanwhile  $m_{A1} = 1$ . At certain  $P_1, P_2$  and  $P_3$  ( $P_1 > P_2 > P_3$ ), this can ensure a minimum reactive current as well as a minimum overall current. The algorithm is as (10).

Note that (10) only determines  $i_Q$ ,  $U_{D1}$  and  $U_{Q1}$ . The AC reference for the other two modules,  $u_2$  and  $u_3$ , are generated by a DC voltage balancing loop in the latter part of this subsection.

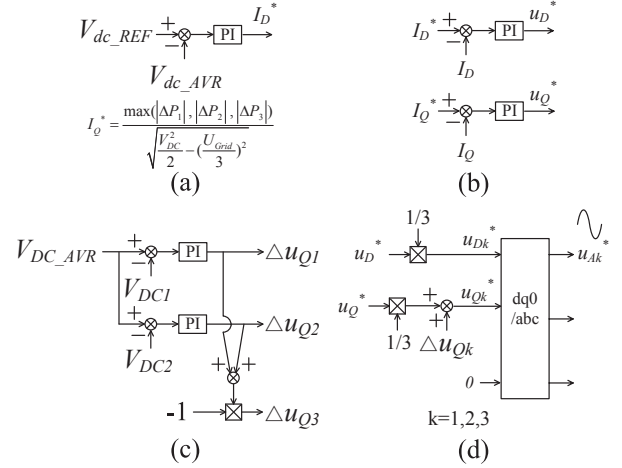


Fig. 5. Control Blocks of Shared  $U_D$  Algorithm

$$\begin{cases} U_{D1} = \frac{I_D V_{DC}^2}{2P_1} = \frac{(1 + \frac{P_2+P_3}{P_1})V_{DC}^2}{2U_{GRID}} \\ U_{Q1} = \sqrt{\frac{V_{DC}^2}{2} - U_{D1}^2} \\ I_Q = \frac{P_1 - U_{D1}I_D}{\sqrt{\frac{V_{DC}^2}{2} - U_{D1}^2}} \\ U_{D2} + U_{D3} = U_{GRID} - U_{D1} \\ U_{Q2} + U_{Q3} = -U_{Q2} \end{cases} \quad (10)$$

The available range of Minimum  $I_Q$  Algorithm is derived by a geometric approach which summarizes all possible position and length of  $u_{A1}$ ,  $u_{A2}$  and  $u_{A3}$  vectors.

The  $u_{A1}$ ,  $u_{A2}$  and  $u_{A3}$  vectors have to meet several constraints. Firstly, the sum of all three modules' AC voltages should be equal to the grid voltage (11). It can also be written in form of modulation index (12).

$$u_{A1} + u_{A2} + u_{A3} = u_{GRID} \quad (11)$$

$$m_{A1} + m_{A2} + m_{A3} = 3m_{rated} \quad (12)$$

Secondly, the  $u_{A1}$  is full in amplitude, that is (13)

$$m_{A1} = 1 \quad (13)$$

Thirdly, the other two modules' AC voltages should not exceed full amplitude (14)

$$\begin{cases} m_{A2} \leq 1 \\ m_{A3} \leq 1 \end{cases} \quad (14)$$

With these constraints, the operation range can be derived by Fig.6.  $\theta$  is the angle between  $u_{A1}$  and  $u_{GRID}$ . Under different  $\theta$ , the maximum component of  $u_{A2}$  on the direction of  $u_{A1}$ , as well as the minimum component of  $u_{A3}$  on the direction of  $u_{A1}$  can be found. As long as they are found, the upper

limit of  $P_2$  and the lower limit of  $P_3$  under different  $\theta$  are also found, then the available range of Minimum  $I_Q$  Algorithm can be derived.

As the  $\theta$  turns bigger, the boundary cases are shown in Fig.6(a)-(e).

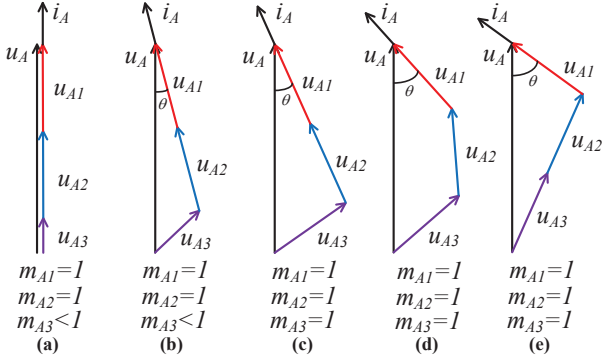


Fig. 6. Boundary U/I Vectors of Minimum IQ Algorithm

Fig.6(a) shows the PFC case. In PFC case,  $P_2$  can be maximized by setting  $m_{A2} = 1$  meanwhile making  $u_{A2}$  in phase with  $u_{A1}$ .

Fig.6(b) shows a reactive component injection case. In this case,  $u_{A2}$  can still be set at  $m_{A2} = 1$  meanwhile in phase with  $u_{A1}$ . As the  $\theta$  is within a certain limit,  $m_{A3} < 1$  is ensured. In this case, the upper limit of  $P_2$  and the lower limit of  $P_3$  is as (15)

$$\begin{cases} P_2 + P_3 = 3\cos(m_{rated}) - 1 \\ P_{2\_MAX} = 1 \\ P_{3\_MIN} = 3\cos(m_{rated}) - 2 \end{cases} \quad (15)$$

Fig.6(c) shows the critical point of the Fig.6(b) case. In Fig.6(c), the  $u_{A2}$  can still be set at full modulation index meanwhile in phase with  $u_{A1}$ ,  $P_{2\_MAX} = P_1$ . At the same time, the  $u_{A3}$  also reaches full amplitude,  $m_{A3} = 1$ . The vectors:  $3m_{rated}$ , 2 and 1, can form a closed triangle.

Fig.6(d) shows the case when  $\theta$  exceeds the case in Fig.6(c). The maximum  $P_2$  can be obtained by setting  $u_{A2}$  at full modulation index, but no longer able to be in phase  $u_{A1}$ . In this case, the vectors form a quadrilateral whose side lengths are:  $3m_{rated}$ , 1, 1 and 1. The upper limit of  $P_2$  and the lower limit of  $P_3$  is as (16).

$$\begin{cases} P_2 + P_3 = 3m_{rated}\cos(\theta) - 1 \\ P_{2\_MAX} = \frac{3m_{rated}\cos(\theta) - 1}{2} + \frac{\sqrt{3 - 9m_{rated}^2 + 6m_{rated}\cos(\theta)}}{\sqrt{1 + 9m_{rated}^2 - 6m_{rated}\cos(\theta)}} \cdot \frac{3m_{rated}\sin(\theta)}{2} \\ P_{3\_MIN} = \frac{3m_{rated}\cos(\theta) - 1}{2} - \frac{\sqrt{3 - 9m_{rated}^2 + 6m_{rated}\cos(\theta)}}{\sqrt{1 + 9m_{rated}^2 - 6m_{rated}\cos(\theta)}} \cdot \frac{3m_{rated}\sin(\theta)}{2} \end{cases} \quad (16)$$

Fig.6(e) shows the critical point of Fig.6(d). In this case, the  $u_{A2}$  and  $u_{A3}$  are synchronized so the quadrilateral in Fig.6(d) goes to a triangle again, whose side lengths are  $3m_{rated}$ , 1 and 2.

The  $\theta$  can not go bigger than Fig.6(e), otherwise the vectors will not be able to form a closed polygon.

Summarizing all the results from Fig.6,(15) and (16), the available range of Minimum  $I_Q$  Algorithm can be drawn in Fig.7 as the blue line surrounded area.

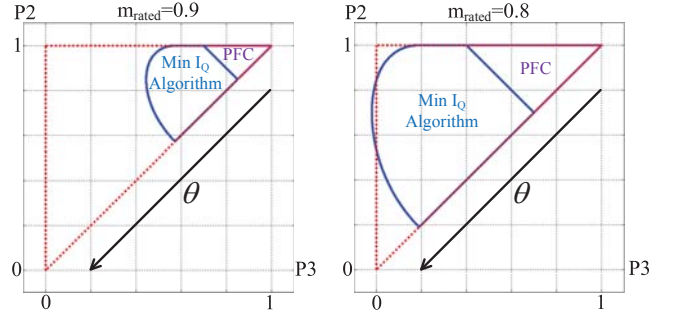


Fig. 7. Operation Range Under Minimum IQ Algorithm

The control implementation is a little complicated. The  $I_Q^*$  is given by (10).  $U_{D1}$  is given by (10) while  $U_{D1}$  is given by its own DC voltage loop, as in Fig.8. Again, here we could also set  $U_{Q1}$  according to (10) while letting  $U_{D1}$  be given by the DC voltage loop.

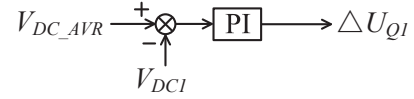


Fig. 8. VDC1 Control Loop

The DC balancing loop of #2 and #3 has two forms according to different  $\theta$ .

When  $\theta$  is small, the location of operating point will locate in region A as Fig.9(a) shows. In region A, the trajectory of  $u_{A2}$  and  $u_{A3}$  is shown in Fig.9(b). When the system is working at M1 point where  $P_2 = P_3$ , the  $u_{A2}$  and  $u_{A3}$  will be the same at  $\frac{u_A - u_{A1}}{2}$ . When the system is working at M2 point where  $P_2$  reaches the maximum value while  $P_3$  reaches the minimum value, the  $u_{A2}$  and  $u_{A3}$  will be as Fig.6(b), where  $m_{A2} = 1$  and  $u_{A2}$  be in phase with  $u_{A1}$ , meanwhile  $m_{A3} < 1$ . Therefore, the adjustment direction should be chosen as the green arrow, which is  $u_{A1} - \frac{u_A - u_{A1}}{2}$ . The balancing loop is shown by Fig.10 and (17).

When  $\theta$  is big, the location of operating point will locate in region B as Fig.9(a) shows. In region B, the trajectory of  $u_{A2}$  and  $u_{A3}$  is shown in Fig.9(c). When the system is working at N1 point where  $P_2 = P_3$ , the  $u_{A2}$  and  $u_{A3}$  will be the same at  $\frac{u_A - u_{A1}}{2}$ . When the system is working at N2 point where  $P_2$  reaches the maximum value while  $P_3$  reaches the minimum value, the  $u_{A2}$  and  $u_{A3}$  will be as Fig.6(d), where  $m_{A2} = m_{A3} = 1$ . Therefore, the adjustment direction should

be chosen as the green arrow, which is vertical to  $u_A - u_{A1}$ . The balancing loop is shown by Fig.10 and (18).

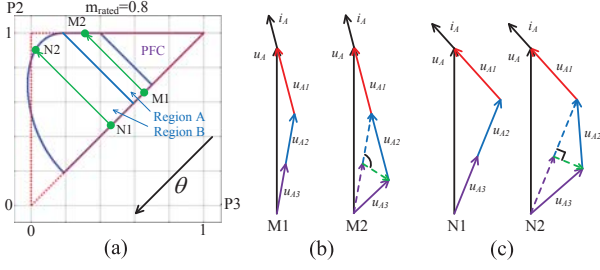


Fig. 9. U/I Vectors Under Minimum IQ Algorithm

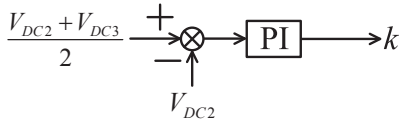


Fig. 10. VDC2 and VDC3 Control Loop

$$\begin{cases} u_{A2} = \frac{u_A - u_{A1}}{2} + k \cdot \frac{u_{A1} - \frac{u_A - u_{A1}}{2}}{|u_{A1} - \frac{u_A - u_{A1}}{2}|} \\ u_{A3} = u_A - u_{A1} - u_{A2} \end{cases} \quad (17)$$

$$\begin{cases} u_{A2} = \frac{u_A - u_{A1}}{2} + k \cdot \perp \left( \frac{u_A - u_{A1}}{|u_A - u_{A1}|} \right) \\ u_{A3} = u_A - u_{A1} - u_{A2} \end{cases} \quad (18)$$

### C. The Maximum UM Algorithm

As have stated above, the Minimum  $I_Q$  Algorithm is unable to cover all the required region. Therefore, a Maximum  $U_M$  Algorithm is proposed for the uncovered region.

The region is derived through the following logical process:

1, At the boundary of Minimum  $I_Q$  Algorithm region, there is always  $m_{A1} = m_{A2} = m_{A3} = 1$  and  $i_A$  be in phase with  $u_{A1}$ . Like J1 and K1 in Fig.11.

2, Starting from the Minimum  $I_Q$  Algorithm boundary, if the voltage vectors are kept while the reactive current is increased, the system operating point will cover all the region which is uncovered by the Minimum  $I_Q$  Algorithm. As an example, if the system starts from J1(K1), by adding reactive current, the system operating point will move through J2(K2) to J3(K3), like Fig.11 and Fig.12 shows.

It is straightforward seen that, by setting  $m_{A1} = m_{A2} = m_{A3} = 1$ , the required  $I_Q$  must be the minimized value. Otherwise, if the  $I_Q$  continues to decrease, the modules will have to increase their AC voltages to maintain the power, which results in overmodulation. As this algorithm features  $m_{A1} = m_{A2} = m_{A3} = 1$ , it is called the Maximum  $U_M$  Algorithm

The control objective of this method is to ensure  $m_{A1} = m_{A2} = m_{A3} = 1$ . The key loops are shown in Fig.13.

Fig.13(a) is the DC voltage balancing loop, which ensures  $V_{DC1} = V_{DC2} = V_{DC3}$ ;

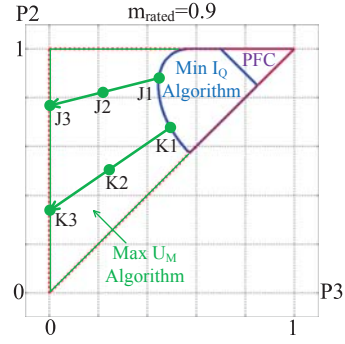


Fig. 11. Operation Range of Maximum UM Algorithm

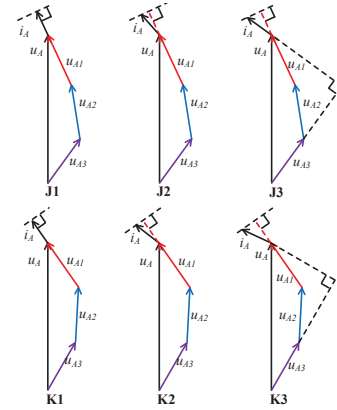


Fig. 12. U/I Vectors of J1/J2/J3 and K1/K2/K3 points in Fig.11

Fig.13(b) is the AC voltage amplitude( $U_M$ ) balancing loop, or the modulation index balancing loop. If one module's AC voltage amplitude is smaller than the average, it will increase its D axis voltage. The reason why D axis voltage is able to adjust the AC voltage amplitude can be found in Fig.14. As the Maximum  $U_M$  Algorithm is derived by adding extra reactive component to the Minimum  $I_Q$  Algorithm, the angle of  $i_A$  will always be larger than all the module AC voltages, thus the terminal location of the AC voltages are all to the right side of  $i_A$  like Fig.14 shows. When a module power is constant, the location of its AC voltage vector terminal will be restricted on the corresponding red line which is vertical to  $i_A$ . It is easily obtained that, when the voltage vector terminal moves on its corresponding red line, a larger  $U_D$ (as well as a larger  $U_Q$ ) always corresponds to a larger  $U_M$ . Therefore,  $U_M$  can be adjusted by  $U_D$ (or  $U_Q$ ).

This loop will ensure  $m_1 = m_2 = m_3 = m_{AVR}$ .

Just like what is stated in Shared  $U_D$  algorithm, here we could also exchange the use of  $U_Q$  and  $U_D$ : using  $U_D$  for DC voltage balancing while  $U_Q$  for modulation index balancing, and it would lead to a same final control result.

Fig.13(c) is the  $I_Q$  adjusting loop. The  $I_Q$  will be adjusted according to the modules' average AC voltage amplitude. If  $m_{AVR}$  is smaller than 1, it will indicate that the modules' AC voltage capacity is not fully utilized, then the  $I_Q$  can be decreased. This loop will ensure  $m_{AVR} = 1$ .

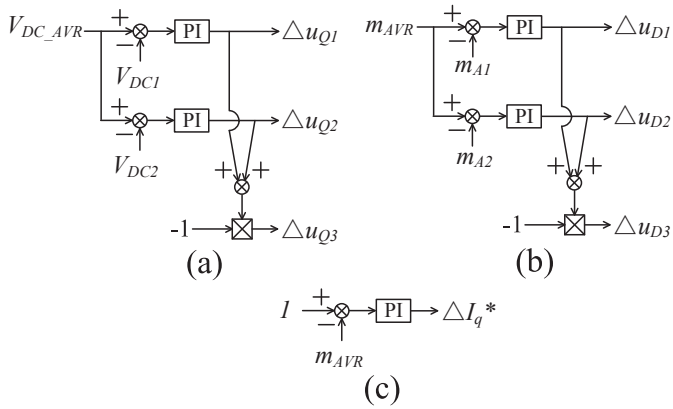


Fig. 13. Control Loops of Maximum UM Algorithm

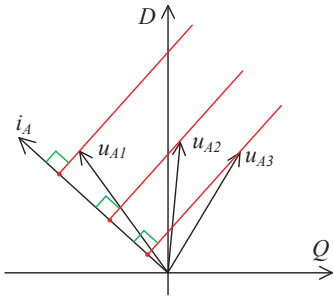


Fig. 14. The Explanation of UM Balancing Loop

## V. SIMULATION RESULTS

In order to verify the proposed reactive component injection control, simulation is carried out in SIMULINK. A single phase three-module PET is built. The parameters of PET AC-DC stage are shown in TABLE I. The DAB stage parameters and waveforms will not be shown because the DAB stage is not concerned in this paper.

TABLE I. PET AC-DC Stage Parameters

Grid Voltage	220V(RMS)
Module Number	3
Rated Power	1500W(Each Module)
DC voltage	130V
$m_{rated}$	0.8
Switching Frequency	10kHz(Each Module)
Inductor	1mH

In order to verify all the three algorithms, two sets of simulation are done. The operating points are marked in Fig.15.

### A. $P_1:P_2:P_3=1:0.8:0.2$

$P_1 : P_2 : P_3 = 1 : 0.8 : 0.2$ , this point is located within the available area of Minimum  $I_Q$  Algorithm. Two algorithms are used to control the system, the Shared  $U_D$  algorithm and the Minimum  $I_Q$  Algorithm, then the outputs are compared.

Fig.16 shows the grid voltage/current and the modulation waves under Shared  $U_D$  algorithm. As  $P_1 : P_2 : P_3 = 1 :$

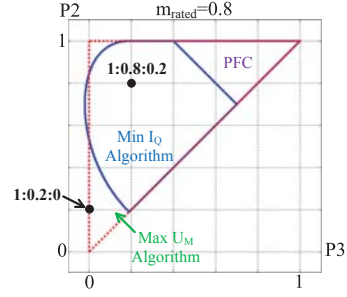


Fig. 15. Two Simulated Points

$0.8 : 0.2$ , there is  $|\Delta P_3| > |\Delta P_1| > |\Delta P_2|$ , according to the theory of Shared  $U_D$  algorithm, the control result should be  $1 = m_{A3} > m_{A1} > m_{A2}$ . This results is verified by the waves.

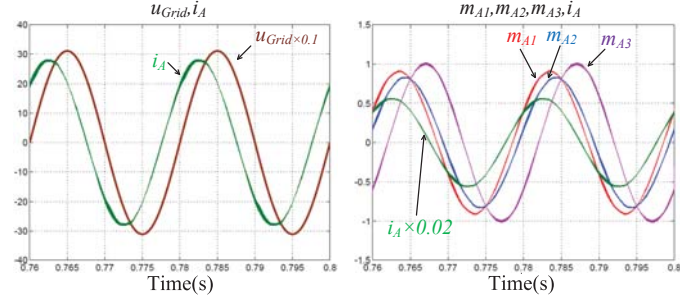


Fig. 16. P1:P2:P3=1:0.8:0.2 under Shared UD Algorithm

Fig.17 shows the grid voltage/current and the modulation waves under Minimum  $I_Q$  algorithm. According to the theory of Minimum  $I_Q$  algorithm, the control result should be  $m_{A1} = 1$  and  $u_{A1}$  be in phase with  $i_A$ . This results is verified by the waves.

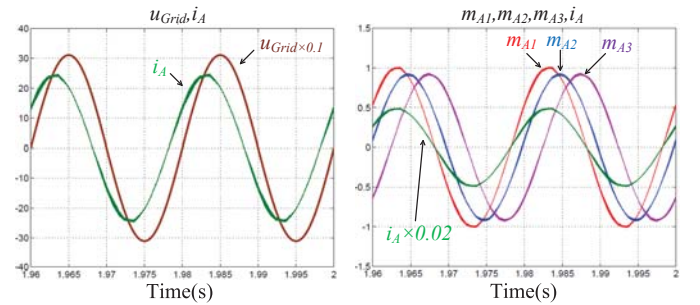


Fig. 17. P1:P2:P3=1:0.8:0.2 under Minimum IQ Algorithm

The current amplitude of Fig.17 is smaller than that of Fig.16, which proves that the Minimum  $I_Q$  algorithm requires the smallest  $I_Q$  as well as the smallest current amplitude.

### B. $P_1:P_2:P_3=1:0.2:0$

$P_1 : P_2 : P_3 = 1 : 0.2 : 0$ , this point is located outside of the available area of Minimum  $I_Q$  Algorithm. Two algorithms

are used to control the system, the Shared  $U_D$  algorithm and the Maximum  $U_M$  Algorithm, then the outputs are compared.

Fig.18 shows the grid voltage/current and the modulation waves under Shared  $U_D$  algorithm. As  $P_1 : P_2 : P_3 = 1 : 0.2 : 0$ , there is  $|\Delta P_1| > |\Delta P_3| > |\Delta P_2|$ , according to the theory of Shared  $U_D$  algorithm, the control result should be  $1 = m_{A1} > m_{A3} > m_{A2}$ . This results is verified by the waves.

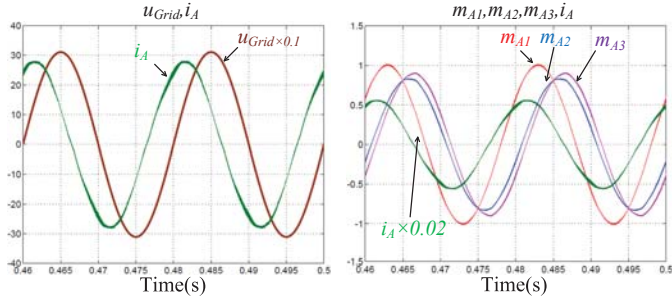


Fig. 18.  $P_1:P_2:P_3=1:0.2:0$  under Shared UD Algorithm

Fig.19 shows the grid voltage/current and the modulation waves under Maximum  $U_M$  algorithm. According to the theory of Maximum  $U_M$  algorithm, the control result should be  $m_{A1} = m_{A2} = m_{A3} = 1$ . This results is verified by the waves.

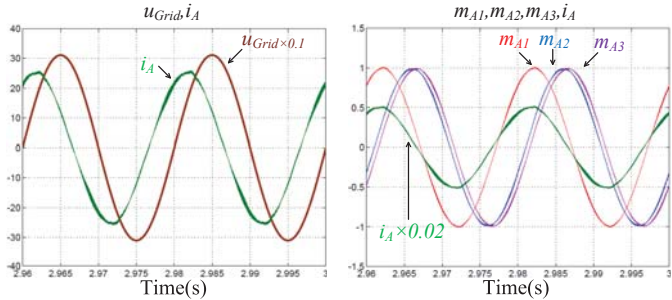


Fig. 19.  $P_1:P_2:P_3=1:0.2:0$  under Maximum UM Algorithm

The current amplitude of Fig.19 is also smaller than that of Fig.18, which proves that the Maximum  $U_M$  algorithm also requires the smallest  $I_Q$  as well as the smallest current amplitude.

## VI. CONCLUSION

This paper proposes a reactive component injection control strategy to handle the over-modulation issue for the AC-DC stage of multi-output PET. In a modular multi-output PET, the AC-DC stage module power is determined by the load power. When the load power is unbalanced, the AC-DC stage module power, as well as the module AC voltage, will also be unbalanced. If the system just applies unity power factor ( $i_Q^*=0$ ) control, overmodulation will occur.

In order to handle the overmodulation issue, this paper proposed a reactive component injection control to eliminate the overmodulation issue. Including three specific algorithms:

the Shared  $U_D$  algorithm, Minimum  $I_Q$  Algorithm and the Maximum  $U_U$  Algorithm. The basic theory of these algorithms are discussed and their control blocks are shown.

Comparing the three algorithms, the Shared  $U_D$  algorithm is easy implemented and full-range available, but it requires larger reactive current; the Minimum  $I_Q$  algorithm and Maximum  $U_M$  Algorithm are comparably complicated, only partial-range available, but they can minimize the required reactive current.

The proposed reactive component injection control and its three algorithms are verified by simulation results.

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